

Impact of Variable Gas Mixtures on Bubble Size Distribution and Mass Transfer in Gas Fermentation Reactors

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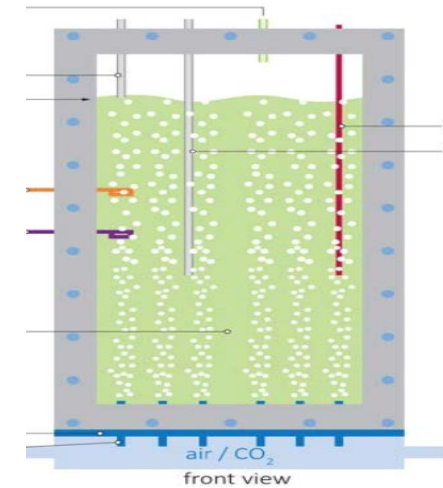
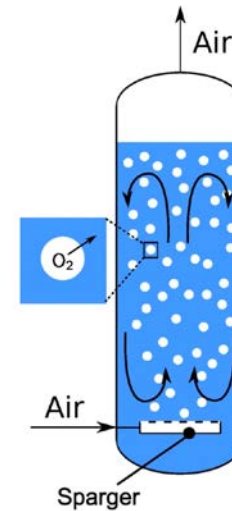
Venue: AIChE Annual Meeting 2022, Phoenix, AZ, USA

Date: 15th November 2022

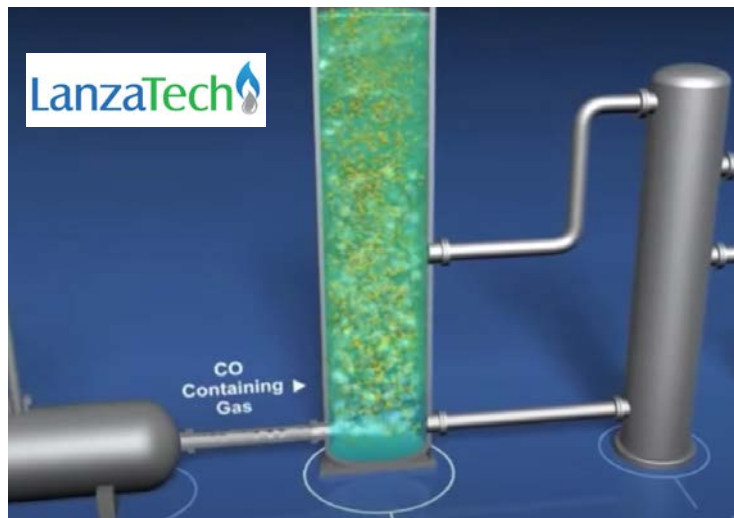
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Background

- Bioreactor: microbial action for conversion
 - Food/beverage/Pharmaceutical industry
 - **Biofuels/molecules**
 - Ethanol/Butane-diol/Methane
 - **CO₂ capture and conversion**
 - **Syngas fermentation**
- Fermentation is a large cost contributor



Flat panel bioreactor*



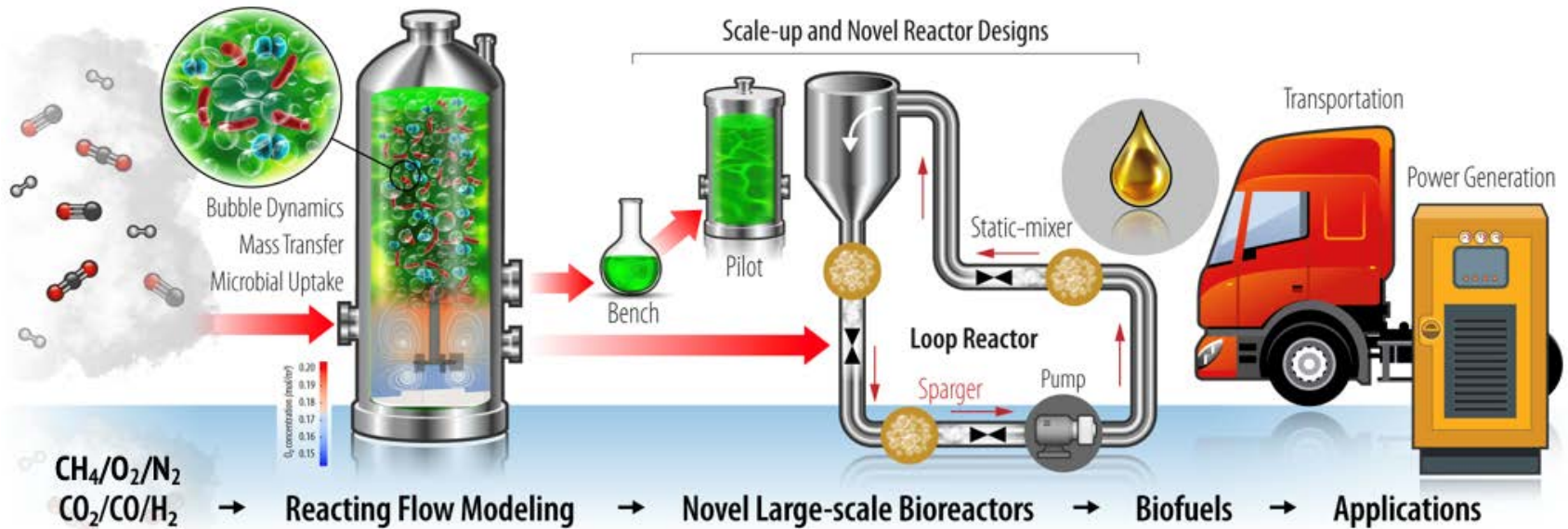
Syngas fermentation** (Lanzatech)



Biomethanation reactor (NREL)

**<https://www.youtube.com/watch?v=k3WLwKrEu7c>

Project goals



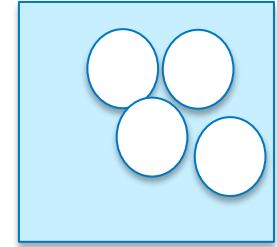
- Enable scaled-up designs and optimization of $\text{CO}_2/\text{CO}/\text{H}_2$ fermenters
 - High fidelity computational models
 - **Focus on bubble dynamics and mass transfer**
 - **Impact of gas mixtures**
 - Coupling with microbial kinetics
- Supports Department of Energy goals on
 - reducing GHG emissions and sustainable aviation fuel production
 - Accelerate lab research to industrial scale

- Model equations
 - Multiphase-Euler model
 - Bubble size distribution modeling
 - Numerical methods
- Model validation
- Bubble column simulation results
 - Hydrodynamics
 - Mass transfer
 - Sensitivities
- Conclusions

Mathematical model and numerical methods

Multiphase Euler-Euler equations

- Gas and liquid as continuous interpenetrating phases
- Compressible low Mach RANS equations



Volume fraction constraint

$$\alpha_L + \alpha_G = 1$$

$$\frac{\partial}{\partial t}(\alpha_i \rho_i) + \vec{\nabla} \cdot (\alpha_i \rho_i \mathbf{V}_i) = 0$$

Mass conservation

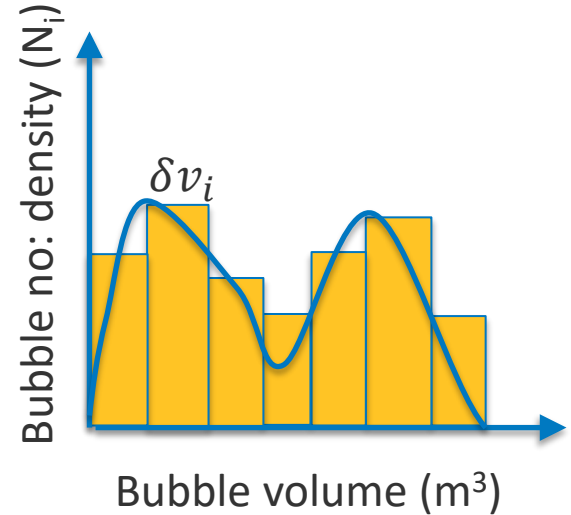
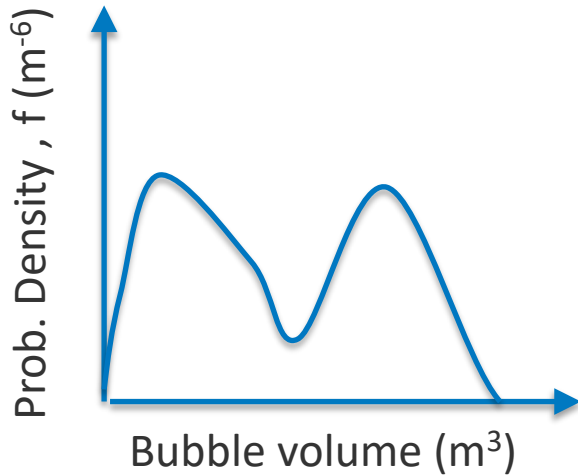
$$\begin{aligned} & \frac{\partial}{\partial t}(\alpha_i \rho_i \mathbf{V}_i) + \vec{\nabla} \cdot (\alpha_i \rho_i \mathbf{V}_i \mathbf{V}_i) \\ &= -\alpha_i \vec{\nabla} P + \alpha_i \rho_i \mathbf{g} + \vec{\nabla} \cdot (\alpha_i \bar{\mathbf{R}}_i) + \mathbf{F}_i \end{aligned}$$

Momentum conservation

$$\begin{aligned} & \frac{\partial}{\partial t}(\alpha_i \rho_i Y_{ij}) + \vec{\nabla} \cdot (\alpha_i \rho_i Y_{ij} \mathbf{V}_i) \\ &= \vec{\nabla} \cdot (\alpha_i \rho_i \bar{D}_{ij} \vec{\nabla} Y_{ij}) + \dot{R}_{ij}^{\text{MT}} \end{aligned}$$

Species transport within
each phase

Bubble size distribution* modeling



number of bubbles per unit volume $N_i = f \delta v_i$

phase fraction of each group $f_i = \frac{N_i v_i}{\sum_j N_j v_j}$

$$\frac{\partial n_v}{\partial t} + \nabla \cdot (v_{ph} n_v) = h_v$$

$$h_v = \underbrace{\frac{1}{2} \int_0^v n_{v'} n_{v-v'} C_{v',v-v'} dv'}_{\text{coalescence}(+)} - \underbrace{n_v \int_0^\infty n_{v'} C_{v,v'} dv'}_{\text{coalescence}(-)} + \underbrace{\int_v^\infty n'_v B_{v'} \beta_{v,v'} dv'}_{\text{breakup}(+)} - \underbrace{n_v B_v}_{\text{breakup}(-)} - \underbrace{\frac{\partial(v n_v)}{\partial v}}_{\text{drift}} + \underbrace{\dot{n}_v}_{\text{nucleation}}$$

PDF transport equation

Bubble dynamics source terms

Drag and mass transfer model

$$F_D = \frac{3}{4}(C_D/d)\alpha\rho_l U_r^2 * \text{sign}(U_r)$$

Drag force

$$C_D = f(Re, Eo, \alpha_g)$$

Ishii Zuber drag model

Species mass transfer (Higbie et al. ¹)

$$\text{MTR} = k_L a (C_j^* - C_j)$$

Oxygen transfer rate

$$C_j^* = \frac{X_{j,G} P}{H_i} \frac{\rho_L}{M_L}$$

Henry's law

$$k_L = \sqrt{\frac{4D}{\pi} \frac{|\mathbf{u}_{\text{slip}}|}{d_b}} \quad a = \frac{6\alpha_G}{d_b}$$

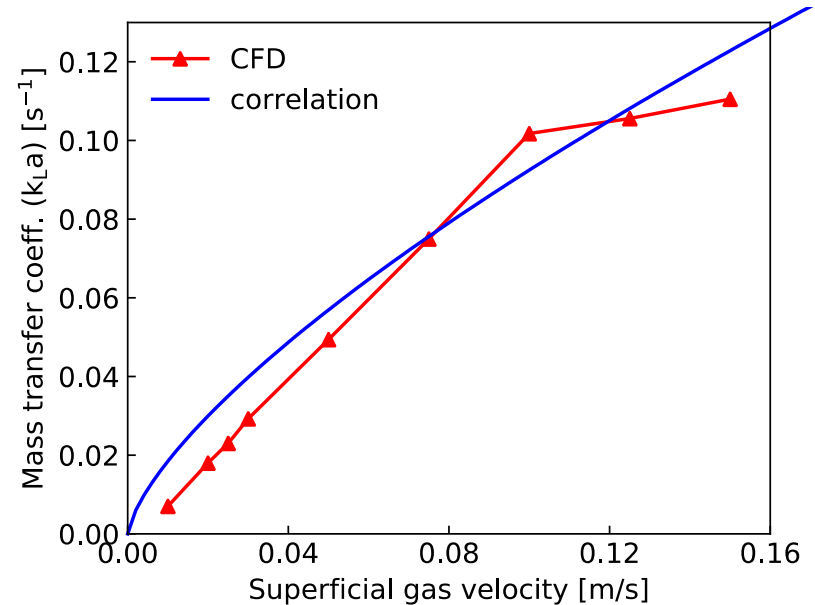
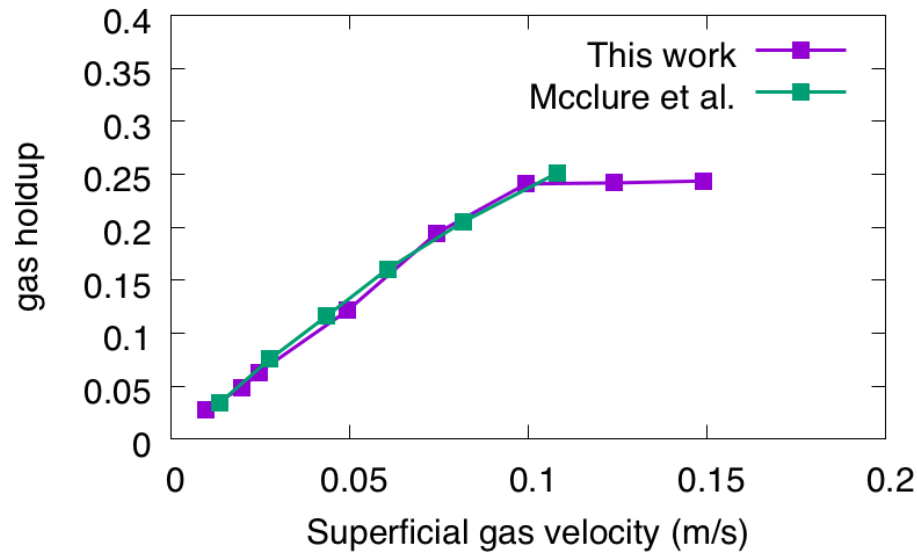
Mass transfer coefficient

¹ Higbie, R., 1935. The rate of absorption of a pure gas into a still liquid during short periods of exposure. Trans. AIChE 31, 365–389.

Numerical methods and solver

- Transport properties
 - Fermentation broth properties are similar to water
 - Multiphase $k-\omega$ SST turbulence model
 - Population balance over 1-5 mm bubbles with 10 classes
- *multiphaseEulerFoam* in OpenFOAM
 - In-house implementation of Higbie mass transfer model
- Simulations performed using
 - 128 Intel Skylake processors
 - 48 hours of run time to simulate 30 seconds for 0.5 million cells
- More details in Rahimi et al., Chem. Engg. Res. Design, 139, 2018

Model validation with small-scale bubble column



$$\text{Superficial gas velocity: } v_{g_s} = \frac{\dot{V}_{mid}}{A_{reactor}}$$

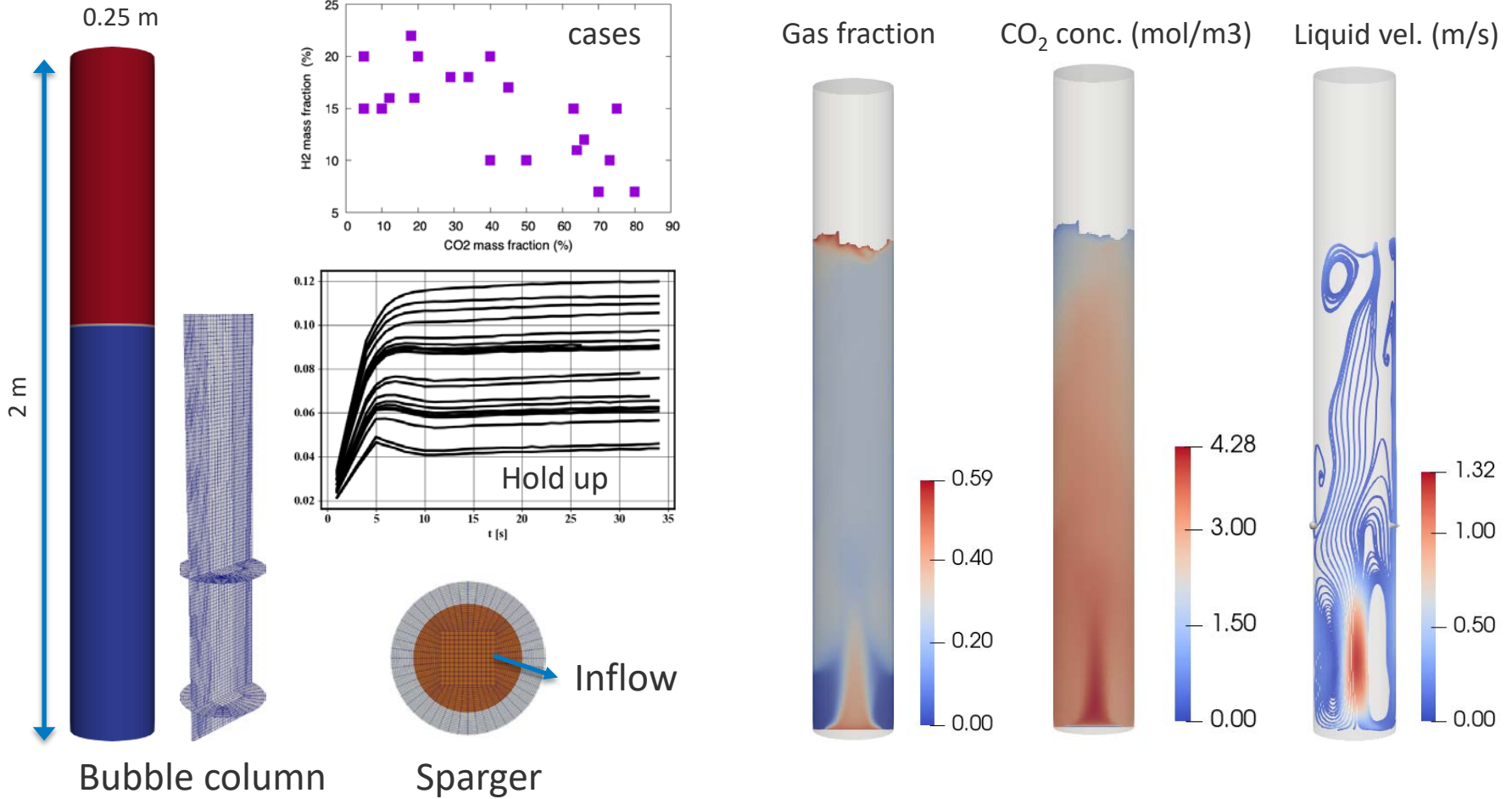
- Validation done for a small-scale bubble column (1 m height, 15 cm diameter)
- Average mass transfer coefficient matches *Heijnen and Van't Riet (1984)*¹
- Gas holdup matches experiments/simulations by McClure et al. (2013)²

¹ Heijnen, J. J., Van't Riet, K., Apr. 1984. Mass transfer, mixing and heat transfer phenomena in low viscosity bubble column reactors. Chem. Eng. J. 28 (2), B21–B42.

² McClure, D. D., Kavanagh, J. M., Fletcher, D. F., Barton, G. W., 2013. Development of a CFD model of bubble column bioreactors: Part one - a detailed experimental study. Chem. Eng. Technol. 36 (12), 2065–2070.

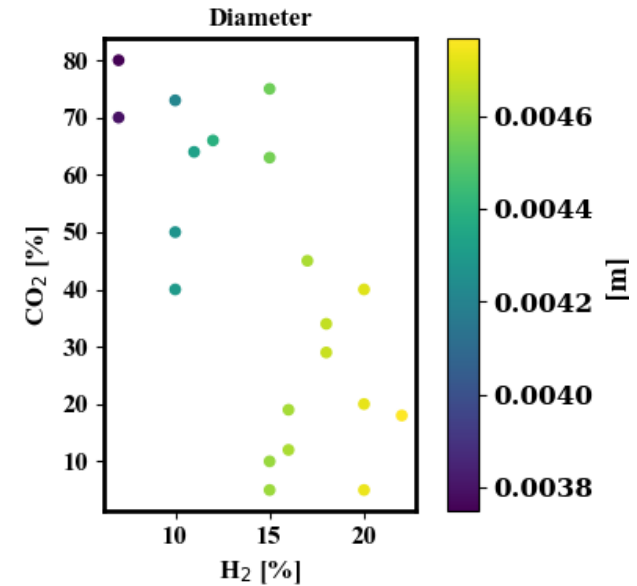
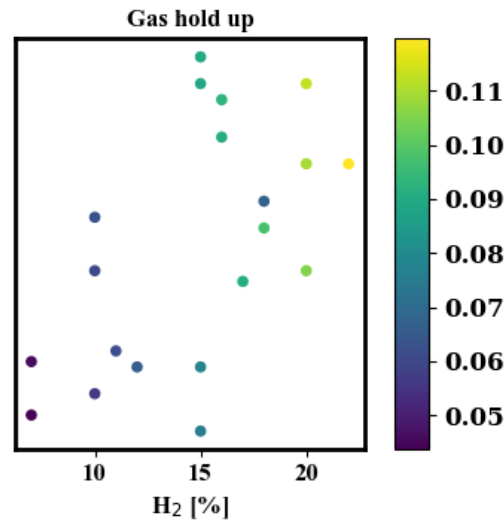
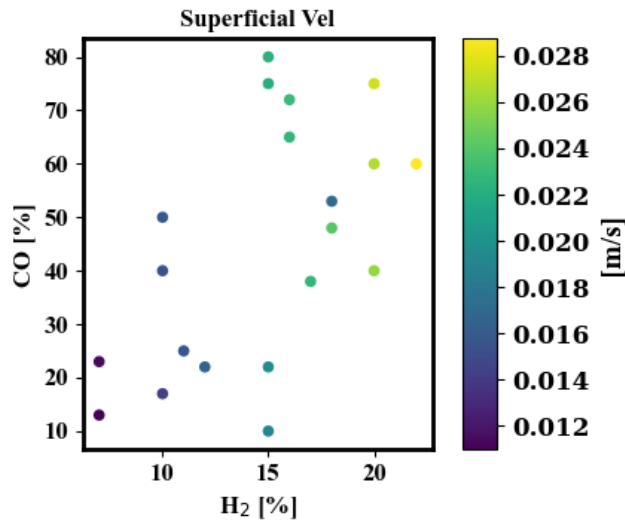
Results

Bubble column simulations

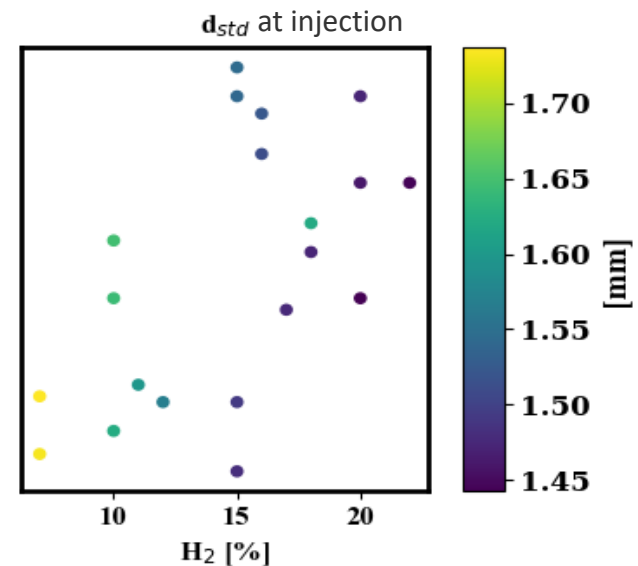


- Bottom inlet with a gas fraction that specifies sparger mass flow rate
- Lateral walls use no-slip condition for liquid and slip for gas
- Vary gas mixture mass fractions (H₂:CO₂:CO) while keeping constant mass flow rate of 0.45 g/s.

Hydrodynamic parameter variations



- Higher H₂ fractions result in higher:
 - superficial velocities
 - Gas hold up
 - Mean diameters
 - Greater spread of bubbles at the inlet
- Same mass flow results in greater volume of H₂



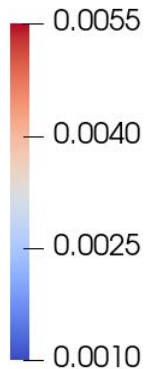
Bubble size distribution variations

Case 1 (less H₂)

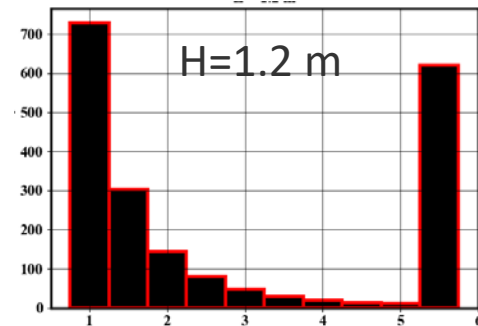
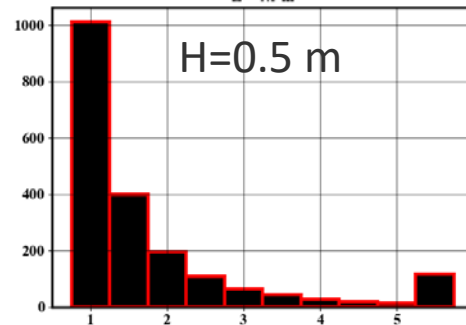
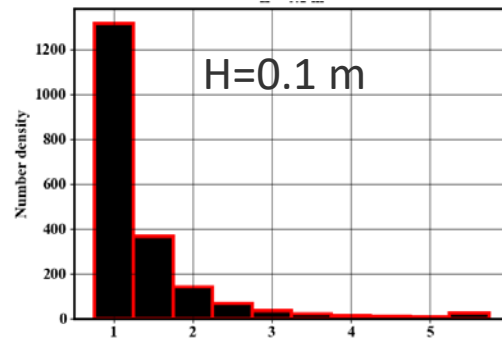
Case 2 (more H₂)



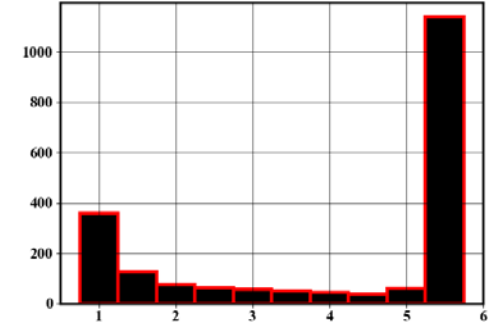
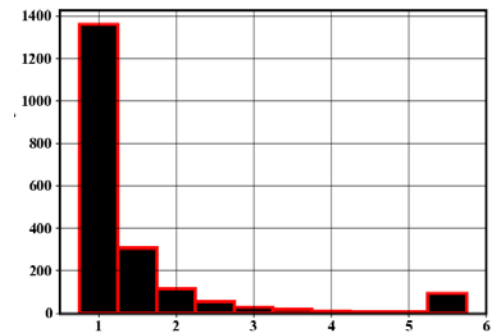
Sauter
dia (m)



Case 1 - H₂:CO₂:CO=7:80:13

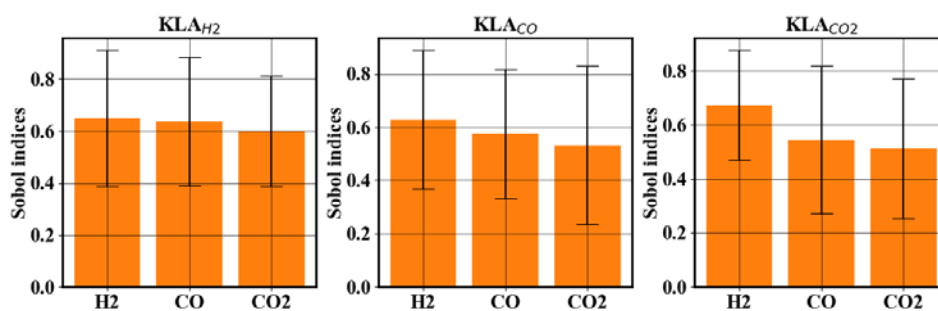
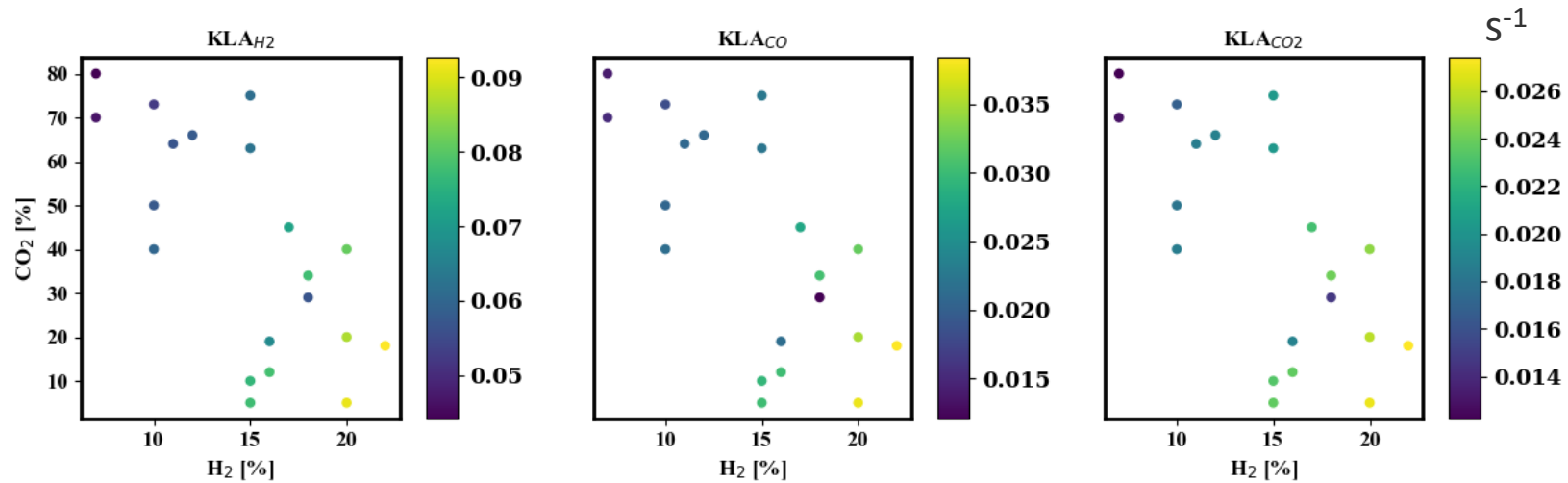


Case 2 - H₂:CO₂:CO=18:34:48

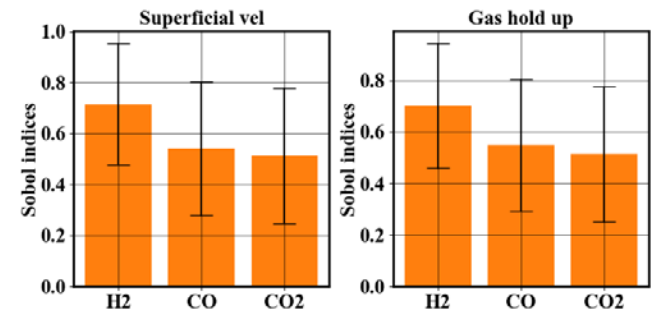


- Higher H₂ fraction at the inlet results in faster bubble coalescence and higher average Sauter diameter

Mass transfer effects



Sobol indices for mass transfer

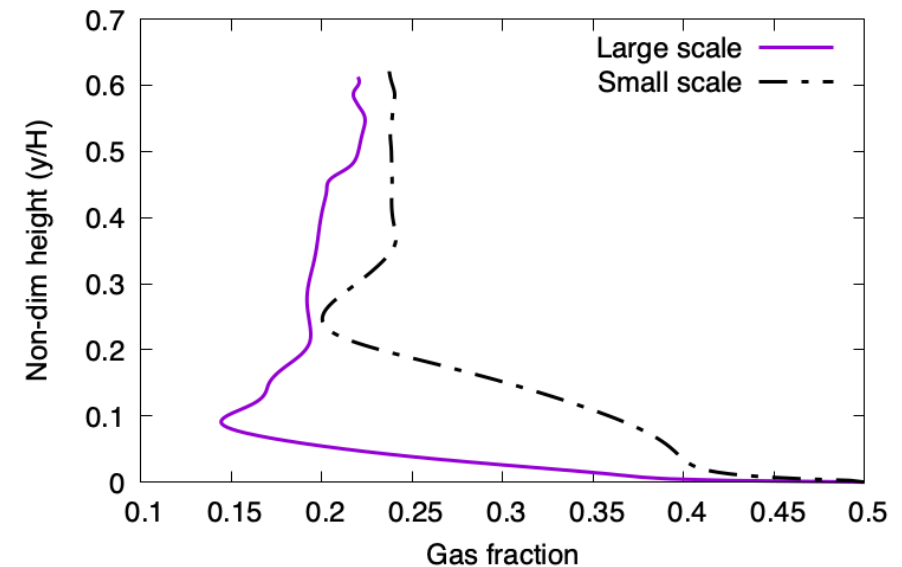
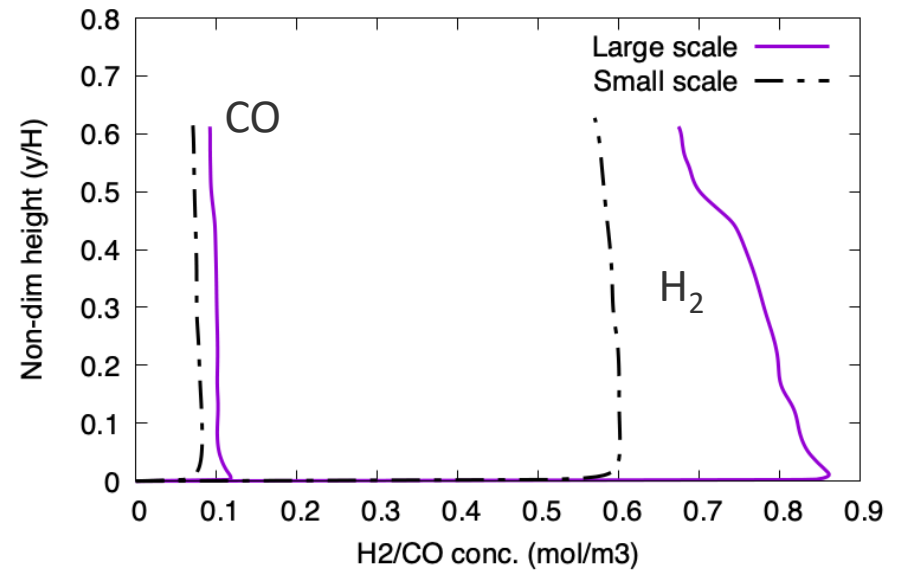
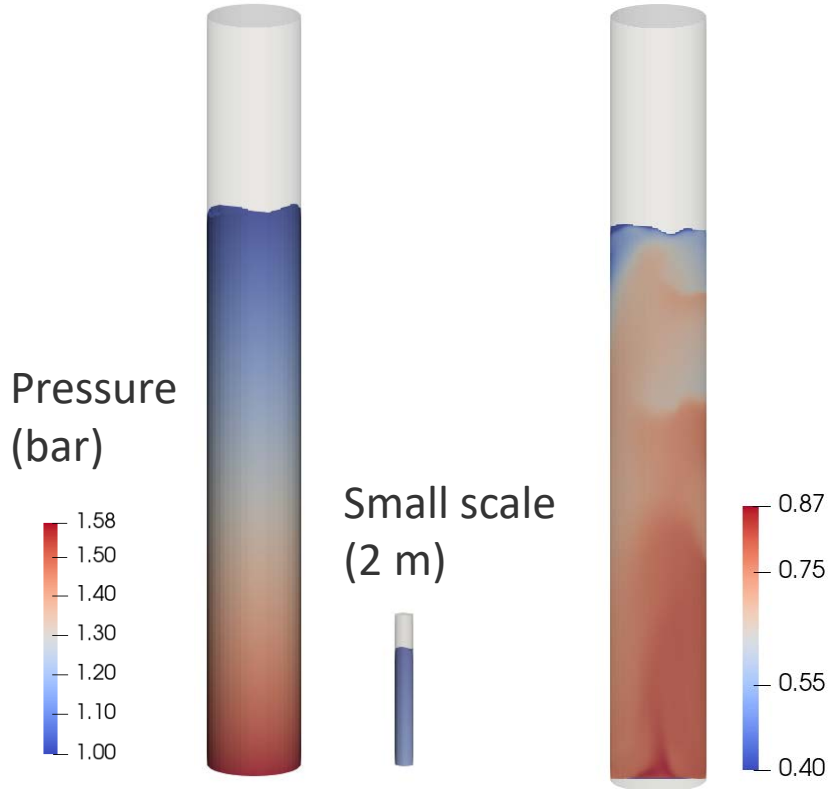


Sobol indices for hydrodynamics

- Higher H_2 results in greater mass transfer for all gases at constant mass flow rate
- Sobol indices – understanding the effect of varying one quantity with respect to total variance, indicates CO/CO_2 have lower impact than H_2

Effect of bubble column height

Large scale (10 m) H_2 conc. (mol/m³)



- Higher hydrostatic pressure head enables greater mass transfer
- Superficial velocity of 5 cm/s is kept the same between cases
- Spatial inhomogenities in species concentration and gas fraction

Conclusions and future work

- **Conclusions**
 - Computational model
 - OpenFOAM based multiphase solver
 - Gas mixtures, bubble size distributions
 - Results
 - Validated small scale bubble column
 - Ensemble simulations with H₂/CO/CO₂ mixtures
 - At constant mass flow rate
 - Greater H₂ fractions increase
 - Superficial velocities, gas holdup and mass transfer
 - Faster coalescence effects
 - Large scale vs small scale bubble column
 - inhomogenous mass transfer/gas fractions at large scale
- **Future work**
 - Microbial kinetics
 - Include product specie, CH₄, which can affect
 - Bubble size distribution and mass transfer
 - Light gas (H₂) gets consumed to heavier gas (CH₄)

Acknowledgements

U.S. DEPARTMENT OF
ENERGY

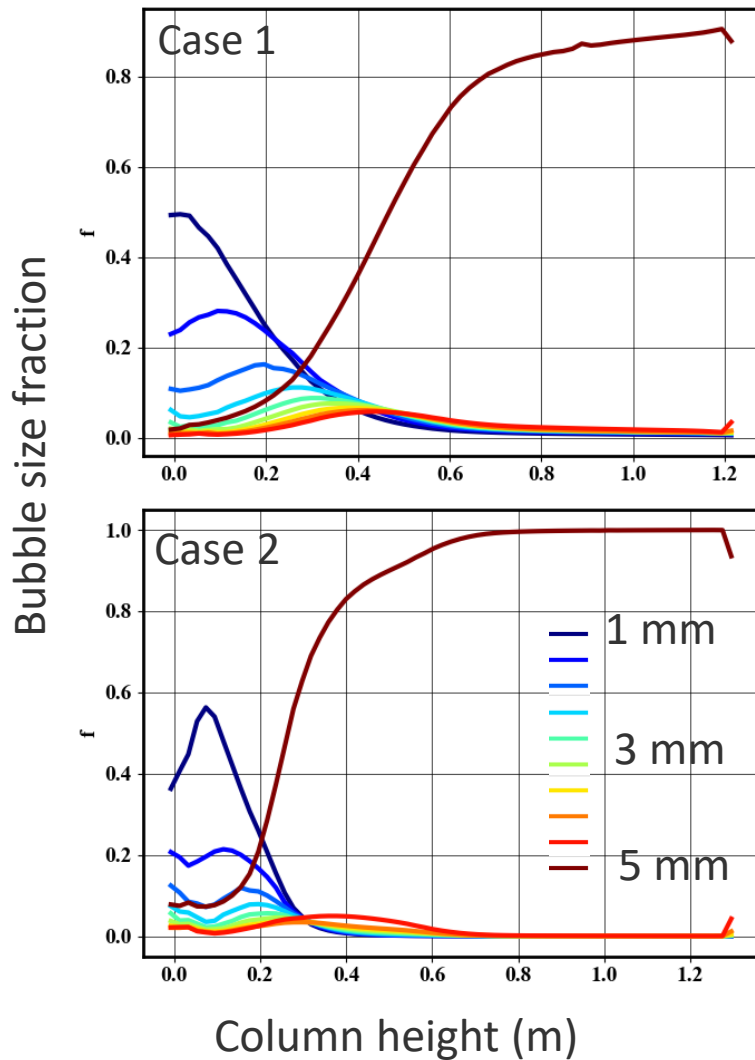
Energy Efficiency &
Renewable Energy

BIOENERGY TECHNOLOGIES OFFICE

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Thank You

Bubble size distribution variations



$H_2:CO_2:CO=7:80:13$

$H_2:CO_2:CO=18:34:48$

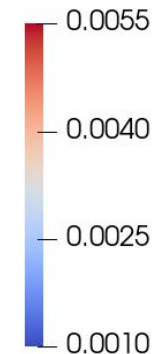


Case 1



Case 2

Sauter dia (m)



- Higher H_2 results in faster bubble coalescence and higher average Sauter diameter