

# Direct analysis of *JV*-curves applied to an outdoor-degrading CdTe module

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# Motivation

Measured  $JV$  curves of outdoor exposed modules hold accessible information on module efficiency and its degradation.

Yet, the dependence on irradiance, temperature and the resistances complicates the analysis. Note that these dependencies might change with outdoor exposure.

We take a critical look at the information in  $JV$  curves and extract a minimum parameter set that we test for its physical meaning.

# Approach – Applying the KH formalism<sup>1</sup>

3 step process:

- 1) Individual  $JV$ -curves (raw data) are **determined** by 4 independent **parameters**.
- 2) **Analyze** the **dependence** of the parameters on  $T_{\text{meas}}$ ,  $\phi_{\text{meas}}$ .
- 3) **Reconstruct**  $JV$ -curves at chosen **reference conditions**, analyze parameters and degradation.

# 1) Determine 4 parameters

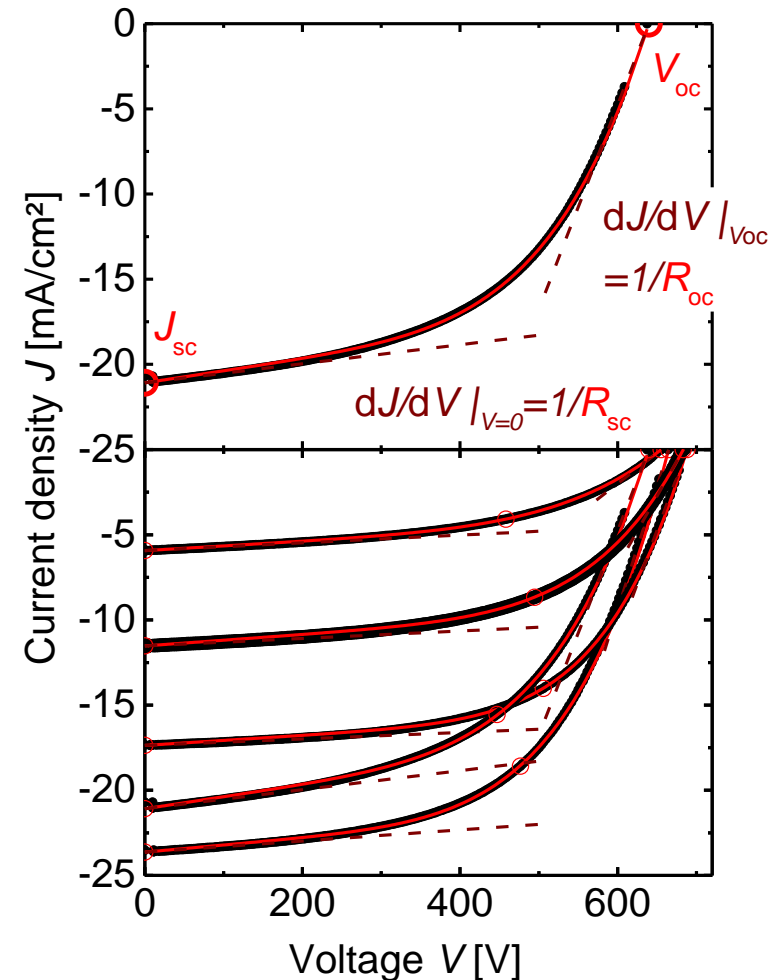
Phenomenological equation<sup>1</sup> is fitted to the measured data

$$J(V) = J_{sc} \left[ \left(1 - \gamma\right) \frac{V}{V_{oc}} + \gamma \left( \frac{V}{V_{oc}} \right)^m - 1 \right]$$

where

$$\gamma = 1 - \frac{1}{R_{sc}} \frac{V_{oc}}{J_{sc}}$$

$$m = \frac{V_{oc} (1/R_{oc} - 1/R_{sc})}{J_{sc} - V_{oc} / R_{sc}}$$

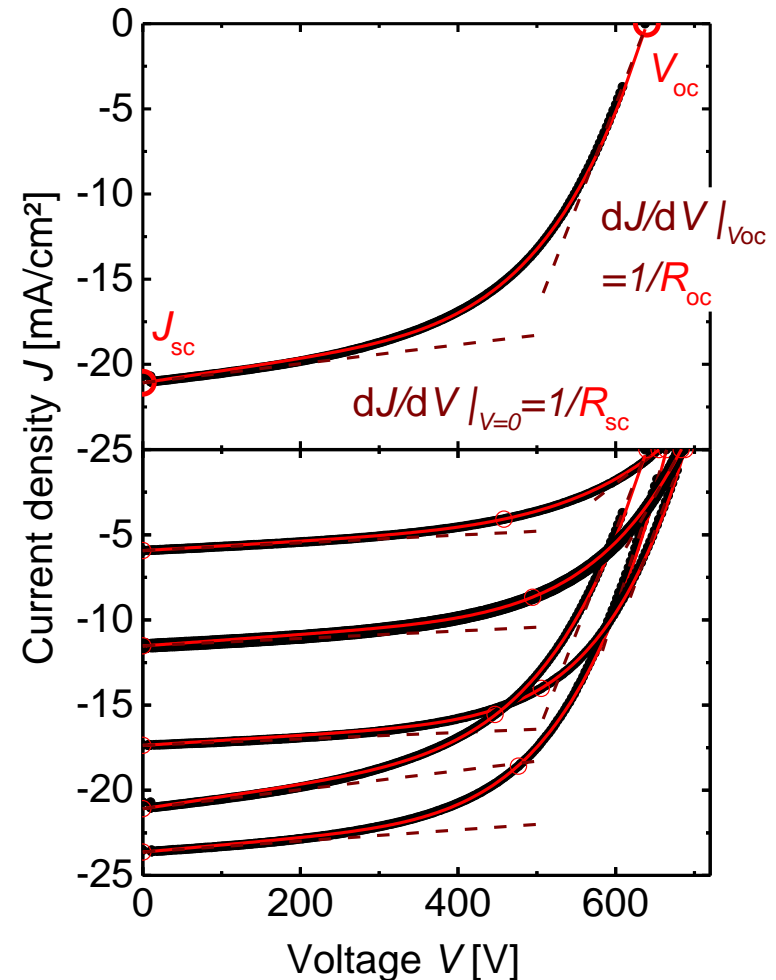


# 1) Determine 4 parameters

Phenomenological equation is fitted to the measured data

$$J(V) = J_{sc} \left[ \left(1 - \gamma\right) \frac{V}{V_{oc}} + \gamma \left( \frac{V}{V_{oc}} \right)^m - 1 \right]$$

The equation by itself has no physical meaning but various, more complex, physically motivated solar cell models are compatible with it<sup>2</sup>.

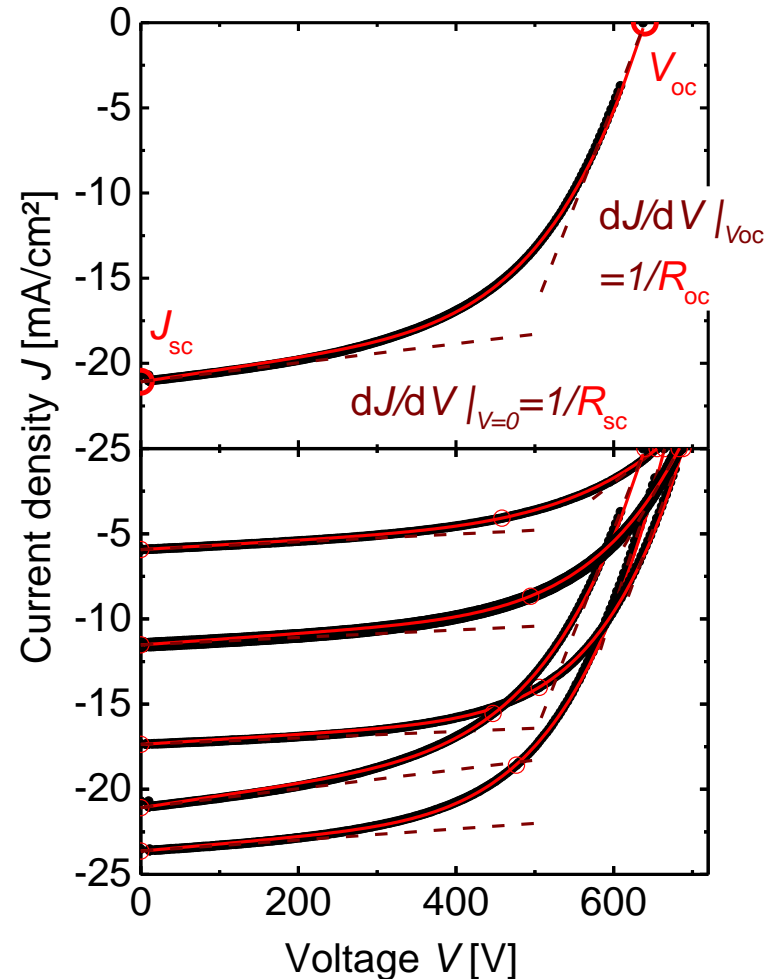


# 1) Determine 4 parameters

## The four parameters

- short circuit current  $J_{sc}$
- open circuit voltage  $V_{oc}$
- differential resistance  $R_{sc}$
- differential resistance  $R_{oc}$

are physically meaningful.



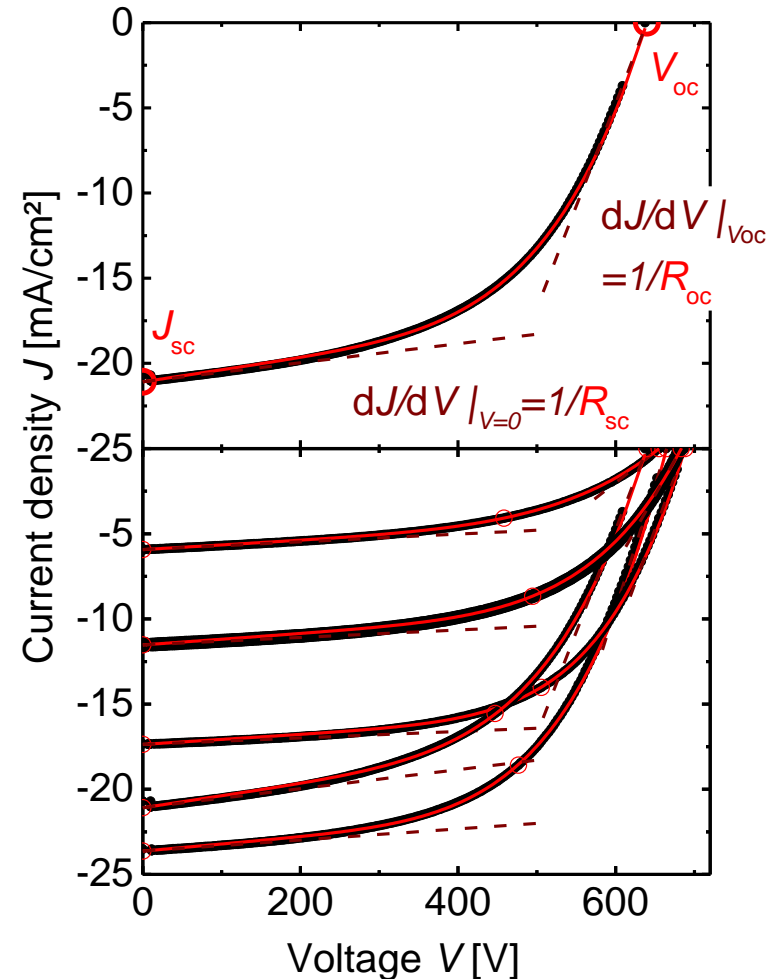
# 1) Determine 4 parameters

## The four parameters

- short circuit current  $J_{sc}$
- open circuit voltage  $V_{oc}$
- differential resistance  $R_{sc}$
- differential resistance  $R_{oc}$

are physically meaningful.

The equation fits the  $JV$  curves reliably in all irradiance ranges and at all stages of degradation.



## 2) Analyze $T_{\text{meas}}$ , $\phi_{\text{meas}}$ dependence

Parameter:  $J_{\text{sc}}$

Assumed dependence:  $J_{\text{sc}}(\phi_{\text{meas}}, T_{\text{meas}}) = \{\alpha_{\text{Jsc}} T_{\text{meas}} + \kappa_{\text{Jsc}}\} \phi_{\text{meas}}$

Value at reference conditions:  $J_{\text{sc@ref}} = J_{\text{sc}}(\phi_{\text{ref}}, T_{\text{ref}}) = \{\alpha_{\text{Jsc}} T_{\text{ref}} + \kappa_{\text{Jsc}}\} \phi_{\text{ref}}$

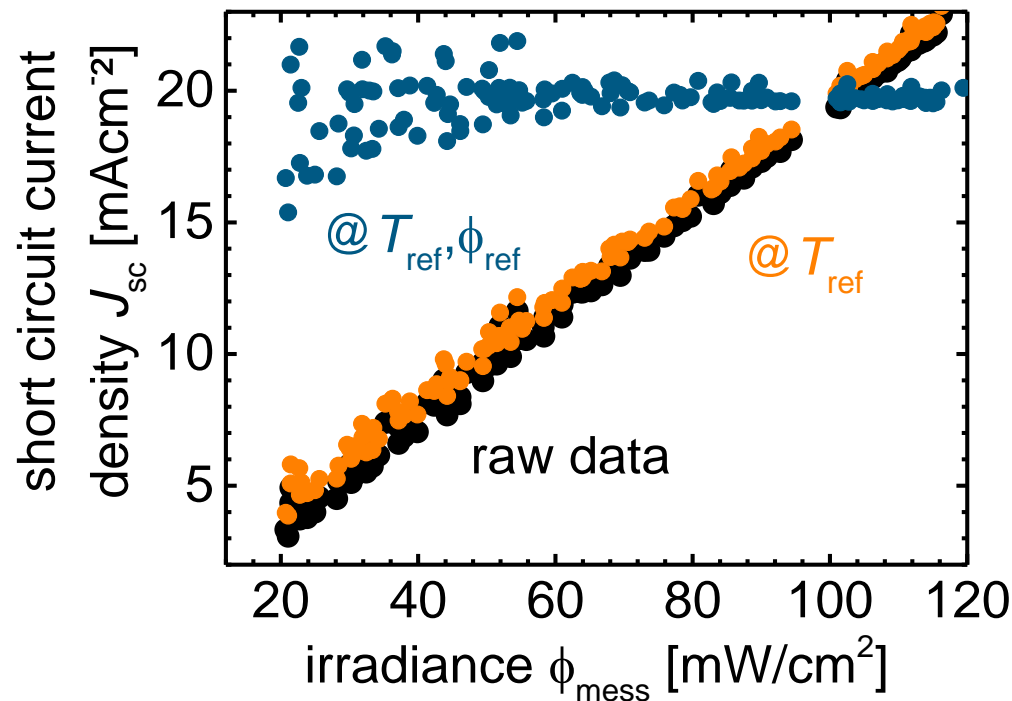
Translation of raw data:  $J_{\text{sc,meas@ref}} = \{\alpha_{\text{Jsc}}(T_{\text{ref}} - T_{\text{meas}})\} \phi_{\text{ref}} + J_{\text{sc}}(\phi_{\text{ref}} / \phi_{\text{meas}})$



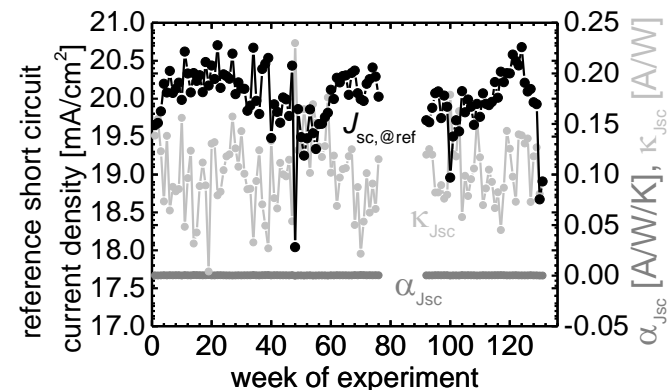
## 2) Analyse $T_{\text{meas}}, \phi_{\text{meas}}$ dependence

Exemplary parameter:  $J_{\text{sc}}$

Assumed dependence:  $J_{\text{sc}}(\phi_{\text{meas}}, T_{\text{meas}}) = \{\alpha_{\text{Jsc}} T_{\text{meas}} + \kappa_{\text{Jsc}}\} \phi_{\text{meas}}$



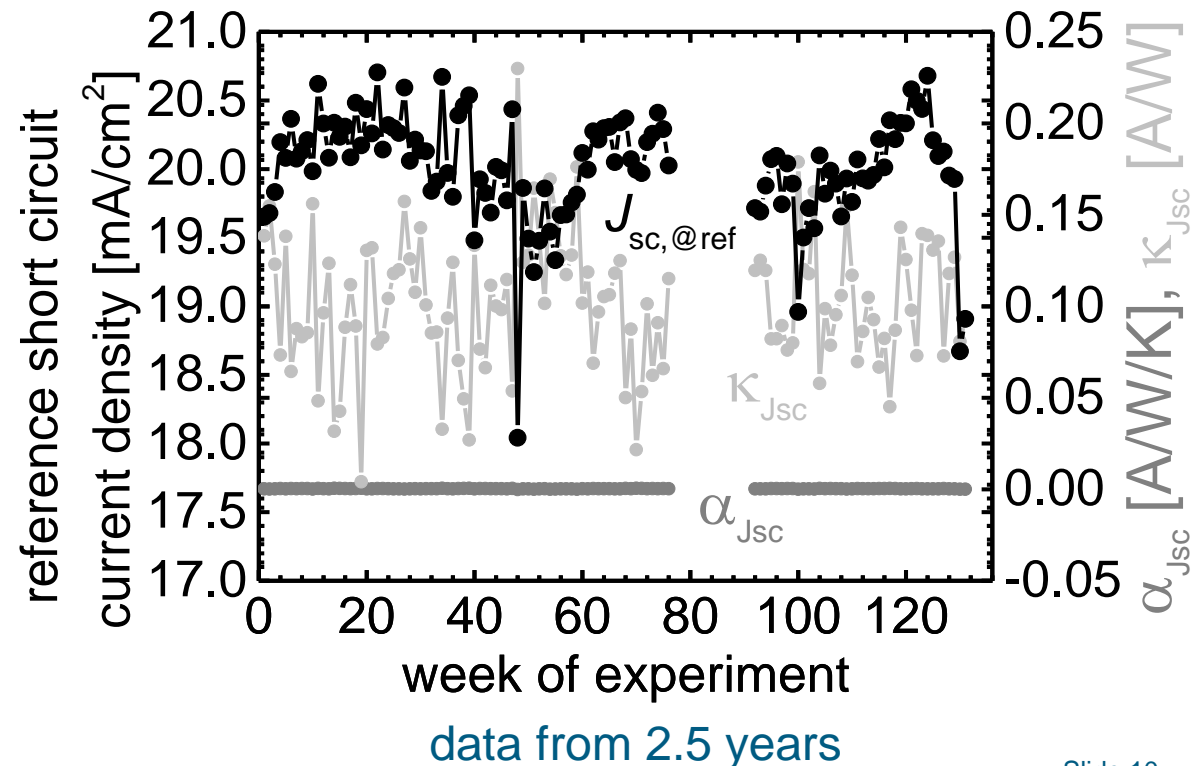
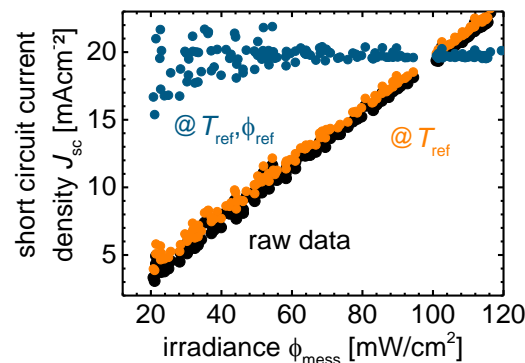
data from 1 week



## 2) Analyse $T_{\text{meas}}, \phi_{\text{meas}}$ dependence

Exemplary parameter:  $J_{\text{sc}}$

Assumed dependence:  $J_{\text{sc}}(\phi_{\text{meas}}, T_{\text{meas}}) = \{\alpha_{\text{Jsc}} T_{\text{meas}} + \kappa_{\text{Jsc}}\} \phi_{\text{meas}}$

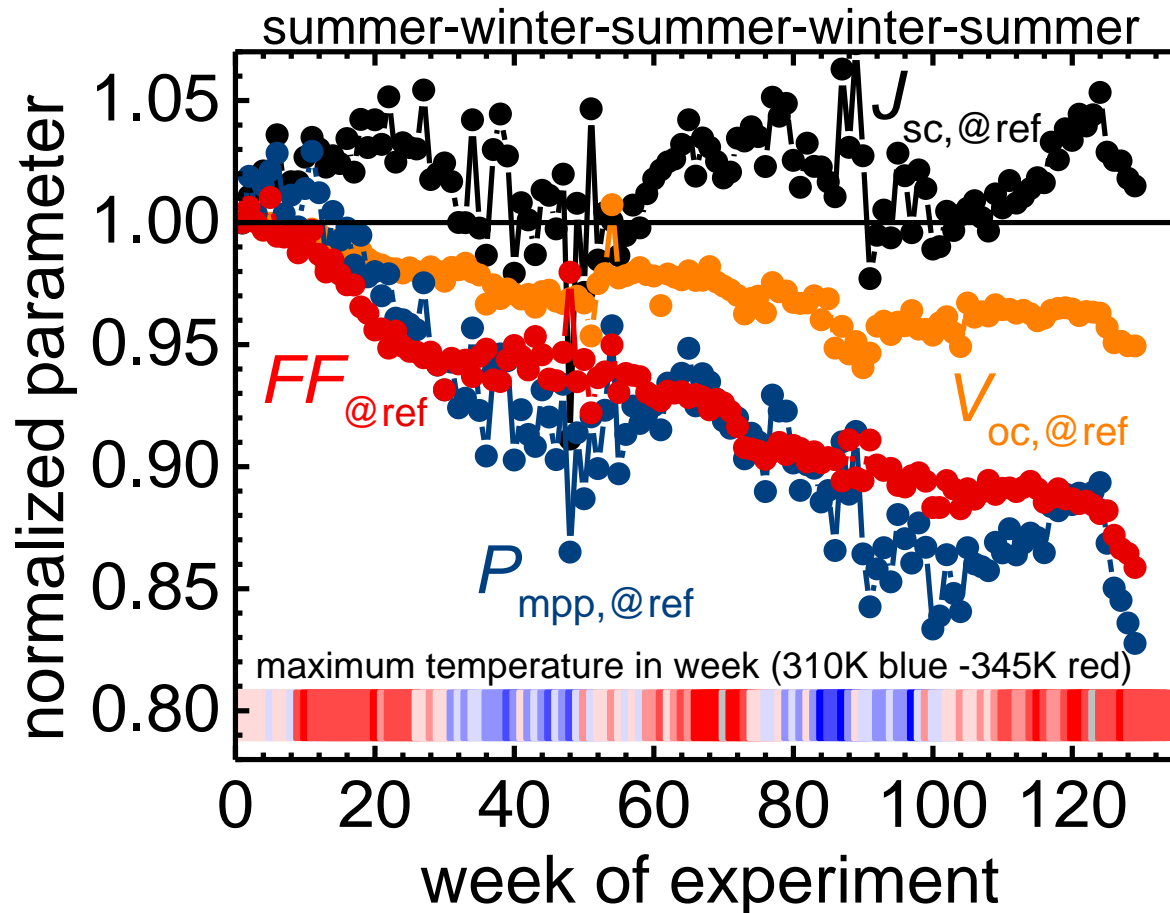


# Approach – Applying the KH formalism

3 step process:

- 1) Determined individual  $JV$ -curve parameters.
- 2) Analyzed  $T_{\text{meas}}, \phi_{\text{meas}}$  dependence  
(Analysis of  $V_{\text{oc}}, R_{\text{sc}}, R_{\text{oc}}$  follows)
- 3) Reconstruct  $JV$ -curves at chosen reference conditions

### 3) Reconstruct at reference conditions



## Findings

Analyses of  $V_{oc}$ ,  $R_{sc}$ , and,  $R_{oc}$  hint at voltage dependent charge carrier collection in CdTe (has been observed before <sup>3</sup>)

→ Let's go back to step 2)

## 2) Analyze $T_{\text{meas}}$ , $\phi_{\text{meas}}$ dependence

Parameter:  $V_{\text{oc}}$

Assumed dependence:

$$V_{\text{oc}}(J_{\text{sc,meas}}, T_{\text{meas}}) = V_{\text{oc}}^0 - \{\alpha_{\text{Voc}} - \varepsilon_{\text{Voc}} \log(J_{\text{sc,meas}})\} T_{\text{meas}}$$

standard diode equation of an illuminated solar cell <sup>4</sup>:

$$V_{\text{oc}} = E_a / q - \{nk / q \log(J_{00}) + nk / q \log(J_{\text{sc}})\} T$$

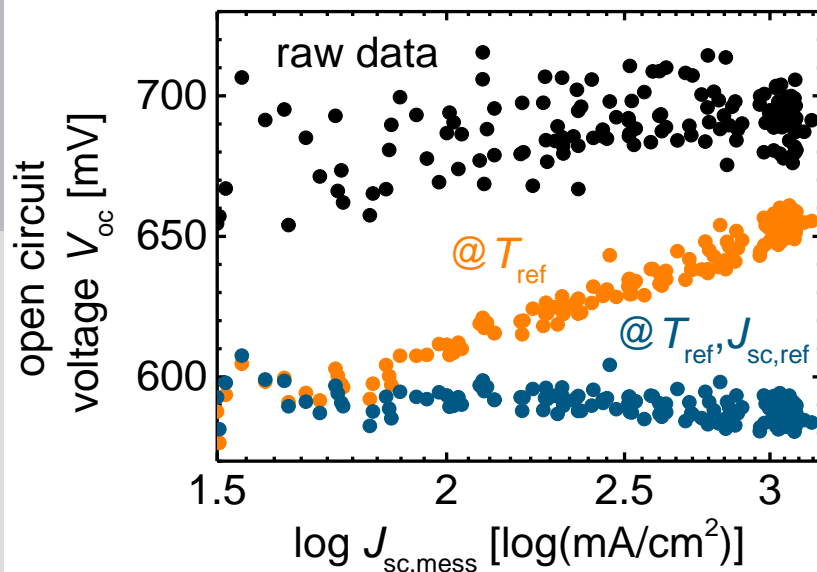
$$\varepsilon_{\text{Voc}} \rightarrow n$$

## 2) Analyze $T_{\text{meas}}$ , $\phi_{\text{meas}}$ dependence

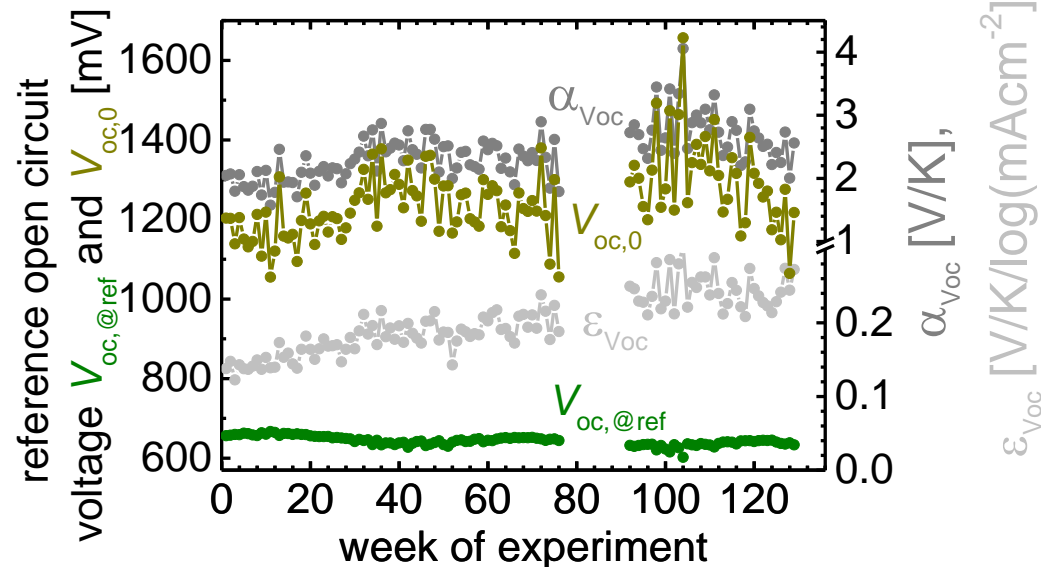
Parameter:  $V_{\text{oc}}$

Assumed dependence:

$$V_{\text{oc}}(J_{\text{sc,meas}}, T_{\text{meas}}) = V_{\text{oc}}^0 - \left\{ \alpha_{\text{Voc}} - \varepsilon_{\text{Voc}} \log(J_{\text{sc,meas}}) \right\} T_{\text{meas}}$$



data from 1 week



data from 2.5 years

## 2) Analyze $T_{\text{meas}}$ , $\phi_{\text{meas}}$ dependence

Parameter:  $R_{\text{oc}}$

Assumed dependence:

$$R_{\text{oc}}(J_{\text{sc,meas}}, T_{\text{meas}}) = R_s + \beta_{\text{Roc}} T_{\text{meas}} / J_{\text{sc,meas}}$$

Werner plot<sup>5</sup> equation

$$R_{\text{oc}} = R_s + \frac{nkT}{q} \frac{1}{J_{\text{sc,meas}}}$$

$$\beta_{\text{Voc}} \rightarrow n$$

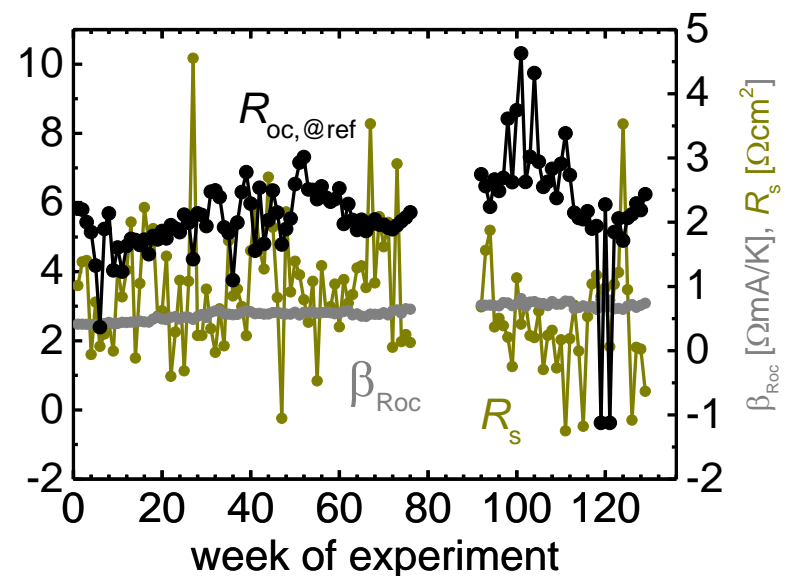
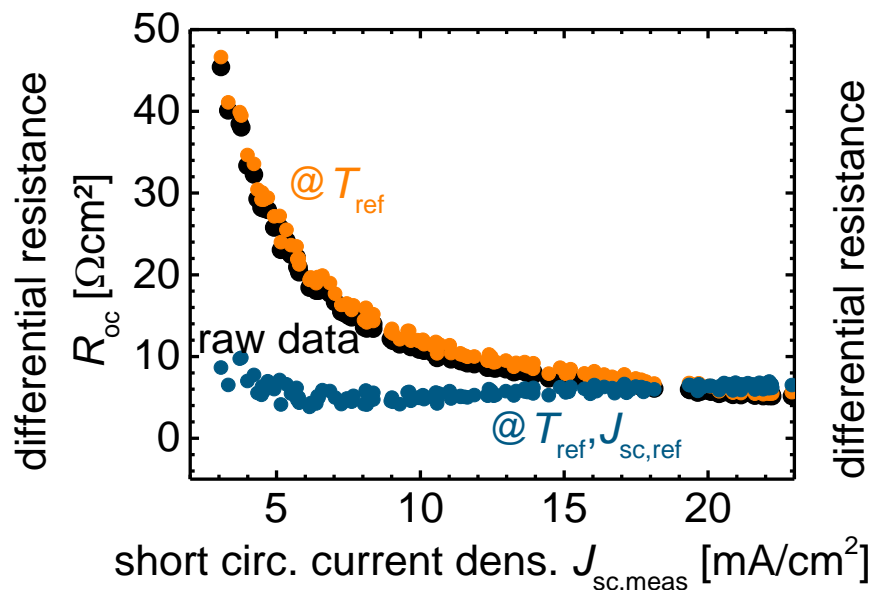


## 2) Analyze $T_{\text{meas}}$ , $\phi_{\text{meas}}$ dependence

Parameter:  $R_{\text{oc}}$

Assumed dependence:

$$R_{\text{oc}}(J_{\text{sc,meas}}, T_{\text{meas}}) = R_s + \beta_{\text{Roc}} T_{\text{meas}} / J_{\text{sc,meas}}$$



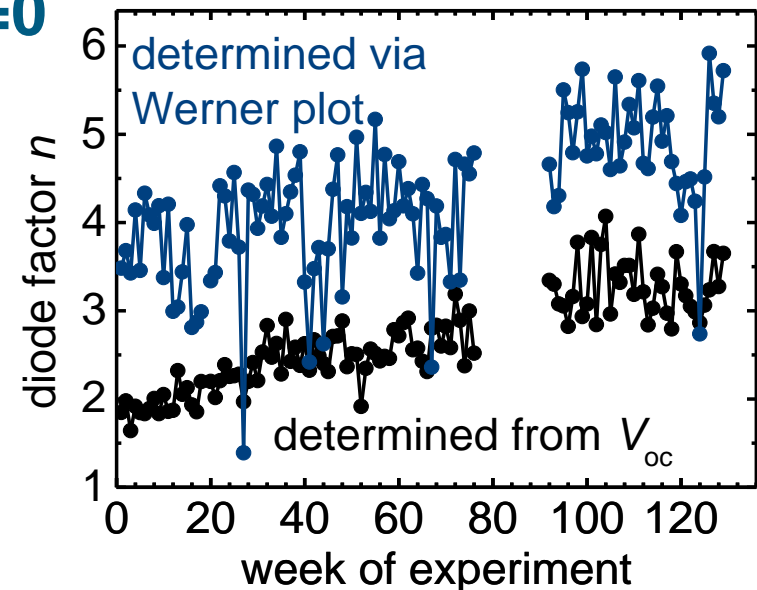
# Findings

Diode factor  $n$  determined from  
 Werner plot<sup>5</sup> **assuming  $dJ_{sc}/dV=0$**

$$R_{oc} = \frac{nkT}{q} \frac{1}{J_{sc,meas}} + R_s$$

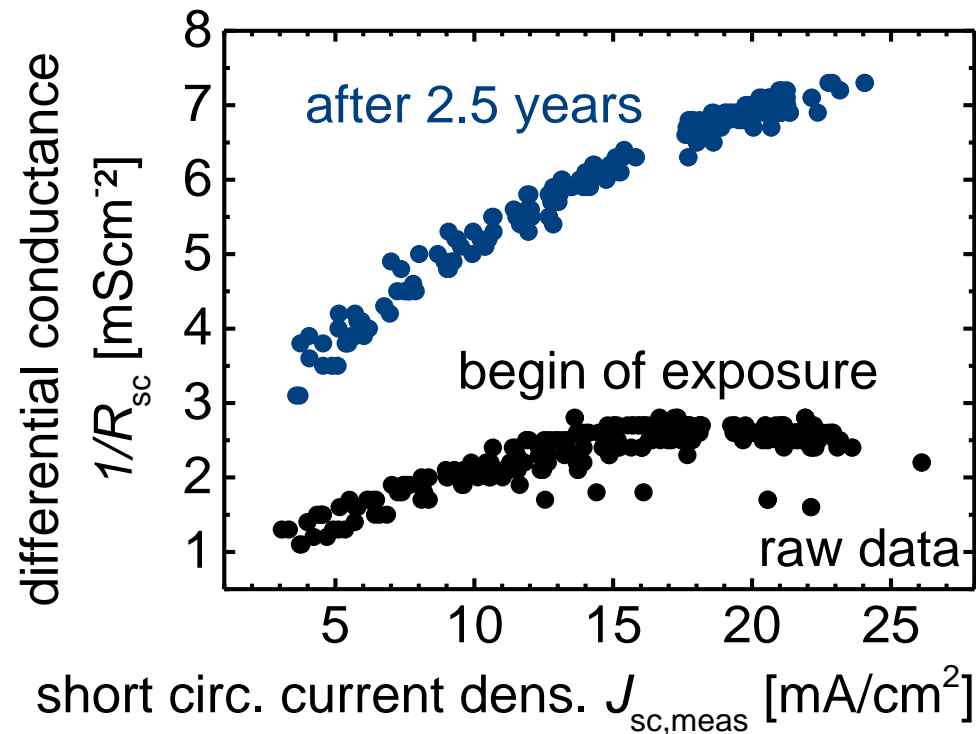
differs from value determined  
 from  $V_{oc}$

$$V_{oc} = E_a / q - nkT / q \log(J_{00}) \\ + nkT / q \log(J_{sc})$$



# Findings

$R_{sc}$  raw data hint at a change in voltage dependent charge carrier collection in CdTe over time



# Summary and Outlook

## Advantages of the Karmalkar-Haneefa formalism

- Only 4 parameters
- Physically meaningful
- Comparison across technologies, interpretation for specific technology and module
- Especially significant in analysis of solar modules with non-negligible resistances
- Easy calculation of effect of losses in energy yield

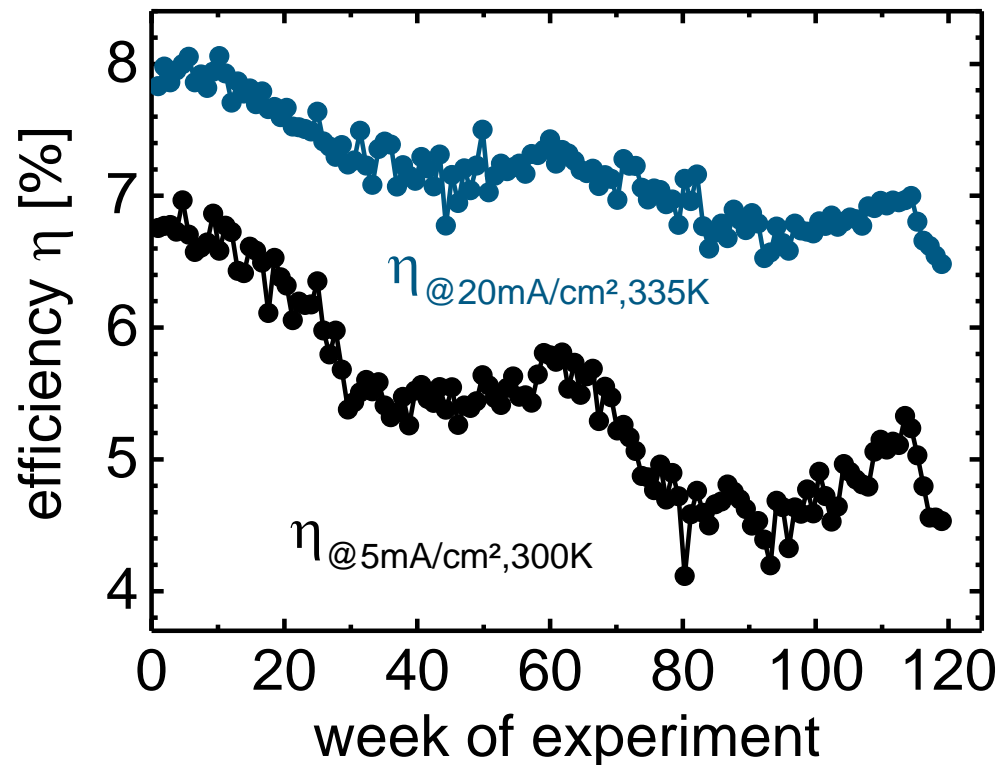
# Thanks

- To the colleagues in Juelich and at the NREL
- To you

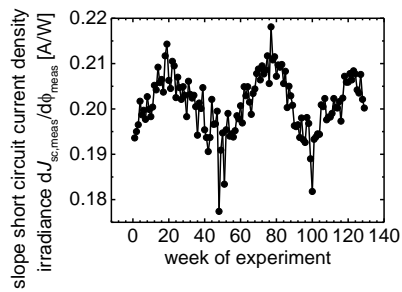
Questions and suggestions are very welcome

## References:

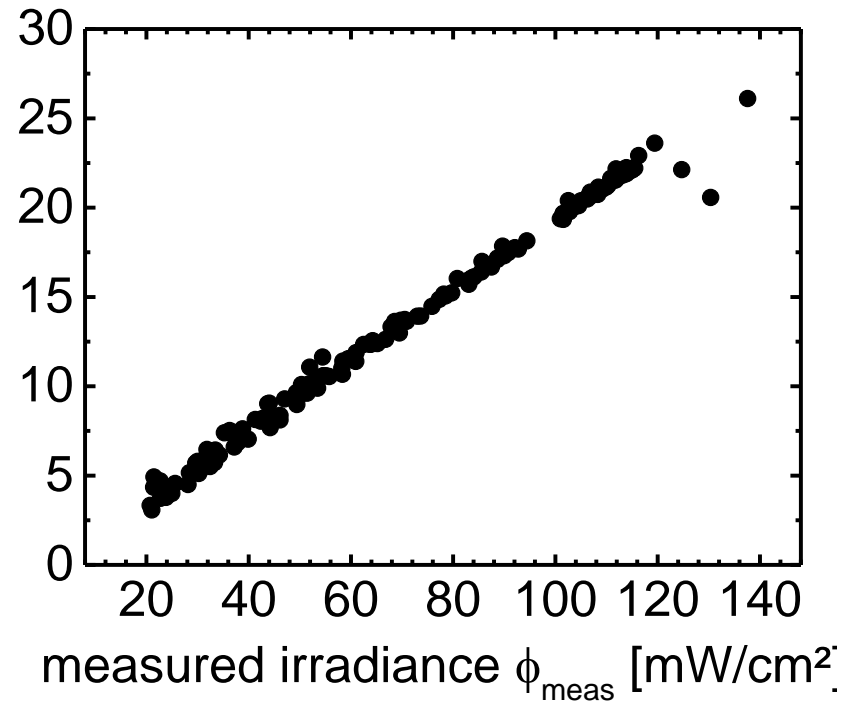
- <sup>1</sup> S. Karmalkar, S. Haneefa, "A physically based explicit J–V model of a solar cell for simple design calculations," *IEEE Electron Device Letters*, vol. 29, pp. 449–451, 2008.
- <sup>2</sup> A. K. Das, S. Karmalkar, "Analytical derivation of the closed-form power law J–V model of an illuminated solar cell from the physics based implicit model," *IEEE Transactions on Electron Devices*, vol. 58, pp. 1176–1181, 2011.
- <sup>3</sup> S. Hegedus, D. Desai, C. Thompson, "Voltage dependent photocurrent collection in CdTe/CdS solar cells," *Prog. Photovolt.: Res. Applic.* 15, 587–602, 2007.
- <sup>4</sup> J. Nelson, *The physics of solar cells*, London, Imperial College Press, 2003.
- <sup>5</sup> J. H. Werner, "Schottky barrier and pn-junction I/V plots- small signal evaluation," *Applied Physics A*, vol. 47, pp. 291–300, 1988.



Taking into account the differential resistances, we find a stronger degradation of the efficiency  $\eta_{@ref}$  for low irradiance intensity/short circuit current density conditions.



measured short circuit  
current density  $J_{sc,meas}$  [mA/cm<sup>2</sup>]



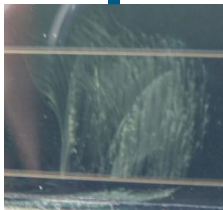
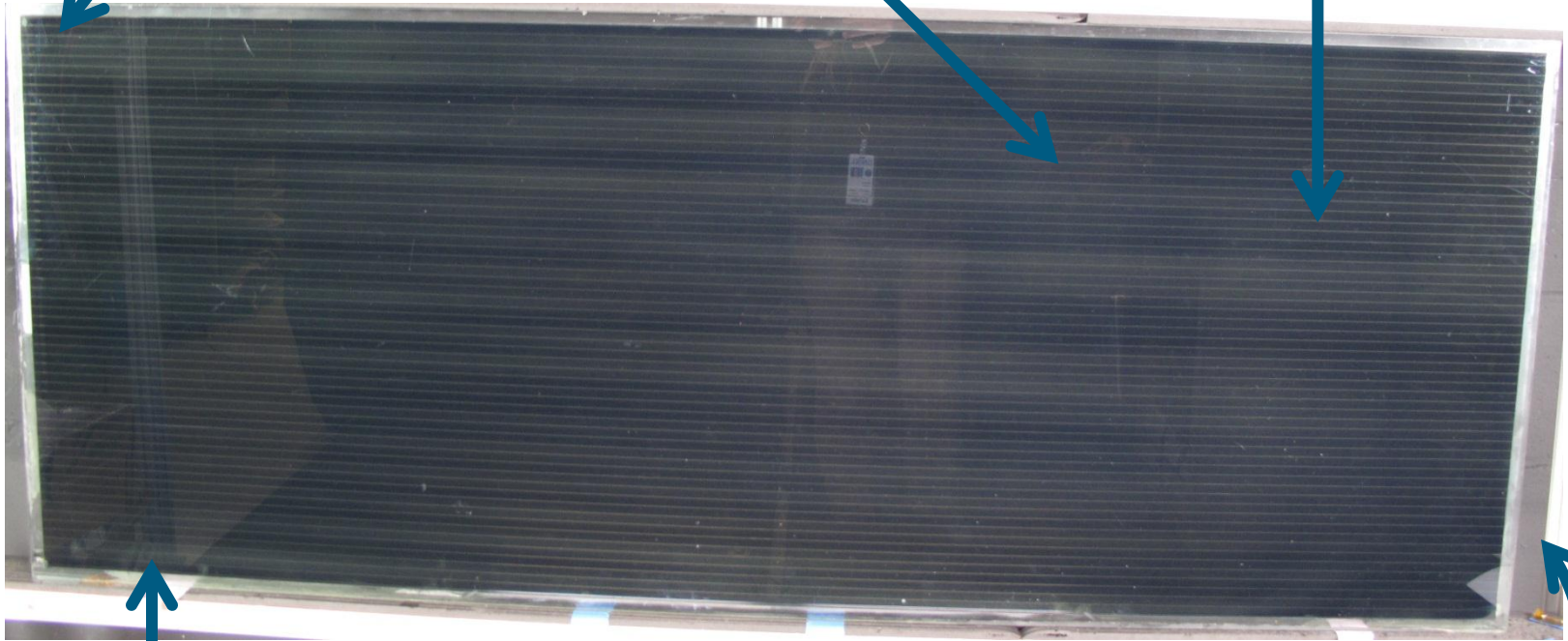
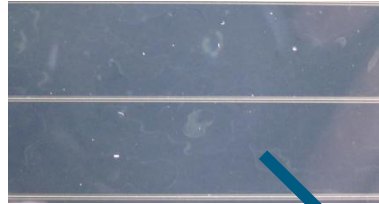
The substitution of irradiance  $\phi_{meas}$  by  $J_{sc,meas}$  when calculating the irradiance dependence of the three parameters  $V_{oc}$ ,  $R_{sc}$  and  $R_{oc}$  is justified by the linear relation between  $J_{sc,meas}$  and  $\phi_{meas}$ .

## Possible origin of degradation

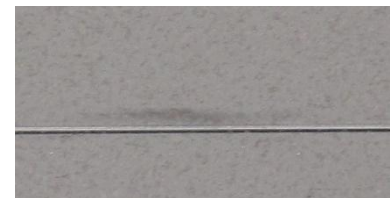
- Corrosion at junction box (at hot and humid days)
- Ion movement (temperature)
- Applied bias – not temperature
- Bias and temperature combined



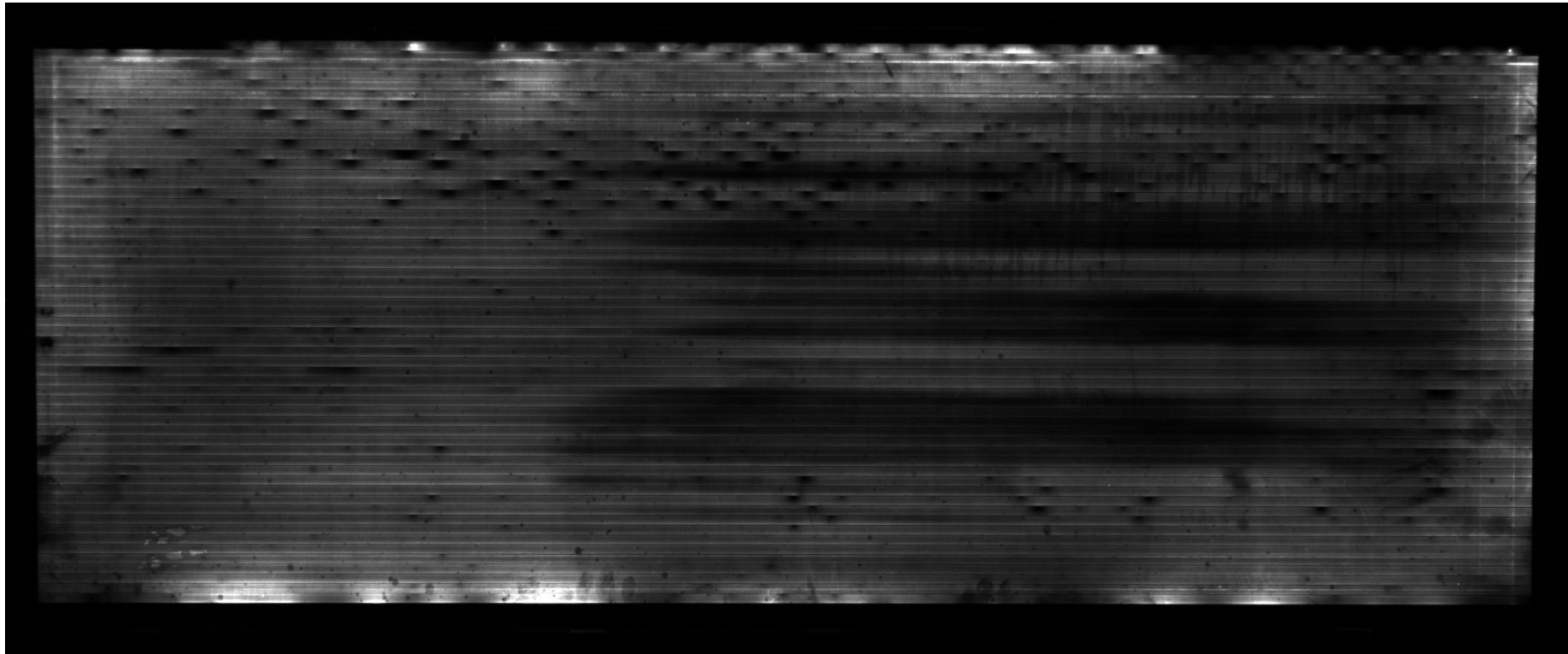
# Visual inspection of module



Corrosion of junction box?



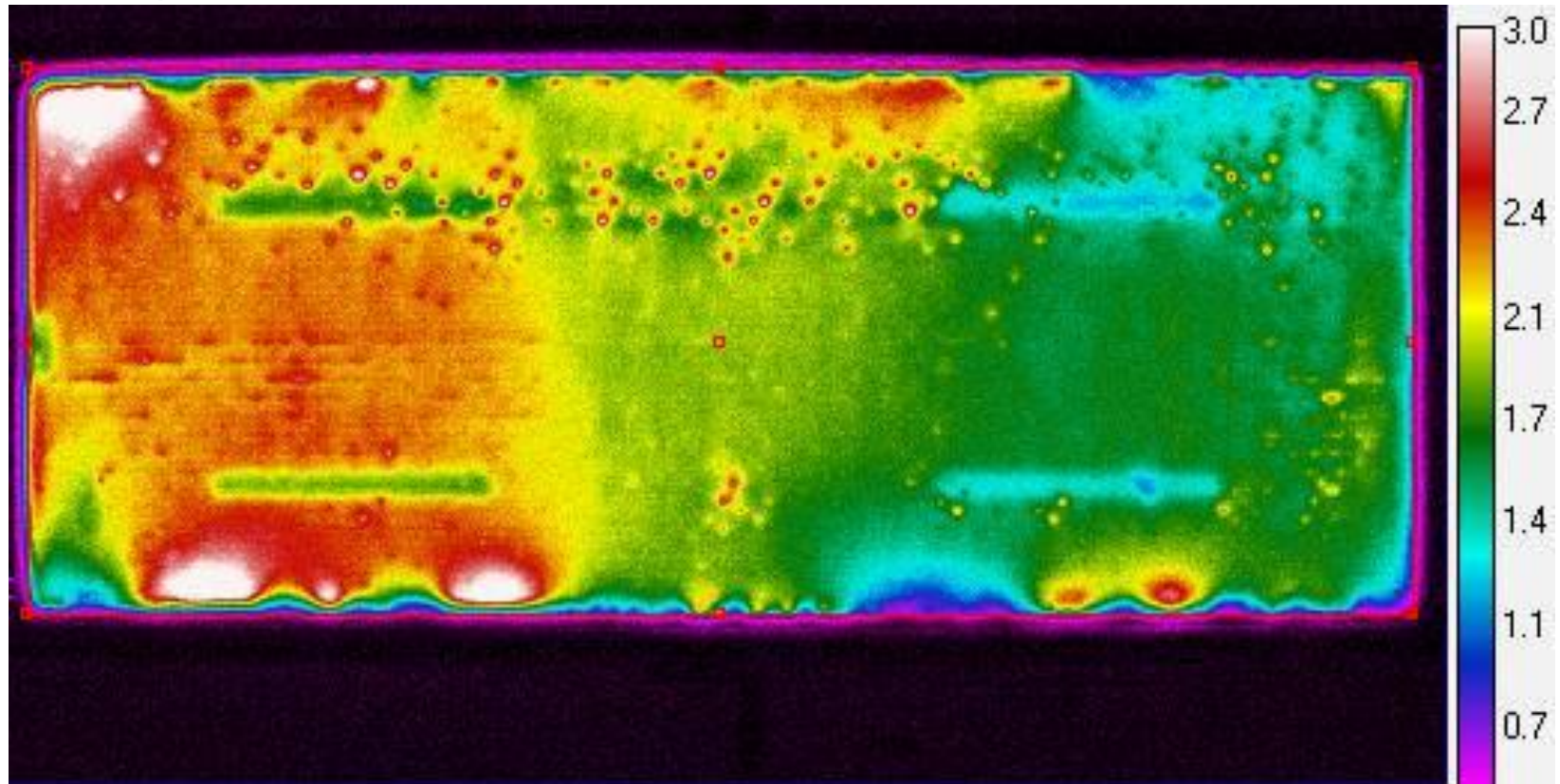
# Electroluminescence



54615mV, 2997 mA applied, 1.28min

Si-CCD 16Mpixel (4095x4095) with Zeiss 72mm IR lens, 1.4/85 zoom, no filter

# IR image



55V, 4.3A, 180 s, bg subtr., FLIR SC8343  
 with InSb CCD array, 25mm f/4 HD lens  
 FLIR 23898-000-0033 cold filter 3-5um

April 7, 2013

Statistic [units]	Image	
Mean [C]	1.19	1.87
Sum	N/A	N/A
Std. Dev. [C]	0.94	0.42
Center [C]	(639.5, 359.5) 1.85	(645.0, 333.0) 1.88
Maximum [C]	(93, 126) 3.91	(93, 126) 3.91
Minimum [C]	(958, 697) -0.35	(44, 97) -0.02
Number of Pixels	921600	575225

Slide 27