Computer Simulation of Shading and Blocking: Discussion of Accuracy and Recommendations

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Abstract A field of heliostats suffers losses due to shading and blocking. Shading occurs when a heliostat is shaded from the sun by a neighboring heliostat and similarly, blocking occurs if some of the reflected sunlight hits the back of a neighbor instead of proceeding towards the receiver. The usefully reflecting region is represented by a set of vertices in the plane of the heliostat. This set of points is called the boundary vector. The boundary vector is used to compute the percentage of loss for a heliostat due to its neighbors and also to compute the image of the heliostat on the receiver. The image is needed to determine the receiver interception fraction and the corresponding percentage of loss due to the receiver size.

The complex geometry of multiple shading and blocking events due to several neighbors suggests that a processing type of code is needed to update the boundary vector for each shading or blocking event. A new version called RSABS simulates the split rectangular heliostat (see figure 1). After a discussion of the errors resulting from our simplifying assumptions, we conclude that the dominant error for the given heliostat geometry is due to the departure from planarity of the neighboring heliostats. Systematic errors of several percent can occur in this way. A programmer's manual for RSABS is included.

We recommend that a version of the heliostat simulation be modified to include losses due to non-reflective structural margins, if they occur. See
Figure 6. We also recommend that the heliostat neighbors be given true guidance rather than assumed to be parallel, and that the resulting non-identical quadrilateral images be processed as in HELIOS by ignoring overlapping events which we find to be extremely rare in optimized fields.
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1) INTRODUCTION

The loss fraction, $F_l$, attributed to the shading and blocking of a heliostat is complementary to the fractions of effectiveness for the heliostat, $F_e$. Clearly, we have

$$F_l + F_e = 1$$

The fraction of effectiveness can be defined in several ways using parallel or stereographic projections of the neighboring heliostats.

It is reasonable to define the fraction of effectiveness for a heliostat, relative to a particular point $P$ on the surface of the receiver, as the ratio of the flux density due to the given heliostat with and without its neighbors. Consequently,

$$F_e(P) = \frac{\int dwS(\alpha) / \int dwS(\alpha)}{A_e(P) / A_H}$$

where $dwS(\alpha)$ is the flux density due to direct beam insolation received from a cone of solid angle $dw$ oriented in a direction $\alpha$ radians from the center of the solar disc. $A_H$ is the reflecting region of the heliostat and $A_e(P)$ is the effective reflecting region after losses due to shading and blocking by the entire set of neighboring heliostats. $A_e(P)$ depends on the point $P$ because the effective region is limited by a stereographic projection of the neighboring heliostats using $P$ as a center. This definition of $F_e$ is inconvenient because it depends on difficult flux density calculations. However, the approximation

$$F_e(P) \approx \frac{A_e(P)}{A_H}$$

holds under the assumptions:

1) The solar disc is uniform, i.e. $S(\alpha)$ is independent of $\alpha$;
2) The heliostats are relatively small so that the apparent solar disc can fill the heliostat; and
3) The heliostats are well guided and $P$ is relatively near the center of the receiver.

It is usually desirable to define the effective fraction of the heliostat in a receiver independent way. Assuming a point sun, we can write

$$F_e = \frac{A_e}{A_H}$$

where $A_H$ is the area of reflecting surface per heliostat and $A_e$ is the usefully reflecting area of the central heliostat in the neighborhood. $A_e$ is determined by a parallel projection of all relevant neighbors. This definition of $F_e$ is used throughout subsequent discussions. It lacks some precision due to the finite size of the solar disc. However, the effect of the solar disc is very slight and can be estimated by redefining $F_e$ in terms of the total usefully reflected power. Let

$$F_e = \frac{\int_{-\infty}^{\infty} \int \sigma \, d\sigma \, d\omega \, S(\alpha) / J A_H}{A_e}$$

where $d\sigma$ is an element of area in a plane perpendicular to the optic axis. $A_e$ is based on the parallel projections, and $J$ is the total direct beam insolation in W/m².

$$J = \int d\omega \, S(\alpha)$$

An inspection of the $d\sigma$ integral reveals regions of zero intensity and regions of maximum intensity equal to $J$, as well as regions of intermediate intensity corresponding to the familiar umbra and penumbra. The contour of 50% intensity corresponds to the boundary of $A_e$. The symmetry of the umbra and the penumbra for long straight edges leads to the result that $F_e \equiv A_e / A_H$. However, the vertices of the useful region $A_e$ are exceptional points which introduce small errors.
Unlike procedures which simply sum the area shaded or blocked in each event, without regard for overlapping which may occur, our shading and blocking processor updates the boundary vector of the useful reflecting region each time a shading or a blocking event occurs. There is an initial boundary vector $B_0$ and a final boundary vector $B_1$ which determines $A_e$ and $F_e$. In general a boundary vector has the form

$$B = \{(u_i, v_i) \mid i = 1 \ldots N\},$$

where $(u_i, v_i)$ represents a point in the plane of the heliostat. The closed region defined by the $N$ vertices of $B$ has the area

$$A = \frac{1}{2} \sum_{i=3}^{N} [(u_{i-1} - u_1)(v_i - v_1) - (u_i - u_1)(v_{i-1} - v_1)]$$

The initial boundary vector $B_0$ gives the area $A_H$ if the $u, v$ coordinates have true scale. However, it is convenient to renormalize the scale of the $u, v$ coordinates so that

$$B_0 \rightarrow A_0 = 1 \text{ and } F_e = A_e.$$  

2) **PRELIMINARY CONSIDERATIONS**

The first shading and blocking processor was developed at the UH Energy Lab in the summer of 1973 for rectangular heliostats in linear neighborhoods with stereographic projections. To our knowledge, this is still the only shading and blocking processor capable of properly handling overlapping images in a general way. The present effort provides an efficient model of the split rectangular heliostat. (See Figure 1). This code is called RSABS.

Early, heliostat design concepts involved square, hexagonal, and circular heliostats. Consequently we proceeded to develop a processor called NGON, which represents regular polygons. This code was used from 1975 to 1979,
The regions $B$ and $C$ each have a boundary vector with 4 points initially. There are three input variables; namely, UMIR, VMIR, and SLOT as shown. An additional glass sequent in the slot converts the heliostat into an H or U shaped heliostat.
even though most heliostat designs had clipped corners and median slots which are ignored by NGON. In 1979 we developed RSABS to include the slot. We do not have a processor for circular heliostats, although we have developed a code (called BL) that represents a bubble enclosed circular heliostat with isolated shading and blocking events. The isolated shading and blocking events include interference by neighboring bubbles as well as by the enclosed heliostat disks. Bubble transmission as a function of angle of incidence for both the enclosing and neighboring bubbles is included. If no bubbles are present circular heliostats could be handled by setting the transmittance function equal to 1.0, but a new code version would be preferable.

The central receiver system concept assumes that the heliostats are mass produced and are structurally similar. Consequently, each heliostat and its neighbors are expected to have the same size and shape. The similarity of the heliostat profiles vastly simplifies the shading and blocking processor. Another simplification, which we use depends on the plane of the collector field. We usually assume that the heliostat centers are coplanar, so that the collector field will have a well defined plane, although it may not be a level plane. Given adverse terrain the collector field may become contoured but we will continue to assume that the neighborhoods are approximately planar. Notice that both the sun and the receiver are expected to be above the plane of the collector field (i.e. planes of the neighborhoods), so that the highest point of a heliostat can not be obscured by a shading or a blocking event. Consequently, the high point of the heliostat is chosen as a fixed point of the processor and is labelled the first vertex.

The boundary vector concept introduced in section (1) assumes that the heliostats have a polygonal profile. It is possible to develop a processor for
arbitrary polygons. For example, if \( X, Y, \) and \( Z \) are polygons having boundary vectors \( \bar{X}, \bar{Y}, \) and \( \bar{Z}, \) then the processor must determine \( \bar{Z} \) so that
\[
Z = X \cup Y, \quad (\cup \text{ denotes the logical intersection}).
\]
In this example, if \( X \) represents the reflective area of a central heliostat and \( Y \) the boundary of a nearly neighbor, then \( Z \) represents their overlap and the polygon \( X - Z \) is the new reflective area, which may be subject to additional events. However, this approach will not necessarily lead to efficient calculations and, therefore, it is desirable to develop processors for a series of progressively more complex cases. For instance, we may consider

1) Rectangles (See Figure 2 for typical events),
2) Split Rectangles (See Figure 1 for basic geometry),
3) Various shapes depending on the shape of the slot, and finally
4) Regular polygons such as octagons.

The first two cases will be developed in this report. The third case is an easy extension of the split rectangle geometry to include a third rectangular piece of glass in the slot. The case of regular polygons is essentially more complex but not as bad as arbitrary polygons.

Before going into the design of the code, it desirable to consider the variety of its applications. For generality, all heliostat geometry is referred to an orthonormal basis \((\hat{u}, \hat{v}, \hat{w})\) which is fixed in the frame of the heliostat. The unit vector \( \hat{w} \) is normal to the plane of the heliostat, hence \( \hat{w} \) depends on the positions of the sun and the receiver. However, \( u \) and \( v \) also depend on the choice of the heliostat mounting system which plays a role in determining the high point of the heliostat.

Figure 3 shows a rectangular heliostat with two events. The cross hatched region remains useful after the events. If event (I) comes first in the processor, then event (II) pinches the useful region into two discon-
Figure 2) Some Typical Shading and Blocking Events.

The closed curve represents the boundary status before processing the event which is represented by the open curve. The dots represent vertices which must be deleted to process the current event. Crossed lines become new vertices. The current image caused NEW points, and INN points must be deleted.
Figure 3) Rectangular Heliostat in (u,v) Plane.

Two events are shown to cause a split region. Points (1,2,3,4) are the vertices of the central heliostat under analysis. The cross hatched area is usefully reflecting. $O_1$ and $O_{II}$ are the images of the center of heliostats I and II under either a shading or a blocking projection. Event II could not cross side 1 \rightarrow 2 with altazimuthal mountings.
connected areas resulting in a boundary having two cycles. This situation cannot be handled by a single boundary vector and will be ignored for the present. This type of overlap problem can not occur for alt-azimuthal mountings since the ū axis is parallel to the ground and therefore the whole upper edge is immune to events. For other mountings the pinch-off problem can occur in realistic collector fields for low solar elevations but very little error occurs if the lower area is deleted. We can afford to ignore it, since all current designs call for alt-azimuthal mountings.

The shading and blocking events depend on the location of the neighbors with respect to the central heliostat. In cell wise models of the collector field, the displacements of the neighboring heliostats are generated independently for each representative heliostat. The neighborhood geometry depends on the incline of the collector field, the type of neighborhood (i.e. radial stagger, N-S stagger, radial cornfield, N-S cornfield, etc.) and the number of neighbors. In an individual heliostat model of the collector field each heliostat has a position vector which locates it with respect to the base of the tower, so that the incline of the field and the type of neighborhood are no longer choices available within the shading and blocking program. However, the size of the neighborhood (i.e., the number of neighboring heliostats) remains a choice under suitable input controls.

The shading and blocking subroutine RSABS and its helper EVENT are designed to handle split rectangular heliostats in the framework of the cell-wise performance code system. See figure 3. Conversion to other code environments is easy. Appendix B contains a list of RSABS and EVENT.

We should also consider the variety of outputs which may be required from a shading and blocking program. The boundary vector is always available if needed by the heliostat image generator. The boundary vector leads
quickly to the area of the useful region and the fraction of glass which is usefully reflecting. The useful fraction is frequently the only required output. However, if the heliostat has a sun sensor for guidance purposes, it may be necessary to have a special test in order to determine whether the sensor is exposed to the (reflected) sun at any given time. Current heliostat designs call for computer guidance, so this feature has been omitted. It may be desirable to know the fraction of shading and the fraction of blocking separately, although this feature is not built into the code at this time. We have an additional output array, giving the serial number of the neighbors which are responsible for the first and second shading and blocking events. This output is occasionally useful for interpreting results.

3) TASK STRUCTURE OF CODE

The following list indicates the purpose of each functional element required for a rectangular heliostat shading and blocking subroutine.

1) An initial phase to construct a standard initial boundary vector in dimensionless units. Auxiliary constants are set.

2) The high point of the heliostat is located and its index in the standard boundary vector is determined.

3) The initial boundary vector is loaded, so that its first point is the high point. The initial number of vertices is set.

4) A neighbor heliostat is selected and its displacement from the central heliostat is computed.

5) The displacement is tested to determine whether the neighbor lies on the reflecting or the shading side of the central heliostat.

6) The neighboring heliostat is given a shading and a blocking projection into the plane of the central heliostat. The \((u,v)\) coordinates of the central image points are computed.
7) The remote images are bypassed. (Remote means \( u_O^2 + v_O^2 \) is large, see Figure 3 for example of a non-remote event).

8) Each vertex in the current boundary vector is tested to see if it lies inside of an image heliostat (i.e. inside of a shaded or blocked region). Basic process control variables are set here. See Figure 2.

9) If no event occurred, the program proceeds to the next image.

10) Dependent control variables are set and the tail-end of the boundary vector is shifted by the number of vertices which are required to accommodate the event. New points will occur and old points will be lost. A net gain or loss is possible.

11) The new points are computed and loaded into the appropriate components of the boundary vector. The current number of vertices is reset.

12) After all images are processed, the area of the region defined by the boundary vector is computed.

13) Subroutine returns with the shading and blocking fraction for a single heliostat at a single time.

The over-all structure of the code is shown in Figure 4.

A slotted-rectangular heliostat requires two boundary vectors \( \tilde{B} \) and \( \tilde{C} \), and the useful area is the sum of useful areas due to \( \tilde{B} \) and \( \tilde{C} \). See figure 1. In the list above, items (4-11) are inside of the loop over neighbors and their images. If the heliostat is slotted (i.e. split) each neighbor has two rectangular images which can interact with the two rectangular regions in the central heliostat. Each of the four combinations can occur. Hence, it is convenient to build items (8-11) into a subroutine called EVENT which can be called four times for the slotted heliostat case. An H or U-shaped heliostat
A similar situation exists in the individual heliostat performance model but in the cellwise optimization program, YEAR is replaced by RCELL which calls SBDATA which then calls RSABS.

Figure 4) Nest of Calls for RSABS.
can be handled in a similar way, with nine calls to EVENT and three boundary vectors. The test for remote images works so efficiently that the additional complexity of the code is barely noticeable in CPU time. See conclusions. As the drive and pedestal occupy the lower half of the slot they will rarely cast a shadow on a neighbor or block a reflected beam, thus their presence can be ignored.

4) TEST PHILOSOPHY FOR EVENTS

A neighboring heliostat may or may not cause an event. The call to EVENT is bypassed if the projected image of the neighbor lies outside of the initial boundary vector which represents the maximum extent of the reflecting region in question. This bypass excludes the so called remote images which are easy to detect.

A subroutine listing of RSABS and, starting at line 244, of EVENT is given in appendix B and fortran variables are defined in appendix A. Just inside EVENT the loop 150 goes over the current list of boundary points (K=1, NGON) and tests to see if any points are inside of the image of the neighbor. The first point found to be inside the image sets

\[ IGON = K \quad (I-GO-IN), \]

and the last inside point sets

\[ IGOT = K \quad (I-GO-OUT). \]

If no point is inside, then IGON=0 and RETURN occurs. The K=1 point (selected as the highest point of the heliostat) is not tested because it is a fixed point and in RSABS we assume an alt-azimuthal mounting so that K=2 is also fixed.

All other control variables depend on IGON and IGOT. The list of boundary points splits into several parts. See Table 1. In general, the
Table 1) Shows Correspondence between Current and Updated Points

<table>
<thead>
<tr>
<th>CURRENT POINTS</th>
<th>UPDATED POINTS</th>
</tr>
</thead>
<tbody>
<tr>
<td>BU(1)</td>
<td>BU(1)</td>
</tr>
<tr>
<td>BU(2)</td>
<td>BU(2)</td>
</tr>
</tbody>
</table>

• BU(1) 1 1 • BU(LAST)
• BU(2) 2 2 Unchanged
• LAST LAST • BU(LAST)
• IGON IGON • SU(1)
• Deleted Deleted • SU(2) Update
• IFRT IFRT • BU(IFRT)
• ICORN ICORN • BU(ICORN) Shifted

initial group of boundary points is unchanged. The middle group is replaced by the newly computed points and the final group is unchanged but must be shifted to join the last new point. The initial group must occur. However, no final group occurs if the last current point is inner, so that the new points are final. The following variables refer to the current boundary vector, which does not include the inserted points.

LAST=IGON-1 (last of first group)
IGON (first of deleted group)
IGOT (last of deleted group)
IFRT=IGOT+1 (first of final group)
ICORN (last of final group)

The following variables are required to construct the updated boundary vector.

INN=IGOT-IGON+1 (number of inner points)
NEW =2 if INN is even
     3 if INN is odd
JCORN=NEW-INN (change in ICORN)
KFRT=IFRT+JCORN (first of final group)
KORN=ICORN+JCORN (last updated point)
    +ICORN

The odd-even rule for NEW is valid for rectangular images. For other shapes, a more complicated test is needed to determine NEW. It is important to shift the final group before loading the new points. However, no shift occurs if

JCORN=0, or IGOT=ICORN.
The new points are either corners of the neighboring heliostat image or combinations of components from the neighboring heliostat image and the current boundary vector. In order to select the right combination we have to know whether the first new point belongs to constant U or a constant V segment of the current boundary vector. Let

\[ JINDEX = INDEX + LAST, \]

so that JINDEX is even if the LAST leads a constant U segment and JINDEX is odd if LAST leads a constant V segment. One further test is needed to decide between the larger and smaller alternatives for a component, so that the new point will go inside of the glass region. This is a relatively fussy construction and if there is any doubt about how it is working one can set

\[ IPSAB = 2 \]

in order to output the boundary vector for closer study.

5) INPUT REQUIREMENTS AND GEOMETRY OF SPLIT-RECTANGULAR HELIOSTAT

Figure 1 shows the geometry of the split (or slotted) rectangular heliostat. There are three basic linear dimensions: UMIR, VMIR, and SLOT as shown in the figure. According to this model, the reflecting area of the heliostat, is given by

\[ AHELI = VMIR \times (UMIR - SLOT), \]

however, various minor features such as clipped corners and gaps between the segments may cause AHELI to differ from the actual reflecting area, which is always called HGLASS.

Shading and blocking also depends on the geometry of the heliostat neighborhood. For a radial stagger neighborhood, the radial and azimuthal spacing parameters are given by

\[ R = XGRND \times DMIR \]
\[ Z = YGRND \times DMIR \]
where \( XGRND \) and \( YGRND \) are determined by the optimization program and are independent of \( DMIR \) which represents heliostat size. We define

\[
DMIR = \left[ \frac{1}{2} (UMIR^2 + VMIR^2) \right]^{\frac{1}{2}}
\]

so that for a square heliostat

\[ DMIR = UMIR = VMIR. \]

\( DMIR \) is a convenient scale, it is not simply related to the diagonal. The fraction of ground coverage is given by

\[
FGRND = \frac{.5 \times RHELI}{XGRND \times YGRND}
\]

where

\[ RHELI = \frac{HGLASS}{DMIR^2}. \]

Notice that \( DMIR \) cancels out of \( FGRND \), and \( HGLASS \) introduces the true heliostat area. These identities remain true for the split rectangular heliostat, however, the value of the mechanical limit (in \( DMIR \) units) may have to be adjusted for a new geometry.

The fraction of shading and blocking is called \( FMIRX \). A look at the listings in appendices A and B reveals that \( FMIRX \) is transmitted to the external program by common group GRP6. In previous shading and blocking codes, the components of the boundary vectors were in meters, so that

\[
FMIRX = \frac{.5 \times POLYA}{AHELI},
\]

where \( POLYA \) is twice the area of the region enclosed by the boundary vector. In this case \( POLYA \) and \( AHELI \) have the dimensions meters squared. However, in RSABS the components of the boundary vectors are in dimensionless units of \( DMIR \). Consequently, we have

\[
FMIRX = FINVER \times (POLYA_1 + POLYA_2)
\]

where

\[
FINVER = 0.250 \times DMIR^2 / AHELI
\]

and the two boundary vectors give a total useful area of \( POLYA_1 + POLYA_2 \).

(There are two factors of .5: one factor from the area of triangles which is
omitted from POLYA; the other factor is a normalization for the two boundary vectors of the slotted heliostat).

6) **THE DOMINANT ERROR**

The assumptions which have been discussed up to this point lead to very small errors in the shading and blocking calculations. However, several problems relating to heliostat guidance must be considered. The effect of ignoring heliostat guidance errors is very small, but the effect of assuming parallel neighbors leads to errors of several percent in the fraction of useful area, FMIRX.

Guidance errors are typically about 3 milliradians. The resulting errors in FMIRX are small and will average to zero in a reasonable time period. Furthermore, the errors in FMIRX are not strongly correlated with receiver flux spillage so that the assumption of perfect guidance appears to be justified for FMIRX.

The projection of a neighboring heliostat onto the plane of the central heliostat depends on the plane of the neighbor, as well as the plane of the central heliostat. For simplicity we assume that the plane of the neighbors is parallel to the central heliostat. Consequently, the shape of the images is similar to the shape of the central heliostat and the test for events is greatly simplified. Actually, the planes are not parallel due to the independent tracking of the heliostats and the independence of their guidance errors. Assuming perfect tracking, the angle between the planes of adjacent heliostats is roughly equal to the azimuthal spacing parameter divided by the slant range to the receiver. For the Barstow pilot plant, this angle ranges from .035 radians to .148 radians. The worst case error in FMIRX is given by

$$\delta\text{FMIRX} \approx \pm \frac{1}{2} \varepsilon \tan i$$

where $i$ is the angle of incidence on the heliostat and $\varepsilon$ is the angle between adjacent heliostat planes. If $\varepsilon = .148$ and $\tan i = 1.0$, then
\[ \delta \text{FMIRX} \approx 7\%, \]
but this will be a rare case. Unfortunately we do not expect these errors to cancel out in a sum over heliostats since all neighbors tilt toward the central heliostat (simulating a parabola). Hence, a correct calculation is desirable. A glance at figure 5, shows that a correct calculation turns the images into parallelograms, so that a more sophisticated approach to the code would be required.

The exact projections are available in the HELIOS program from SANDIA/Albuquerque (Ref. 3). However, in that code the overlap of quadrilaterals is handled for single events, instead of providing a multi-event processor as is done here. HELIOS is very accurate, but CPU time requirements become troublesome for large numbers of heliostats.

7) SUMMARY AND COMPARISON

The RSABS shading and blocking code derives from the following assumptions

1) The effective fraction is defined by a parallel projection from the center of the solar disc. Umbra and penumbra effects are ignored. The effective fraction refers to total redirected sunlight.

2) The heliostat geometry is split-rectangular. There are two boundary vectors. This technique can be reduced to the simple rectangular case or extended to the U and the H shapes.

3) Any mounting system is allowed but alt-azimuthal is less troublesome because it cannot produce split regions. For other mounting system splits can occur, and the lower region will be thrown away. This occurs very rarely.

4) The effect of guidance errors is negligible, and therefore is ignored in the calculation of FMIRX.
Figure 5) Image of a Non-Parallel Neighbor.

Dashed line shows intersection of heliostat plane with plane of neighbor. Dotted region is parallelogram. For a rectangular heliostats $d_1 = d_2$ but the image becomes a parallelogram.

$$
\delta_1 = \varepsilon d_1 \cos \phi_1 \tan i
$$

where $\varepsilon$ is angle between the plane of the neighbor and the plane of the central heliostat and $i$ is angle of incidence for the heliostat.
5) The effect of independent tracking, with the consequence of non-coplanar neighbors, is ignored. This approximation gives the dominant error. This error would be insignificant for a commercial size system, but in the smaller Barstow plant it may cause significant errors in the performance of selected heliostats having large incidence angles.

6) Near the singular point in the collector field, the azimuthal orientation of neighboring heliostats varies greatly as the heliostats slew in azimuth to track the sun. However, in this region the heliostats are horizontal, so no shading or blocking occurs. In all other parts of the collector field, the edges of neighboring heliostats are nearly parallel so our current processor is nearly correct.

7) RSABS is a faster subroutine than its predecessors, NGON, etc., in spite of the complexity introduced by the slot.

8) The effect of the slot variable is shown in Table 3. Slotting is not favored from a shading and blocking viewpoint since the deleted part of the heliostat is usually effective. However it may be necessary if there is a valid requirement for mirror inversion (safety or dust aversion).

<table>
<thead>
<tr>
<th>Hours Past Solar Noon</th>
<th>Solar Elev. (deg.)</th>
<th>AV. FMRX SLOT Width 0.0 m. 1.0 m.</th>
<th>MAX.DEV. of FMRX</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>56.3</td>
<td>.988 .986</td>
<td>-.004</td>
</tr>
<tr>
<td>.874</td>
<td>54.2</td>
<td>.990 .988</td>
<td>-.004</td>
</tr>
<tr>
<td>1.749</td>
<td>48.4</td>
<td>.993 .992</td>
<td>-.004</td>
</tr>
<tr>
<td>2.632</td>
<td>40.3</td>
<td>.996 .996</td>
<td></td>
</tr>
<tr>
<td>3.498</td>
<td>30.8</td>
<td>.989 .988</td>
<td>-.006</td>
</tr>
<tr>
<td>4.372</td>
<td>20.6</td>
<td>.945 .948</td>
<td>+.057</td>
</tr>
<tr>
<td>5.246</td>
<td>10.0</td>
<td>.817 .852</td>
<td>+.112</td>
</tr>
</tbody>
</table>

TABLE 3
Effect of Slot Size Using RSABS
(Equinox Afternoon)

20
Figure 6) Realistic Heliostat Geometry

There are 12 panels, four clipped corners and 10 gaps between panels in addition to the central slot. A nonreflecting margin is indicated in black. The margin contributes to shading and blocking loses and must be included in the heliostat profile. It is reasonable to consider the margin and the gaps as a default $\text{FMIRX} < 1$ for no shading and blocking. However, this is not now in the code.
This data describes a heliostat which is 10 meters square. The surround field has a radius of 120 heliostat widths, the receiver is 12 heliostat width high and located 1/3 diameter from the south boundary.
*At 10° degrees of elevation, more neighbors are required to calculate FMIRX correctly. The second value is obtained using 24 neighbors instead of 8, as previously. Significant overlap of shading events has been processed at these low sun elevations. The additional neighbors have no effect at the higher elevations in this table.

8) **RECOMMENDATIONS**

A recent study of shading and blocking using the multievent processor (Ref. 4) shows that practically no over-lapping of events occurs for optimized fields. Hence, the need of an event processor is less than originally expected. Hence, it is practical to consider the exact guidance of the neighbors and process the quadrilateral events as in HELIOS. This would not apply to low sun situations where significant overlap of shading events occurs. For low sun, an accurate treatment requires the more difficult boolean processor with topological complexities but, fortunately, these cases do not contribute significantly to the optimization problem.

Figure 6 shows one of the realistic heliostat geometries. A partially filled slot should also be considered. The geometry of this heliostat is modeled separately for imaging, and for shading and blocking. For imaging the true area of glass is obtained by suming over the reflective areas of the panels. For shading and blocking the outer profile is required which must include the margins as shown in Figure 6. It may also include the corners for convenience. We recommend that the margin effect should be included in the model since it relates to both cost and performance. It would then be possible to do trade studies with and without margins.
REFERENCES


Appendix A) List of Fortran Variables used in the Shading and Blocking subroutine RSABS and its subroutine EVENT.

Appendix B contains a complete listing of RSABS and EVENT. Since RSABS is adapted to operation in the cellwise performance program its common groups may contain some irrelevant variables, which will not be discussed here.

RSABS and EVENT are connected by the common group DIMSS, and INPUT is connected to RSABS by HELI2 which contains the basic linear dimensions for the split rectangular heliostat.
Appendix A) List of Fortran Variables used in RSABS and EVENT

EVENT contains the following variables.

<table>
<thead>
<tr>
<th>Group</th>
<th>Variable</th>
<th>Purpose</th>
</tr>
</thead>
<tbody>
<tr>
<td>ARG</td>
<td>BU</td>
<td>U component of boundary vector for current side</td>
</tr>
<tr>
<td>ARG</td>
<td>BV</td>
<td>V component of boundary vector for current side</td>
</tr>
<tr>
<td>DIMSS</td>
<td>CL2</td>
<td>Half width of rectangle in U direction</td>
</tr>
<tr>
<td>DIMSS</td>
<td>CW2</td>
<td>Half width of rectangle in V direction</td>
</tr>
<tr>
<td>ARG</td>
<td>ICORN</td>
<td>Number of boundary points</td>
</tr>
<tr>
<td>ARG</td>
<td>IFRT</td>
<td>Index of first point in final group</td>
</tr>
<tr>
<td>ARG</td>
<td>IGON</td>
<td>Index of first inside point</td>
</tr>
<tr>
<td>ARG</td>
<td>IGOT</td>
<td>Index of last inside point</td>
</tr>
<tr>
<td>DIMSS</td>
<td>INDEX</td>
<td>Index of high point</td>
</tr>
<tr>
<td></td>
<td>INN</td>
<td>Number of inside points</td>
</tr>
<tr>
<td>IS</td>
<td></td>
<td>DO200 loop parameter</td>
</tr>
<tr>
<td>IS1</td>
<td></td>
<td>DO202 loop control for JCORN&gt;0</td>
</tr>
<tr>
<td>IS2</td>
<td></td>
<td>DO202 loop control for JCORN&lt;0</td>
</tr>
<tr>
<td>JCORN</td>
<td></td>
<td>Change in ICORN</td>
</tr>
<tr>
<td>JINDEX</td>
<td></td>
<td>Branch control for loading new points</td>
</tr>
<tr>
<td>K</td>
<td></td>
<td>DO150 loop parameter</td>
</tr>
<tr>
<td>KFRT</td>
<td></td>
<td>Index of IFRT after shift</td>
</tr>
<tr>
<td>LAST</td>
<td></td>
<td>Index of last point in fixed group</td>
</tr>
<tr>
<td>NEW</td>
<td></td>
<td>Number of new points</td>
</tr>
<tr>
<td>ARG</td>
<td>UBC</td>
<td>U component of shading/blocking (center point)</td>
</tr>
<tr>
<td>Group</td>
<td>Variable</td>
<td>Purpose</td>
</tr>
<tr>
<td>-------</td>
<td>----------</td>
<td>---------------------------------------------------</td>
</tr>
<tr>
<td></td>
<td>UBP</td>
<td>U component of shading or blocking (plus side)</td>
</tr>
<tr>
<td>ARG</td>
<td>USH</td>
<td>U component of shift for slot</td>
</tr>
<tr>
<td></td>
<td>USHP</td>
<td>U component of shift for slot</td>
</tr>
<tr>
<td>VBC</td>
<td></td>
<td>V component of shading or blocking (center point)</td>
</tr>
<tr>
<td>VBP</td>
<td></td>
<td>V component of shading/blocking (plus side)</td>
</tr>
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</table>
RSABS contains the following variables in addition to those listed above for EVENT:

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<th>Group</th>
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<th>Purpose</th>
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</thead>
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<td>Intermediate variables</td>
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<td>&quot;</td>
</tr>
<tr>
<td>C</td>
<td>&quot;</td>
<td>&quot;</td>
</tr>
<tr>
<td>D</td>
<td>&quot;</td>
<td>&quot;</td>
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<tr>
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<td>U component of standard boundary vector.</td>
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</tr>
<tr>
<td>AV</td>
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</tr>
<tr>
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</tr>
<tr>
<td>BV</td>
<td>V component of boundary vector for left side</td>
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<td>U component of boundary vector for right side</td>
<td></td>
</tr>
<tr>
<td>CV</td>
<td>V component of boundary vector for right side</td>
<td></td>
</tr>
<tr>
<td>DIMSS</td>
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<td>Width of Rectangle in U direction</td>
</tr>
<tr>
<td></td>
<td>&quot;</td>
<td>Half width of Rectangle in U direction</td>
</tr>
<tr>
<td></td>
<td>CL2</td>
<td>Width of Rectangle in V direction</td>
</tr>
<tr>
<td></td>
<td>&quot;</td>
<td>Half width of rectangle in V direction</td>
</tr>
<tr>
<td>GRP6</td>
<td>COSI</td>
<td>Cosine of incidence for heliostat</td>
</tr>
<tr>
<td></td>
<td>COSZZ</td>
<td>Cosine of azimuth around tower</td>
</tr>
<tr>
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<td>DHNX</td>
<td>X component of displacement of neighbor</td>
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<tr>
<td></td>
<td>DHNY</td>
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<td></td>
<td>DHNZ</td>
<td>Z component of displacement of neighbor</td>
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<td>DMINR</td>
<td>Heliostat size parameters for layout</td>
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<td>Projection of DHN onto UNOR.</td>
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<td>Projection of DNH onto U axis of Helios</td>
</tr>
<tr>
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<td>DVN</td>
<td>Projection of DHN onto V axis of Helios</td>
</tr>
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<td>DUS</td>
<td>Projection of USUN onto U axis of Helios</td>
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<td>DVS</td>
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</tr>
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<td>Description</td>
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</tr>
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<td>----------</td>
<td>-------------</td>
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<tr>
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</tr>
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<td>Actual reflecting area of heliostat</td>
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<tr>
<td>I</td>
<td>DO 101 loop parameters, etc.</td>
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</tr>
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<tr>
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</tr>
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<tr>
<td>J</td>
<td>Do 101 loop parameters</td>
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<tr>
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</tr>
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<td>NCELT</td>
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<td></td>
</tr>
<tr>
<td>ROTYZ</td>
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<td>SB</td>
<td>Field array to output neighbors causing events</td>
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<td>Sine of azimuth around tower</td>
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<td>=SLOT/DMIR</td>
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<td>=SL/2</td>
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<td>Intermediate value of SB</td>
<td></td>
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<td>U component of blocking after shift</td>
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</tr>
<tr>
<td>UGRNDX</td>
<td>Y component of normal to collector field</td>
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</tr>
<tr>
<td>URGNDY</td>
<td>Z component of normal to collector field</td>
<td></td>
</tr>
</tbody>
</table>
HELII2  UMIR  U component of heliostat width
_GRP5  UNORX  X component of normal to heliostat
        UNORY  Y component of normal to heliostat
        UNORZ  Z component of normal to heliostat
        USC    U component of shading (center point)
        USH    U component of shift for events
_GRP5  USUNX  X component of direction towards sun
        USUNY  Y component of direction towards sun
        USUNZ  Z component of direction towards sun
_GRP3  UUX    X component of U axis of heliostat
        UUY    Y component of U axis of heliostat
        UUZ    Z component of U axis of heliostat
        UVX    X component of V axis of heliostat
        UVY    Y component of V axis of heliostat
        UVZ    Z component of V axis of heliostat
        VBC    V component of blocking (center point)
        VC     =VBC or VSC
_HELII2 VMIR  V component of heliostat width
        VSC    V component of shading (center point)
        WDX    =XGRND(IMIR, JMIR)
        WDY    =YGRND(IMIR, JMIR)
        XA     X component of cell centers
        XAA    X component of intermediate variables
        XCM    X component of data for cornfield neighborhoods
        XGRND  Radial spacing parameters for neighbors
        XS     X component of spacing for neighbors
        XSM    X component of data locating staggering neighborhoods
_GRP5  XTPHI  X component of subreceiver point
        YA     Y component of cell centers
        YAA    Y component of intermediate variables
        YCM    Y component of data for cornfield neighborhoods
        YGRND  Azimuthal spacing parameters for neighbors
        YS     Y component of spacing for neighbors
        YSM    Y component of data locating staggered neighborhoods
_GRP5  YTPHI  Y component of subreceiver point
        ZB     Azimuthal angle of cell center with respect to subreceiver point
Appendix B) List of Code for RSABS and EVENT (line 244 ff)

1*#RUN *|=; HSELCG1496/XY/R-RSABS (BCD,NOGO,OPTZ)
2       SUBROUTINE SAB3(NCELI,NCELJ,NCELJ4,SB,XGRND,YGRND,XA,YA)
3C
4C       * * * * * SLOTED RECTANGULAR HELIOSTATS * * * * *
5C
6C       SHADING AND BLOCKING FOR CELL MODEL OF LARGE SYSTEM
7C       INPUTS BOUNDARY OF HELIOSTAT AND ARRANGEMENT OF ITS NEIGHBORS
8C       OUTPUTS BOUNDARY OF LUMINOUS REGION AND ITS AREA
9C       IPSAB PRINT OPTIONS - 2 GIVES DIAGNOSTIC OUTPUT
10C      PARALLEL PROJECTIONS
11C      INCLINED FIELD OPTION (ROT**)
12C      VARIABLE LIST OF NEIGHBORS
13C      FOUR DIFFERENT NEIGHBORHOODS AVAILABLE
14C      KORY = 1 FOR RADIAL ORIENTATION
15C      KORY = 2 FOR NORTH-SOUTH ORIENT.
16C      LRAY = 1 FOR CORNFIELD NEIGHBORHOODS
17C      LRAY = 2 FOR STAGGERED NEIGHBORHOODS
18C      SB FOR OUTPUT OF EVENTS
19C
20C      * * * * * * * F W LIPPS JUNE 1979 * * * * * * *
21C
22C
23C      INTEGER SB
24C      LOGICAL IBLOK,ISHAD
25C       COMMON /CELL/ DA,AC,NTOWI,NTOWJ,NBOR,KORY,LRAY,LGEO,DTRIM,
26C          &          NORDER
27C       COMMON /HELO/ NGON,IAXIS,RH,WH,DMIR,DMECH,HGLASS,CHL(3)
28C       COMMON /HELI2/ UMIR,VMIR,SLOT
29C       COMMON /DIMSS/ CL,CW,CL2,CW2,INDEX
30C       COMMON /PRINT/IFINT,JDISK,KDISK,LDISK,IPDAY,IPLONG,IFLUX,
31C          &          IPSAB,IPMIR,IPANCT,ENERGY,TRMF,TRMI
32C       COMMON /SITE/ XLAT,ILAT,HS,EGRND,IGRND
33C       COMMON /GRPSB/UGRNDX,UGRNDY,UGRNDF,XTPHI,YTPHI,
34C          &          ROTXX,ROTXY,ROTYY,ROTXZ,ROTYZ
35C       COMMON /GRP3/UUX,UUY,UUX,UUX,UUY,UXZ,URECX,URECY,URECZ
36C       COMMON /GRP4/UXX,UXY,UXZ,UYZ,UYZ,RJS,RJS2,SINASQ
37C       COMMON /GRP5/UNORX,UNORY,UNORZ,USUNX,USUNY,USUNZ,RSTAR
38C       COMMON /GRP6/IMIR,JMIR,CO5I, SOLARA,FMI RX
39C       DIMENSION BU(18),BV(18),CU(18),CV(18),AU(4),AV(4)
40C       DIMENSION SB(NCELI,NCELJ)
41C       DIMENSION XA(NCELI),YA(NCELJ)
42C       DIMENSION XGRRD(NCELI,NCELJ),YGRND(NCELI,NCELJ)
43C       DIMENSION XSM(24),YSM(24),XCM(24),YCM(24)
44C       DATA XSM/1.0,0.5,0.0,0.0,0.5,0.0,0.5,0.2,0.1,0.5,1.0,0.5,
45C          &          0.0,-0.5,-1.5,-2.0,-1.5,-2.0,-1.5,-2.0,0.5,0.1,0.5/,
46C       DATA YSM/0.0,0.5,0.0,0.5,0.0,-0.5,-1.0,-0.5,0.0,0.0,0.5,1.0,0.5,
47C          &          2.0,1.5,0.0,0.5,0.0,-0.5,-1.0,-1.5,-2.0,-1.5,-1.0,-0.5/,
48C       DATA XCM/1.1,0.1,0.0,-1.1,-1.0,0.1,2.0,2.0,2.0,1.0,
49C          &          0.0,-2.0,-2.0,-2.0,-2.0,-1.0,0.1,2.0,2.0/,
50C       DATA YCM/0.1,1.1,0.0,-0.1,-1.0,0.1,2.0,2.0,
& 2.2.2.1.0.-1.-2.-2.-2.-2.-2.-1./
51 DATA INIT/0/
52 IF (INIT.EQ.1) GO TO 103
53 INIT = 1
55C
56 CL=(UMIR-SLOT)/(2.*DMIR)
57 CW=VMIR/DMIR
58 SL=SLOT/DMIR
59 CL2=CL/2.
60 CW2=CW/2.
61 SL2=SL/2.
63 UCNTR2=2.*UCNTR
64 FINVER=.250/(CL*CW)
65 AU(1)= CL2
66 AV(1)= CW2
67 AU(2)= -CL2
68 AV(2)= CW2
69 AU(3)= -CL2
70 AV(3)= -CW2
71 AU(4)= CL2
72 AV(4)= -CW2
73 IF(NGNNE.4)STOP
74 NGONP = 5
75 PHIM=3.1415965/2.
76C
77 103 IF(KORY.EQ.2)GO TO 104
78C
79C ** FOR RADIAL ORIENTATION **
80 ZB = 0
81 IF(ABS(YTPHI-YA(JMIR)).GT.1E-6,OR.ABS(XTPHI-XA(IMIR)).GT.1E-6)
82 & ZB = ATAN2(YTPHI-YA(JMIR),XTPHI-XA(IMIR))
83 COSZZ = CO SCZ B>
84 SINZZ = SIN(ZB)
85C
86 104 WDX = XGRND(IMIR,JMIR)
87 WDY = YGRND(IMIR,JMIR)
88C
89INDEX LOADS HIGHEST VERTEX INTO FIRST CORNER OF(BU,BV)
90C CA- VERSION WORKS FOR ALL MOUNTING SYSTEMS WITH K=2,ICORN
91C INDEX = 0 OR 2 FOR ALT-AZIMUTHAL MOUNTINGS WITH K=3,ICORN
92C
93INDEX = 0
94 A = UGRNDX*UNORX + UGRNDY*UNORY + UGRNDZ*UNORZ
95 IF(A .GT. .9999) RETURN
96 B = UGRNDX*UVX + UGRNDY*UVY + UGRNDZ*UVZ
97 IF(B.LT.0.)INDEX = 2
98CA- C = UGRNDX*UUX + UGRNDY*UUY + UGRNDZ*UUZ
99CA- PHIH = ATAN2(B/UMIR,C/VMIR)/PHIM
100CA- IF(PHIH.LT.0.0) PHIH = 4.0 + PHIH
INDEX = INT PHIH
DO 101 I = 1, NGON
J = I + INDEX
IF (J.GT. NGON) J = J - NGON
BU (I) = AU (J) - UCNTR
BV (I) = AV (J)
CU (I) = AU (J) + UCNTR
CV (I) = AV (J)
CONTINUE
DO 102 I = NGONP, 18
BU (I) = 0.
BV (I) = 0.
CU (I) = 0.
CV (I) = 0.
ICORN1 = NGON
ICORN2 = NGON
DUS = UX*USNX + UY*USNY + UZ*USNZ
DVS = UX*USNX + UY*USNY + UZ*USNZ
SCAN NEIGHBORS FOR SHADING AND BLOCKING OF BOTH SIDES
DO 115 I = 1, NBOR
IF (LRAY.EQ.1) GO TO 116
** STAGGERED NEIGHBORS **
XS = XSM (I) * WDX
YS = YSM (I) * WDY
GO TO 117
** CORNFIELD NEIGHBORS **
XS = XCM (I) * WDX
YS = YCM (I) * WDY
IF (KORY.EQ.2) GO TO 118
** FOR RADIAL FIELDS **
XAA = COSZZ*XS - SINZZ*YS
YAA = SINZZ*XS + COSZZ*YS
GO TO 119
FOR N-S FIELDS
XAA = XS
YAA = YS
IF (ABS (EGRND).LT.0.0001) GO TO 120
** FOR INCLINED FIELDS **
DHNX = XAA*ROTXX + YAA*ROTXY
DHNY = XAA*ROTXY + YAA*ROTYY
DHNZ = XAA*ROTXZ + YAN*ROTYZ
GO TO 121

FOR LEVEL FIELDS

120 DHNX = XAA
121 DHNY = YAA
122 DHNZ = 0.

123 DPN = UNORX*DHNX+UNORY*DHNY+UNORZ*DHNZ
124 IF(DPN.LT.0.0001)GO TO 115
125 DUN = UUX*DHNX+UUY*DHNY+UUZ*DHNZ
126 DVN = UVX*DHNX+UVY*DHNY+UVZ*DHNZ
127 DPNC= DPN/COSI
128 UBC = DUN + DUS*DPNC
129 VBC = DVN + DVS*DPNC
130 USC = DUN - DUS*DPNC
131 VSC = DVN - DVS*DPNC
132 UC = UBC - UCNTR
133 VC = VBC

IBLOK = .F.
134 IF(ABS(VBC).GT.CW)GO TO 122
135 IF(ABS(UBC).GT.CL)GO TO 131
136 CALL EVENT(UBC,UC,VC,BU,BV,ICORN1,IGON)
137 IF(IGON.NE.0)IBLOK = .T.
138 USH = UBC - UCNTR2
139 IF(ABS(USH).GT.CL)GO TO 132
140 CALL EVENT(USH,UC,VC,CU,CV,ICORN2,IGON)
141 IF(IGON.NE.0)IBLOK = .T.
142 UC = UBC + UCNTR
143 USH = UBC + UCNTR2
144 IF(ABS(USH).GT.CL)GO TO 133
145 CALL EVENT(USH,UC,VC,BU,BV,ICORN1,IGON)
146 IF(IGON.NE.0)IBLOK = .T.
147 USH = UBC - UCNTR2
148 IF(ABS(USH).GT.CL)GO TO 134
149 CALL EVENT(USH,UC,VC,CU,CV,ICORN2,IGON)
150 IF(IGON.NE.0)IBLOK = .T.

UC = USC - UCNTR
151 VC = VSC

ISHAD = .F.
152 IF(ABS(VSC).GT.CW)GO TO 123
153 IF(ABS(USC).GT.CL)GO TO 135
154 CALL EVENT(USC,UC,VC,BU,BV,ICORN1,IGON)
155 IF(IGON.NE.0)ISHAD = .T.
156 USH = USC - UCNTR2
157 IF(ABS(USH).GT.CL)GO TO 136
158 CALL EVENT(USH,UC,VC,CU,CV,ICORN2,IGON)
159 IF(IGON.NE.0)ISHAD = .T.
160 UC = USC + UCNTR
200 USH = USC + UCNTR2
201 IF(ABS(USH).GT.CL)GO TO 137
202 CALL EVENT(USH,UC,VC,BU,BV,ICORN1,IGON)
203 IF(IGON.NE.0)ISHAD = .T.
204 137 IF(ABS(USC).GT.CL)GO TO 123
205 CALL EVENT(USC,UC,VC,CU,CV,ICORN2,IGON)
206 IF(IGON.NE.0)ISHAD = .T.
207 123 CONTINUE
208C
209 IF(.NOT.IBLOK)GO TO 124
210 JMIRP = JMIR + NCELJ
211 SBLOK = SB(IMIR,JMIRP)
212 IF(SBLOK.NE.0)JMIRP = JMIRP + 2*NCELJ
213 SB(IMIR,JMIRP)=I
214 124 IF(.NOT.ISHAD)GO TO 115
215 JMIRP = JMIR
216 SSHAD = SB(IMIR,JMIRP)
217 IF(SSHAD.NE.0)JMIRP = JMIRP + 2*NCELJ
218 SB(IMIR,JMIRP)=I
219C
220 115 CONTINUE
221 FMIRX=0.
222 DO 400 I=3,ICORN1
223 A=BU(I-1)-BU(1)
224 B=BV(I-1)-BV(1)
225 C=BU(I)-BU(1)
226 D=BV(I)-BV(1)
227 FMIRX=FMIRX + A*D-B*C
228 400 CONTINUE
229 DO 401 I=3,ICORN2
230 A=CU(I-1)-CU(1)
231 B=CV(I-1)-CV(1)
232 C=CU(I)-CU(1)
233 D=CV(I)-CV(1)
234 FMIRX=FMIRX + A*D-B*C
235 401 CONTINUE
236 FMIRX = FINVER * FMIRX
237 IF(IPSAB.EQ.2)WRITE(6,29)FMIRX,IMIR,BU,JMIR,BV
238 & ,IMIR,CU,JMIR,CV
239 29 FORMAT(1X/,5X,F7.3/,1X,I4,18F7.3))
240 RETURN
241 END
242C
243C SUBROUTINE EVENT(USH,UBC,VBC,BU,BV,ICORN,IGON)
245 COMMON /DIMSS/ CL,CW,CL2,CW2,INDEX
246 DIMENSION BU(18),BV(18)
247C
248C TEST TO SET CONTROL VARIABLES
249 IGON = 0
250 DO 150 K=3,ICORN

34
IF(ABS(UBC-BU(K)).GT.CL2.OR.ABS(VBC-BV(K)).GT.CW2)GOTO 150
IF(IGON.EQ.0)IGON = K
IGOT = K
150 CONTINUE
IF(IGON.EQ.0)RETURN
USHP = USH + CL2
UBP = UBC + CL2
VBP = VBC + CW2
INN = IGOT - IGON + 1
NEW = 2
IF(2*(INN/2).NE.INN)NEW = 3
JCORN = NEW - INN
IFRT = IGOT + 1
LAST = IGON - 1
KFRT = IFRT + JCORN
IF(IGOT.EQ.ICORN)KFRT = 1
TO SHIFT TAIL OF BOUNDARY
IF(KFRT.EQ.1)GO TO 203
IF(JCORN.EQ.0)GO TO 203
IF(JCORN.GT.0)GO TO 201
LIST DECREASES IF JCORN < 0
DO 200 IS = IFRT,ICORN
BU(IS+JCORN) = BU(IS)
BV(IS+JCORN) = BV(IS)
GO TO 203
LIST INCREASES IF JCORN > 0
DO 202 IS = IFRT,ICORN
BU(IS2-IS) = BU(IS1-IS)
BV(IS2-IS) = BV(IS1-IS)
TO CALC AND LOAD NEW POINTS
ICORN = ICORN + JCORN
IF(ABS(USHP).GT.CL2)UBP = UBC - CL2
IF(ABS(VBP).GT.CW2)VBP = VBC - CW2
JNDEX = INDEX + LAST
IF(2*(JNDEX/2).EQ.JNDEX)GO TO 204
LAST POINT LEADS CONST V SEGMENT
BU(IGON) = UBP
BV(IGON) = BV(LAST)
BU(IGON+1) = UBP
BV(IGON+1) = BV(KFRT)
IF(NEW.NE.3)GO TO 205
BV(IGON+1) = VBP
BU(IGON+2) = BU(KFRT)
301   BV(IGON+2) = VBP
302   GO TO 205
303C
304C   LAST POINT LEADS CONST U SEGMENT
305  204   BU(IGON) = BU(LAST)
306   BV(IGON) = VBP
307   BU(IGON+1) = BU(KFRT)
308   BV(IGON+1) = VBP
309   IF(NEW .NE. 3) GO TO 205
310   BU(IGON+1) = UBP
311   BU(IGON+2) = UBP
312   BV(IGON+2) = BV(KFRT)
313C
314  205 CONTINUE
315   WRITE (6,29) BU, BV
316   &, INN, NEW, JCORN, ICORN, IFRT, LAST
317   29 FORMAT (5X,18F7.3/,5X,18F7.3/,10X,6I4)
318   RETURN
319   END
320C
A field of heliostats suffers losses caused by shading and blocking by neighboring heliostats. The complex geometry of multiple shading and blocking events suggests that a processing code is needed to update the boundary vector for each shading or blocking event. A new version, RSABS, (programmer's manual included) simulates the split-rectangular heliostat. Researchers concluded that the dominant error for the given heliostat geometry is caused by the departure from planarity of the neighboring heliostats. It is recommended that a version of the heliostat simulation be modified to include losses due to nonreflective structural margins, if they occur. Heliostat neighbors should be given true guidance rather than assumed to be parallel, and the resulting nonidentical quadrilateral images should be processed, as in HELIOS, by ignoring overlapping events, rare in optimized fields.