

Next-Generation Frequency and Voltage Control using Inverter-Based Resources

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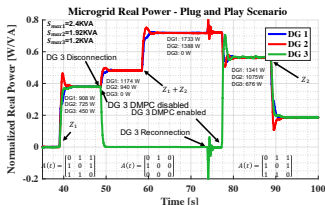
EPRI
ELECTRIC POWER
RESEARCH INSTITUTE

NREL Workshop on Resilient Autonomous Energy Systems

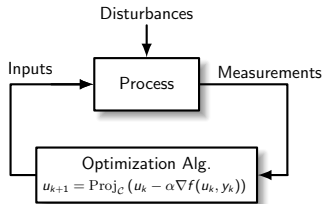
September 7, 2021

JWSP Group Research in Control and Power Systems

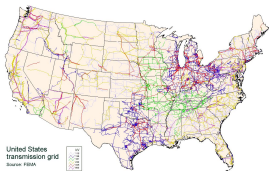
Control + Opt of Microgrids



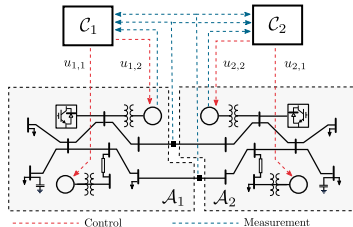
Feedback-Based Optimization



Robust Methods for Power Flow Analysis



Automatic Generation Ctrl.



Motivation

Selected Trends/Challenges in Grid Modernization:

- ① reliability concerns from decreased inertia & new RES, DERs
- ② inadequate legacy monitoring/control architectures (e.g., SCADA)

Required Advances for Next-Grid Control:

- ① use of high-bandwidth **closed-loops** (e.g. 10+ samples/sec)
- ② online coordination of heterogeneous **inverter-based resources** (IBRs)
- ③ **distributed hierarchical controls** for (i) integration of many devices, (ii) local situational awareness, (iii) low-latency localized response

► EPRI Whitepaper: *“Next-Generation Grid Monitoring and Control: Toward a Decentralized Hierarchical Control Paradigm”*

Enabling Fast Control via Inverter-Based Resources

Objectives and design constraints

Big Picture: fully leverage IBR capabilities for freq./volt. control

① Design Objectives

- **Fast** and **localized** compensation of disturbances
- Hierarchical/decentralized architecture (min. delay, **scalability**)
- State/control variable **constraint satisfaction**

② Design Constraints

- Premium on **simplicity** in design and implementation
- Integrable with **legacy controls**
- Uses **realistically available** model info.

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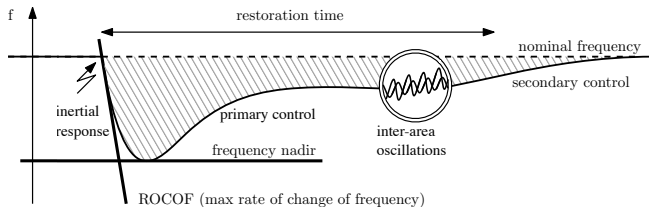
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Outline of Talk

- ① Frequency controller design
- ② Voltage controller design
- ③ Joint frequency/voltage design

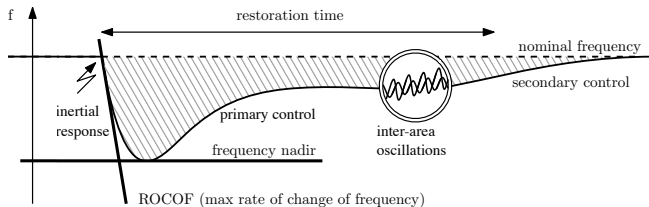
Review: Frequency Control in the Bulk Grid



Fundamentals of frequency control:

- 1 **Inertial** response: fast response of rotating machines
Time scale: immediate
- 2 **Primary** control: turbine-governor control for *stabilization*
Time scale: seconds. Spatial scale: local control, global response
- 3 **Automatic Generation Control (AGC)**: multi-area control which eliminates *generation-load mismatch* within each area
Time scale: minutes. Spatial scale: area control, area response.

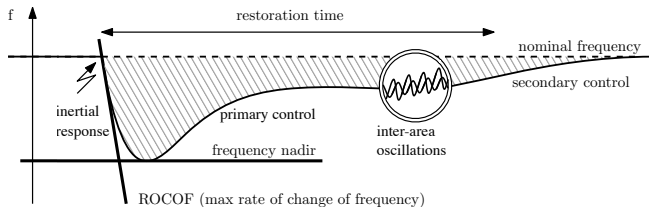
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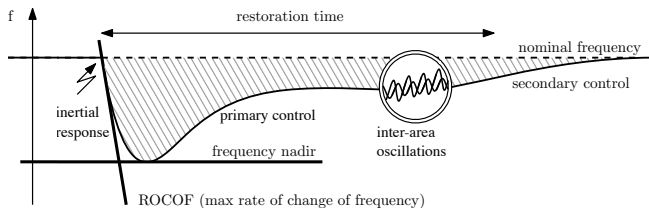
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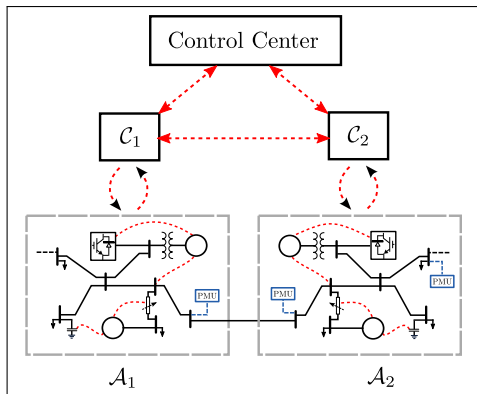
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Overview of Proposed Frequency Controller



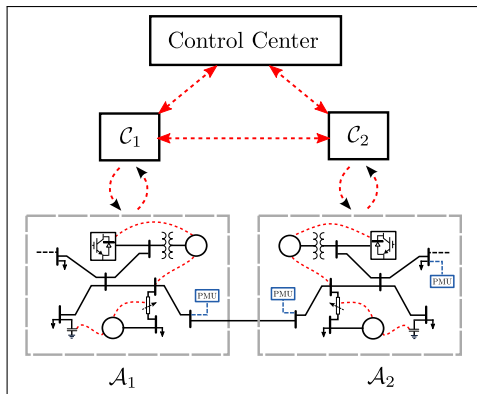
Bulk grid divided into small **local control areas** $\mathcal{A}_1, \dots, \mathcal{A}_N$ (e.g., a few substations each)

Measurements and resources locally available within each LCA

- 1 **Stage 1:** LCA-decentralized controllers C_k redispatch local IBRs
- 2 **Stage 2:** Centralized coordination for severe contingencies

Conceptual goal: very fast and localized secondary-like response

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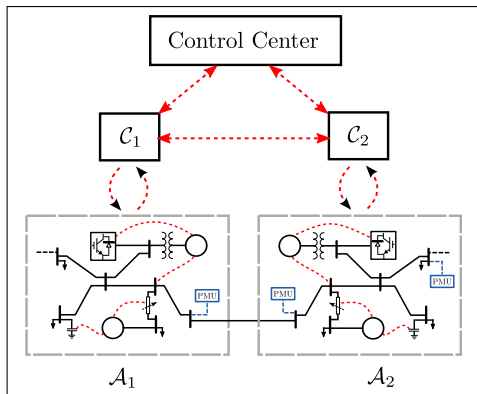
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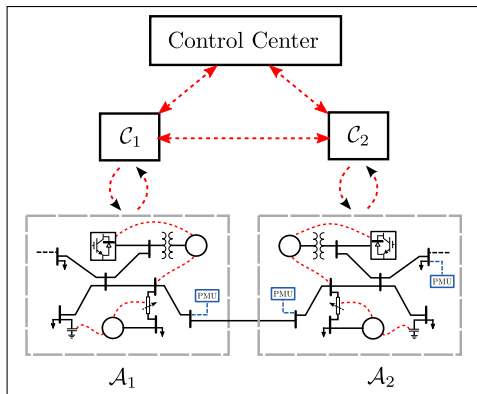
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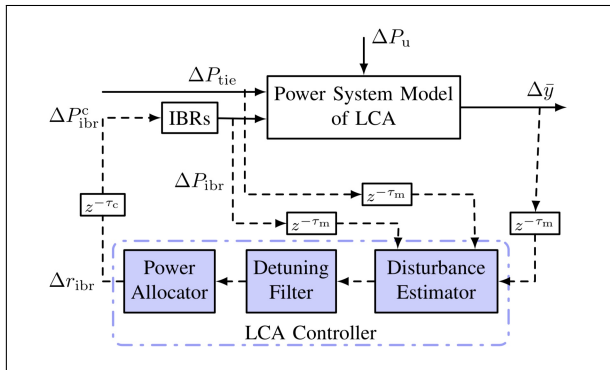
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Philosophy: quickly estimate and compensate all local imbalance

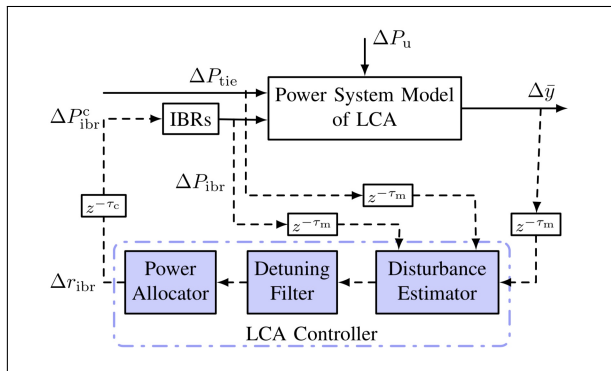


IBRs: can have local f/P droop curve, but must **accept a provided set-point**

- 1 **Disturbance Estimator**: real-time estimate of gen.-load mismatch
- 2 **Detuning (if needed)**: lower bandwidth to ensure robust stability
- 3 **Power Allocator**: compute (constrained) power set-points for IBRs

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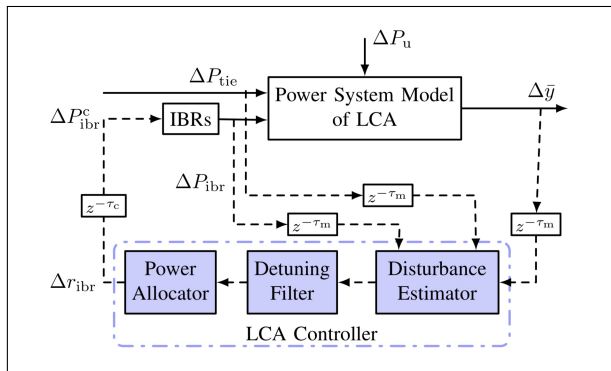


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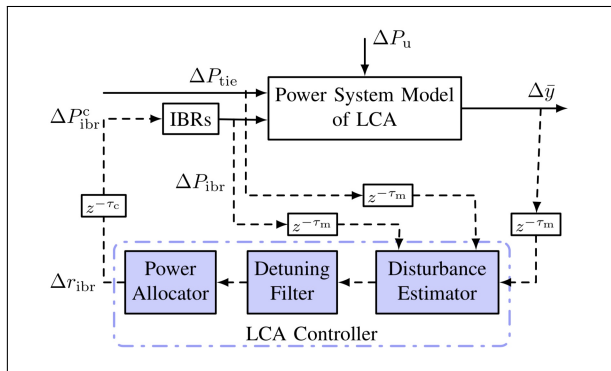


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Stage 1: Design of the Disturbance Estimator

An application of classical internal model control (IMC) ...

- 1 A crude/**aggregate LCA model**, e.g.,

$$\begin{aligned}2H\Delta\dot{\omega} &= -(D + \frac{1}{R_I})\Delta\omega + \Delta P_m - \Delta P_u - \Delta P_{\text{inter}} + \Delta P_{\text{ibr}}^c \\ T_R\Delta\dot{P}_m &= -\Delta P_m - R_g^{-1}(\Delta\omega + T_R F_H \Delta\dot{\omega}),\end{aligned}$$

where $\Delta x = (\Delta\omega, \Delta P_m)$ and $\Delta P_u =$ unknown gen/load mismatch

- 2 **Assume:** $\Delta\omega$ measured, ΔP_{inter} measured (subj. to. delays)
- 3 Discretize LCA model & augment with **disturbance/delay models**

$$\Delta P_u(k+1) = \Delta P_u(k), \quad \Delta\omega_m(k) = \Delta\omega(k - \tau_d), \dots$$

- 4 Design **observer** (e.g., Kalman) to estimate $\Delta\hat{x}(k)$ **and** $\Delta\hat{P}_u(k)$

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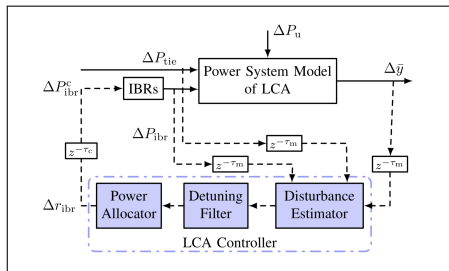
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Stage 1: Detuning and Power Allocator

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Detuning (optional):

low-pass filter

$$F(z) = \frac{1 - e^{-T/\tau}}{z - e^{-T/\tau}}$$

for lowering controller bandwidth

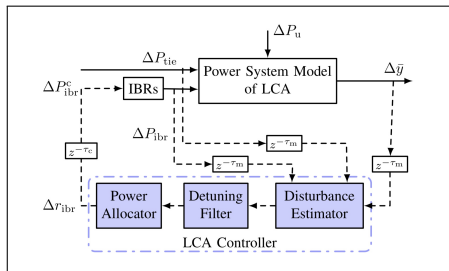
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$$\underset{\varphi_i, P_{ik} \in [\underline{P}_{ik}, \bar{P}_{ik}]}{\text{minimize}} \quad f_i(\{P_{ik}\}) + \lambda_i |\varphi_i|$$

$$\text{subject to} \quad \sum_{k \in I_i} (P_{ik} - P_{ik}^{\text{dispatch}}) + \varphi_i = \Delta \hat{P}_{u,i}$$

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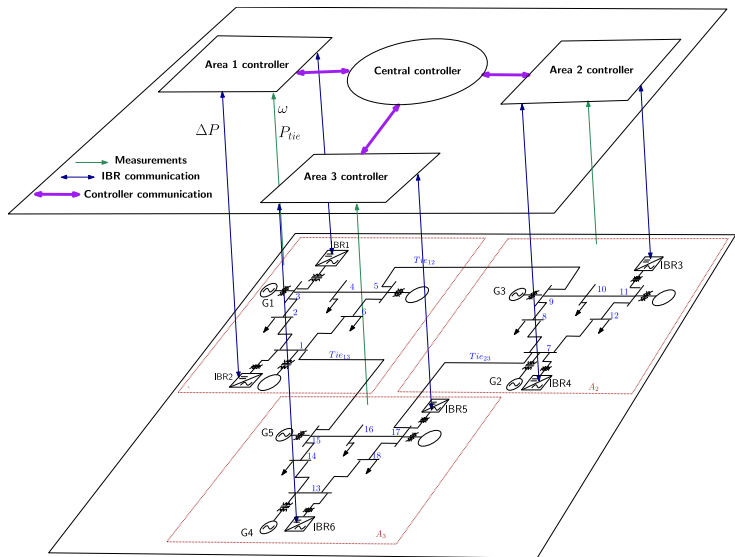
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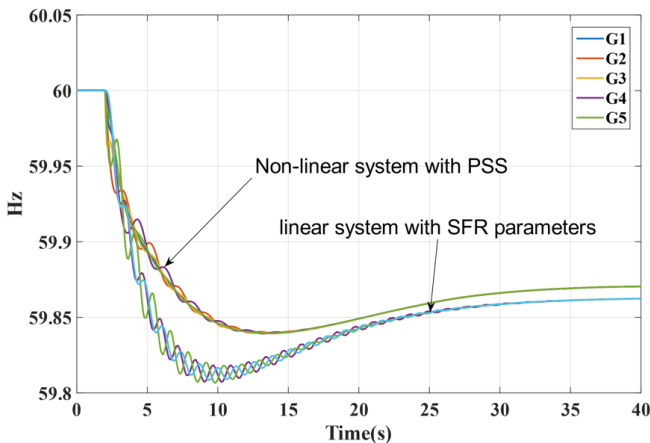
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Case Study: Three-LCA System

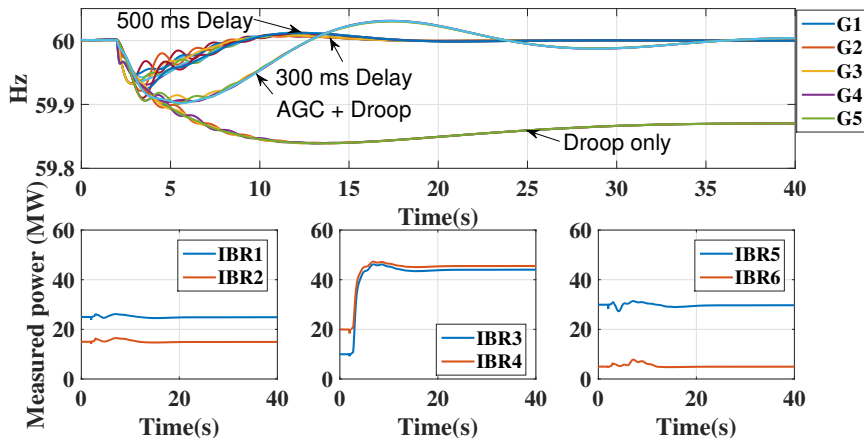


Simplified Model Response vs. True Nonlinear Model

- LCA model parameters set via simple inertia/droop gain aggregation and using largest turbine-gov time constant (**very crude!**)
- 63 MW load increase in Area 2



Scenario: 63 MW Disturbance, Area 2



Localized Response: IBRs in Area 2 ramp quickly; IBRs in Areas 1/3 don't *need* to react, so they don't.

Stage 2: Centralized Coordinator Design

What if local IBR capacity is **insufficient** to meet the disturbance?
Then IBRs in **electrically close** areas should respond.

- mismatch variable φ_i from Stage 1 will be **non-zero**
- total IBR adjustments a_i computed as

$$\begin{aligned} & \underset{\{a_i\}_{i \in \mathcal{A}}}{\text{minimize}} && \sum_{i \in \mathcal{A}} q_i a_i^2 \\ & \text{s.t.} && 0 = \sum_{i \in \mathcal{A}} (a_i - \varphi_i^*) \\ & && 0 \leq a_i \cdot \text{sign}\left(\sum_{i \in \mathcal{A}} \varphi_i^*\right), \quad i \in \mathcal{A} \\ & && a_i + \sum_{j \in \mathcal{I}_i} P_{ij}^* \in [\text{lower}, \text{upper}], \quad i \in \mathcal{A}. \end{aligned}$$

Solution method matters! Centralized vs. privacy-preserving ADMM

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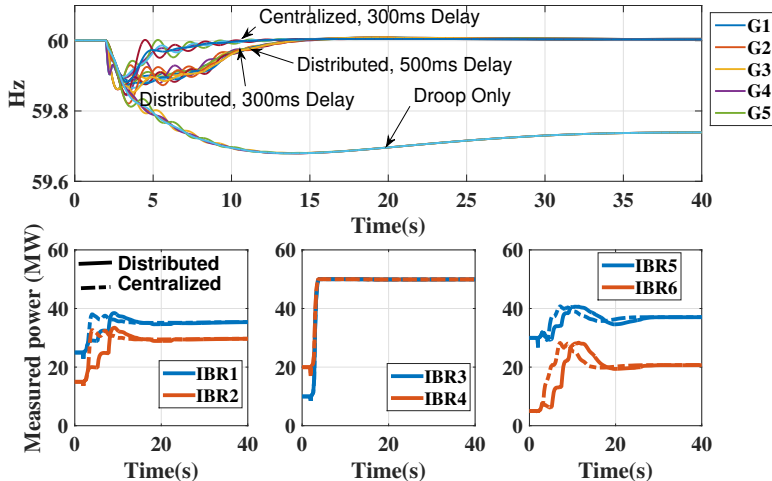
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Scenario: 130MW Disturbance, Area 2



IBRs in Area 2 hit limits; Stage 2 forces Area 1/3 response.

Conclusions for Frequency Control

Summary:

- Two-stage design: local area control & global coordination
- Design enables **fast frequency control** via IBRs
- Response is **localized** to the contingency
- Inherent **robustness** against model imperfections

Ongoing:

- remove even the crude model requirement via **data-driven** control
- extend to incorporate **distribution**-integrated DERs

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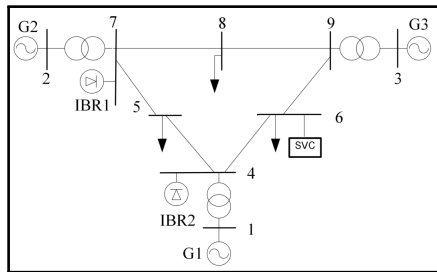
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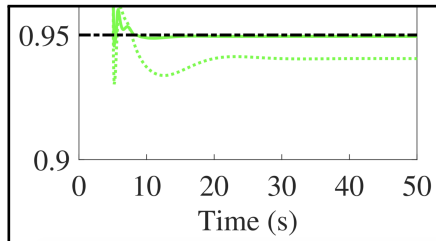
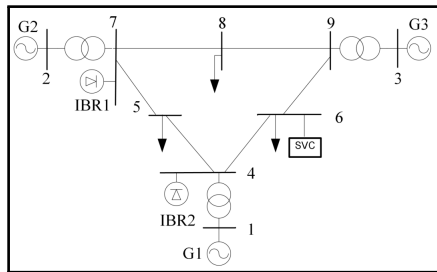
Overview of Proposed Voltage Controller (One-Area)



Control resources:

- SGs: $v_g^{\text{ref}} \rightarrow q_g$
- SVCs: $v_s^{\text{ref}} \rightarrow q_s$
- IBRs: $q_i^{\text{ref}} \rightarrow q_i$

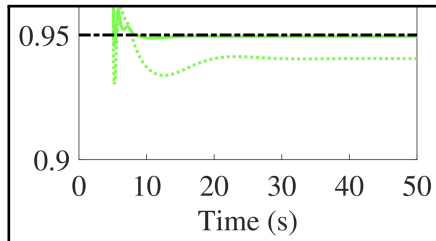
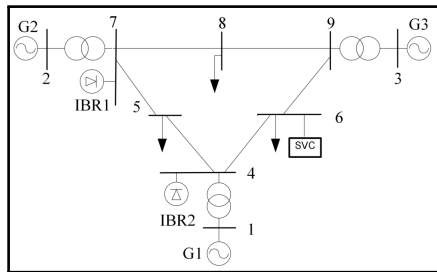
Overview of Proposed Voltage Controller (One-Area)



Control resources:

- SGs: $v_g^{\text{ref}} \rightarrow q_g$
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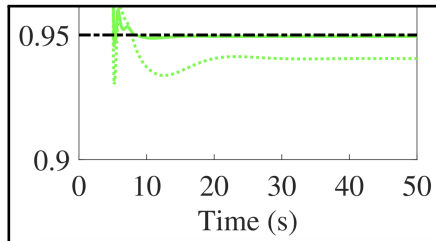
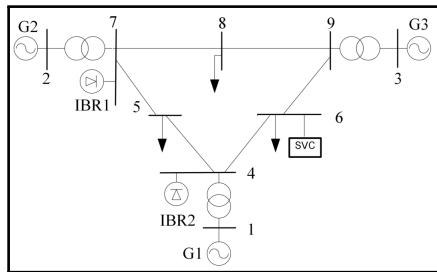
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Model:

$$\dot{x} = f(x, u, w)$$

$$y = (v, q) = h(x, u, w)$$

$$\underset{u \in \{\text{Limits}\}}{\text{minimize}} \quad f(q)$$

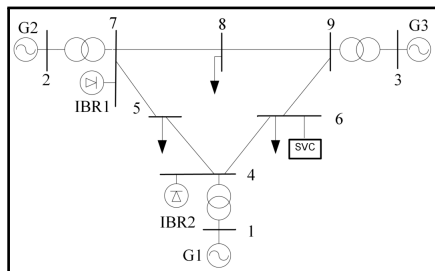
subject to voltage limits
 power limits

Steady-State Optimization Problem (One-Area)

minimize $\text{Priority}(q_g, q_s, q_i) + \text{PenaltyFcn}(q_g, q_s, v) := F(u, y)$
 $v_g^{\text{ref}}, v_s^{\text{ref}}, q_i^{\text{ref}}$

subject to $y = (q_g, q_s, v) = \pi(v_g^{\text{ref}}, v_s^{\text{ref}}, q_i^{\text{ref}}, w) = \pi(u, w)$

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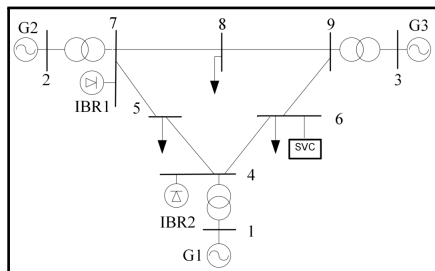


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- vector y assumed to be **measurable** in real-time
- π = steady-state grid model from power flow eqns.
- **approximate sensitivities**
 $\Pi \approx \frac{\partial \pi}{\partial u}$ computable via load flow model

Feedback Implementation of Voltage Controller

- approximate gradient method steps can be evaluated using **real-time system measurements** leading to a **feedback controller**

$$u_{k+1} = \text{Proj}_{\mathcal{U}} \left\{ u_k - \alpha \left(\nabla_u F(u_k, y_k) + \Pi^T \nabla_y F(u_k, y_k) \right) \right\}$$

- nonlinear controller implemented on a nonlinear dynamic transmission system; stability analysis is non-trivial

Theorem: Assume grid is nominally “stable” and “well-behaved”. If

$$u \mapsto \nabla_u F(u, \pi(u, w)) + \Pi^T \nabla_y F(u, \pi(u, w))$$

is a **strongly monotone** operator, then CLS is stable for all sufficiently small controller gains $\alpha > 0$.

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Add-Ons and Extensions for Voltage Controller

The base controller is flexible and admits various modifications

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- 1 **Multi LCA Systems:** use one-area controller in each LCA
- 2 **Faster/Slower Unit Responses:** replace α with diagonal matrix $\alpha = \text{blkdiag}(\alpha_{\text{ibr}}, \alpha_{\text{svc}}, \alpha_{\text{sg}})$ and tune elements as desired
- 3 **Improved Recovery to Pre-Fault Operating Voltages:** integrate term proportional to $\|\Delta v_{\text{sg}}\|_2^2$ into objective function
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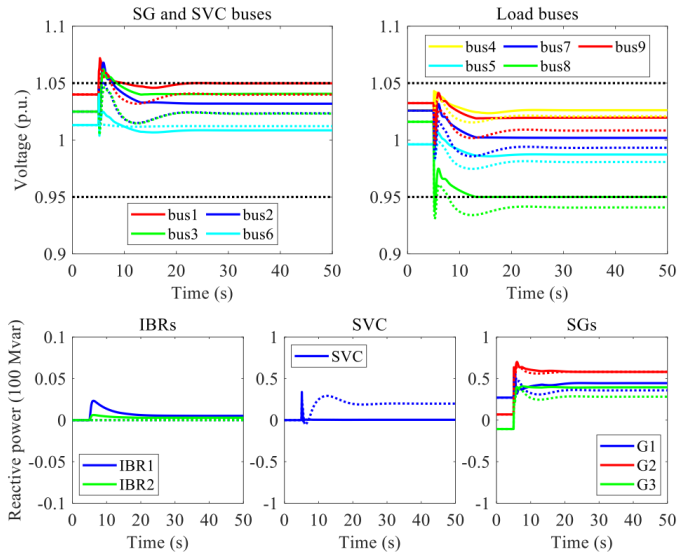
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Scenario: 120 MVAR Disturbance (SG Priority)

solid: with proposed controller

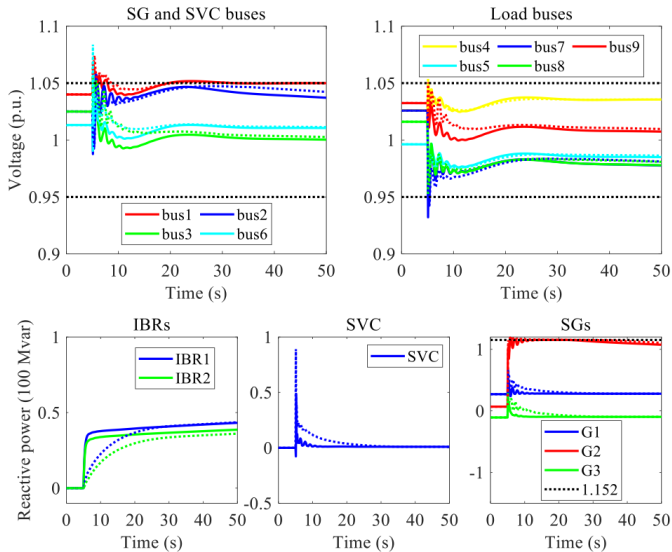
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Scenario: 180 MVAR Disturbance (G2/IBR Priority)

solid: with proposed controller

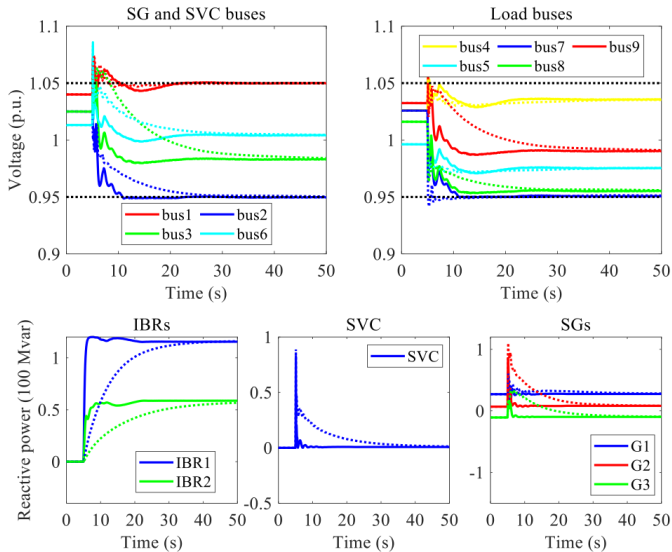
dotted: **ignore**



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solid: with proposed controller

dotted: **ignore**



Conclusions for Voltage Control

Summary:

- Local area control based on local model/meas.
- Flexible design allows operator to set device priority
- Bus voltage and device output constraint satisfaction
- More scenarios: line trips, 3 ϕ -fault, multi-areas, etc. ...

Ongoing:

- combine with online least-squares sensitivity estimation (model-free)
- integration with frequency controller

Paper: <https://www.control.utoronto.ca/~jwsimpson/>

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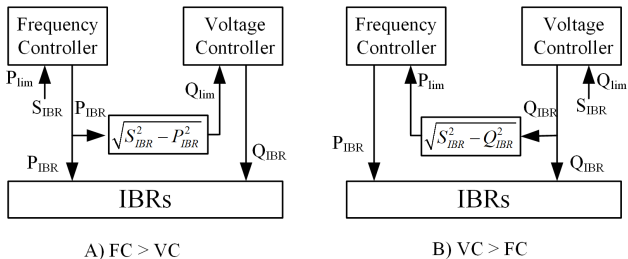
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Integration of Freq. and Volt. Controllers

The two controllers can operate simultaneously.

① Allocate IBR capacity priority



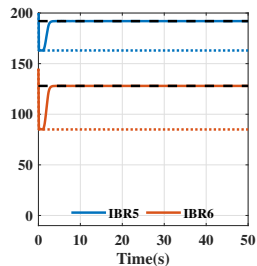
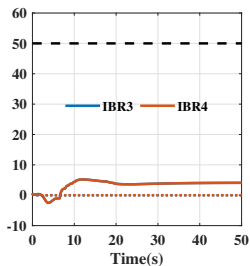
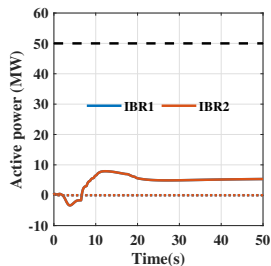
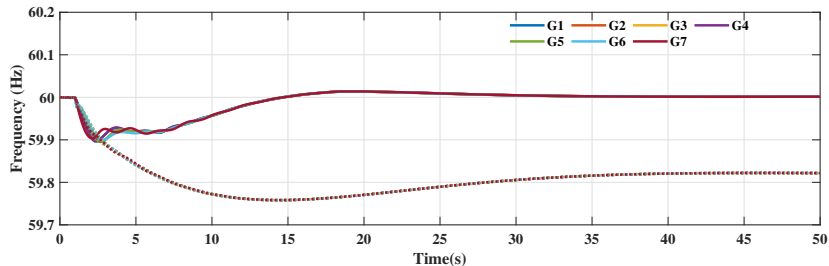
② Dynamic cross-couplings between controllers:

- **voltage-sensitivity** of (e.g., impedance) loads
- **PSS** and VC both operate through SG AVR systems

Scenario: 150MW/80MVAR Disturbance (FC Priority)

solid: with proposed controller

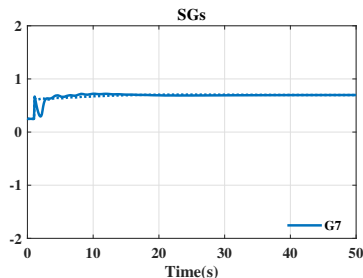
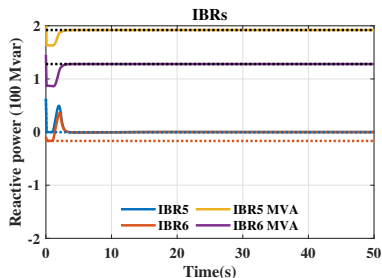
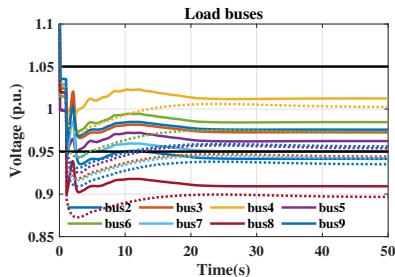
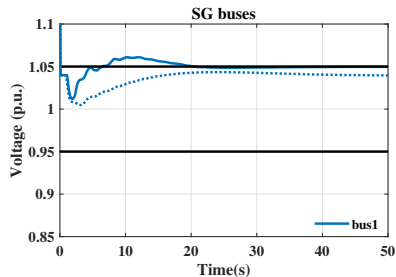
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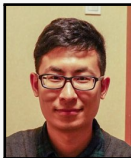
solid: with proposed controller

dotted: without



Collaborators

UWaterloo: Etinosa Ekomwenrenren (PhD), Zhiyuan Tang (PDF), JWSP



EPRI: Evangelos Farantatos, Mahendra Patel, Hossein Hooshyar,
Aboutaleb Haddadi



Questions



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of Electrical & Computer Engineering
UNIVERSITY OF TORONTO



**UNIVERSITY OF
WATERLOO**



**ELECTRIC POWER
RESEARCH INSTITUTE**

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Comparison with Traditional Frequency Control

Traditional frequency control:

- ① **very fast** inertial response of machines limits ROCOF
- ② primary layer (droop) provides **“fast”** & **global** stabilizing response
- ③ secondary layer (AGC) provides **slow** & **“localized”** response

Traditional frequency control + next-gen IBR controller:

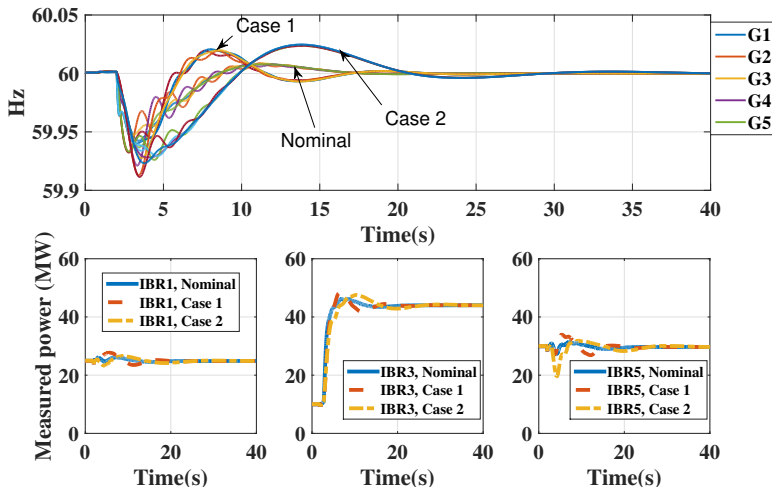
- ① **very fast** inertial response of machines limits ROCOF
- ② Stage 1 (local IBR redispatch) provides **fast & localized** response

Ideally, **minimal activation** of SG turbine-govs

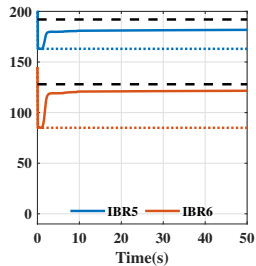
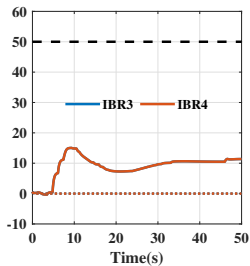
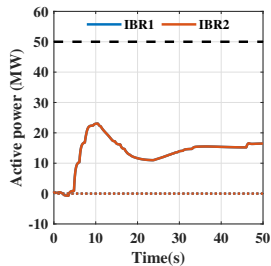
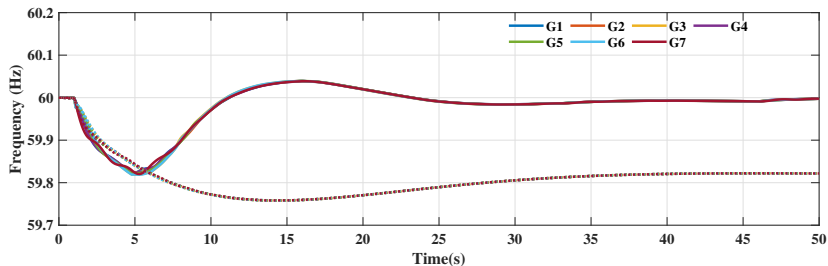
- ③ Stage 2 (global IBR redispatch) provides **fast & semi-local** response
- ④ AGC cleans up any remaining mismatch on minutes time-scale

Frequency Scenario: Robustness Test

- Introduce large (50%–100%) errors in parameters (H , T , R , ...) used for LCA disturbance estimator designs



Scenario: 150MW/80MVAR Disturbance (VC Priority)



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