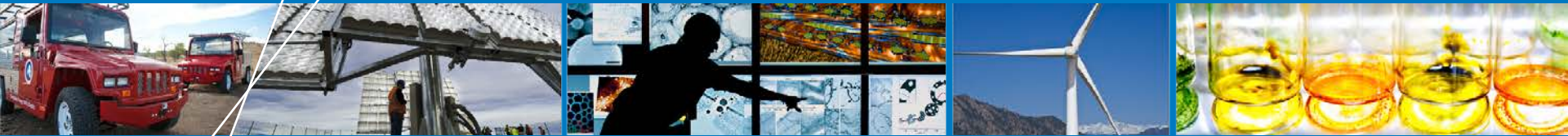


Rolling Element Bearing Stiffness Matrix Determination



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Motivation

- **Limited work on stiffness matrix in the literature**
 - Diagonal matrix approximation typically used
- **Elastic deformation of race causes nondiagonal terms**

$$\begin{bmatrix}
 k_{xx} & k_{xy} & k_{xz} & k_{x\theta_x} & k_{x\theta_y} & 0 \\
 & k_{yy} & k_{yz} & k_{y\theta_x} & k_{y\theta_y} & 0 \\
 & & k_{zz} & k_{z\theta_x} & k_{z\theta_y} & 0 \\
 & & & k_{\theta_x\theta_x} & k_{\theta_x\theta_y} & 0 \\
 & & & & k_{\theta_y\theta_y} & 0 \\
 & & & & & 0
 \end{bmatrix}$$

Symmetric

Coupling between the radial and rotational displacement

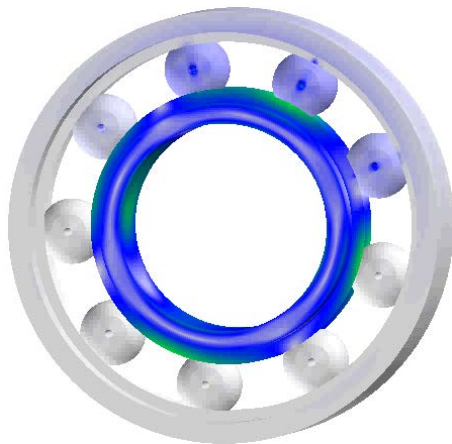
Coupling between the axial and rotational displacement

Coupling between the axial and radial displacement

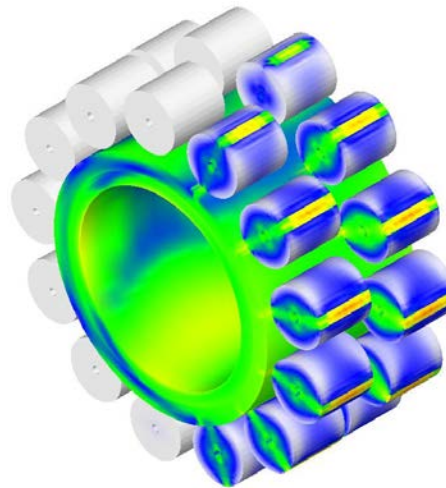
Finite Element/Contact Mechanics Model

- Three-dimensional finite element model includes microgeometry
- Analyze contact between rolling elements and races
 - Contact searched at every time instant as bearing rotates

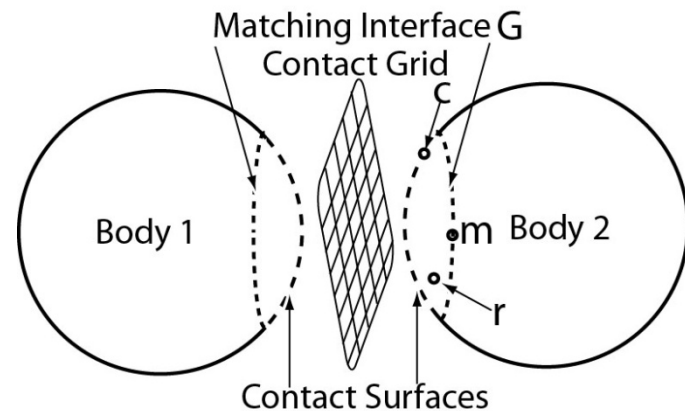
Radial Ball Bearing



Cylindrical Bearing



Contact Grid



Accuracy Order of Finite Element Analysis

- Numerical Jacobian used to compute K
- Order of Jacobian approximation formula should be comparable to the accuracy order of finite element analysis (FEA)
- Method to obtain the accuracy order of FEA

$$V_h = V + \underbrace{c_1 h^{p_1} + c_2 h^{p_2} + \dots}_{e_h}$$

$$\frac{e_{h_3} - e_{h_2}}{e_{h_2} - e_{h_1}} = \frac{V_{h_3} - V_{h_2}}{V_{h_2} - V_{h_1}} \approx \frac{h_2^{p_1} - h_3^{p_1}}{h_1^{p_1} - h_2^{p_1}}$$

$$p_1 = \frac{\log\left\{\left(\frac{V_{h_3} - V_{h_1}}{V_{h_3} - V_{h_2}}\right) \frac{\log \frac{h_2}{h_3}}{\log \frac{h_1}{h_3}}\right\}}{\log\left(\frac{h_1}{h_2}\right)}$$

V_h : finite element solution

V : exact solution

h : finite element size

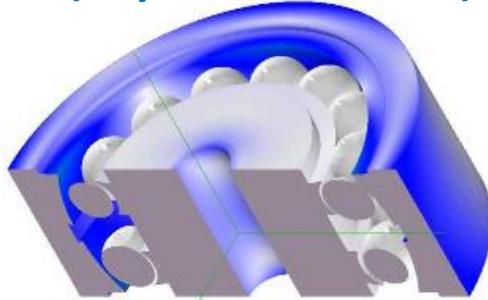
p_1 : order of accuracy

| Accuracy Order | FEA | FEA/Contact |
|----------------|------|-------------|
| p1 | 1.11 | 1.94 |

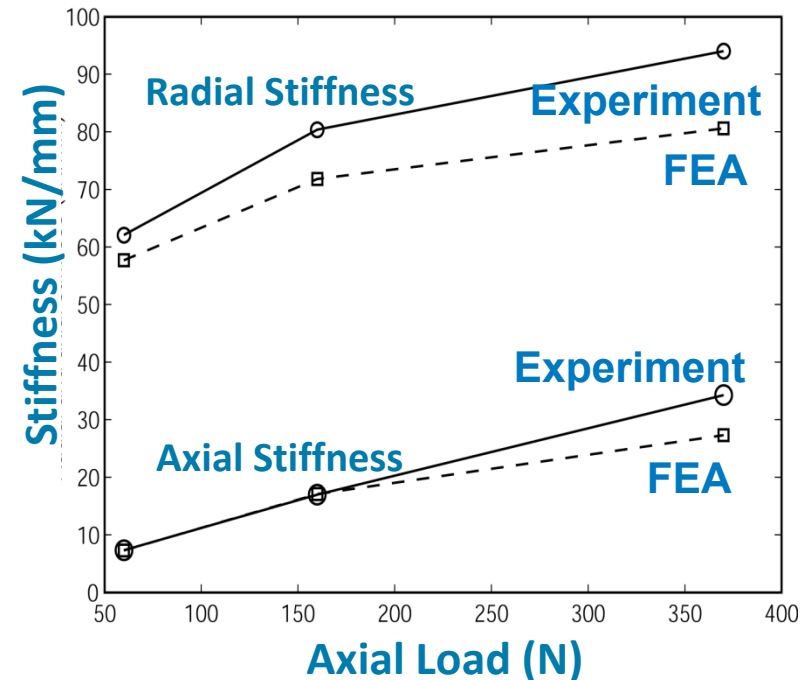
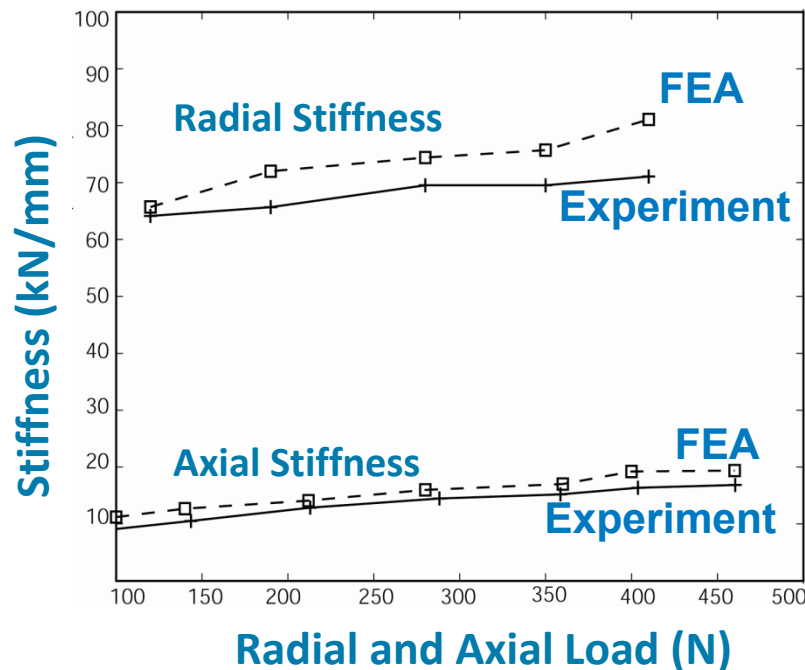
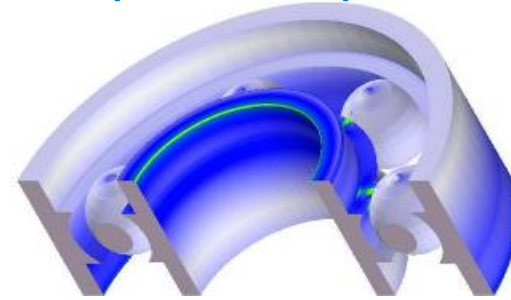
Comparison Against Published Experiments

- Calculated stiffnesses by FEA agree with experiments

(Royston et al. 1998)

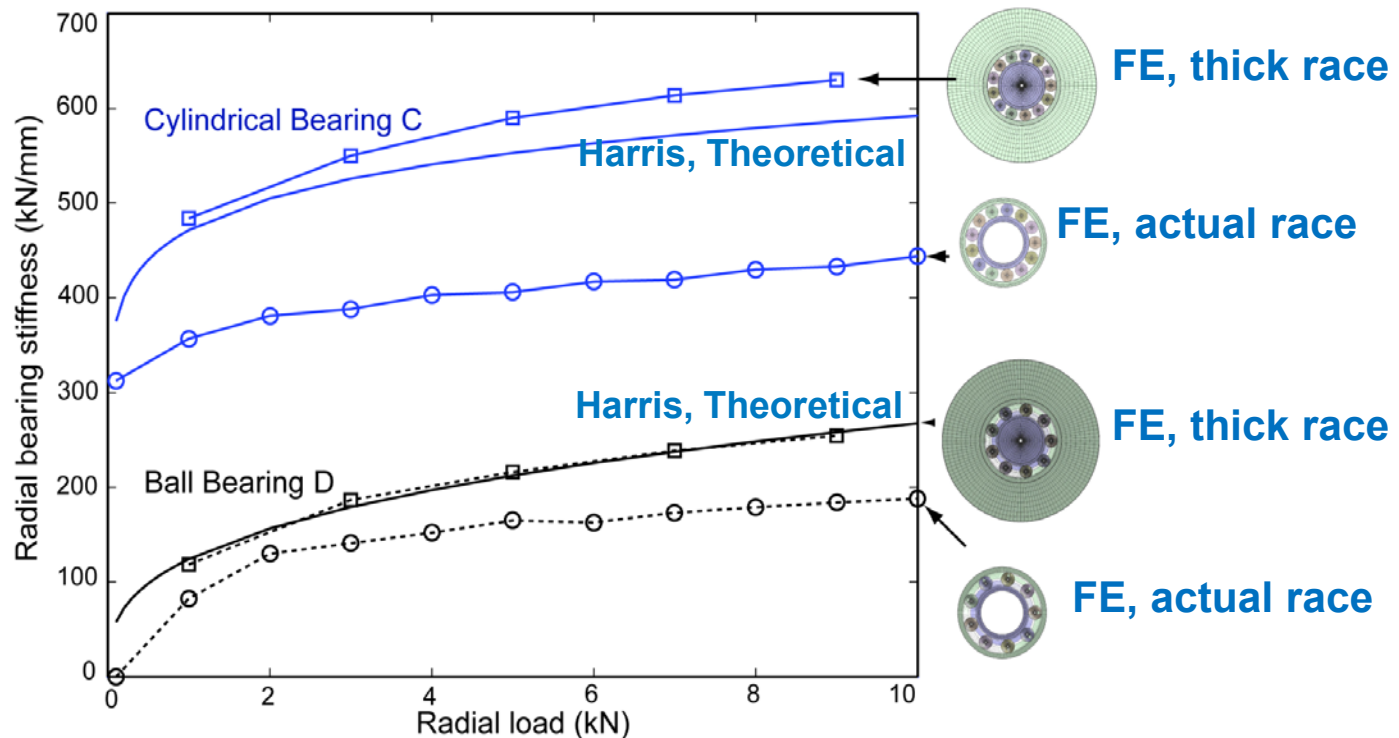


(Kraus 1987)



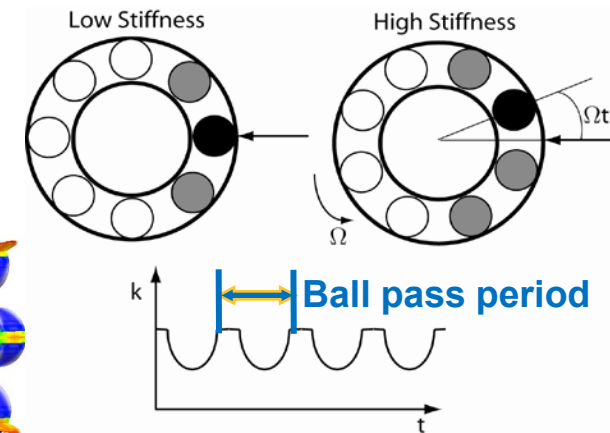
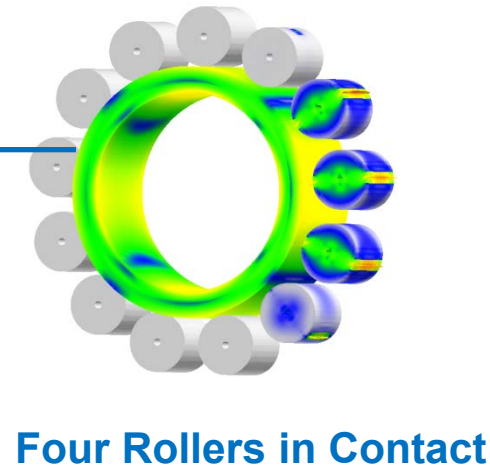
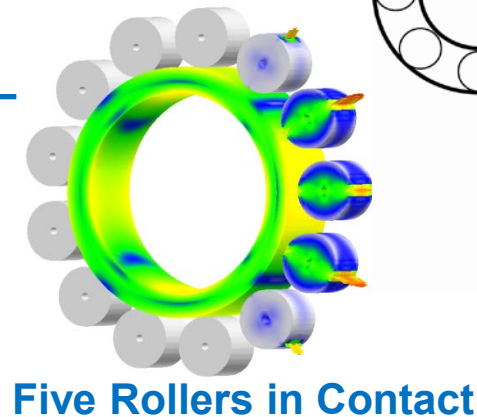
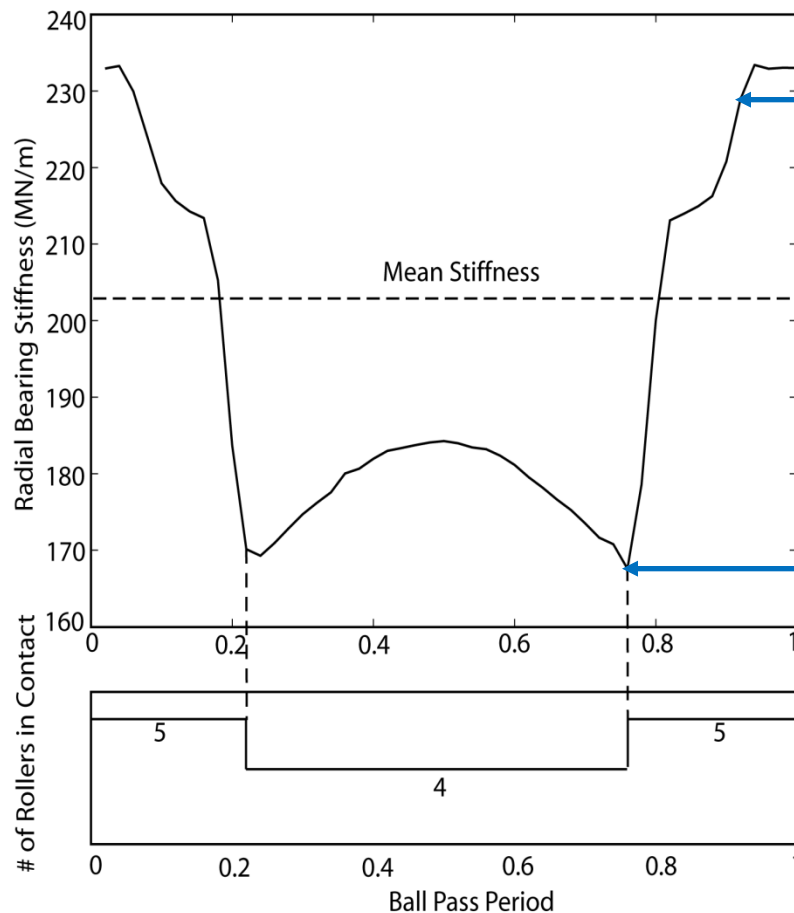
Comparison Against Theoretical Models

- FEA stiffness agrees with the theoretical model
 - Only with unrealistic races that match Harris's assumptions
- Theoretical models predict higher stiffness with design dimensions



Bearing Stiffness Is Time-Varying

- Number of rollers in contact changes periodically
- Can excite gearbox vibration



Off-Diagonal Stiffnesses Affect Gear Vibration

- Gear dynamics with off-diagonal stiffnesses differ from gear dynamics with a diagonal stiffness matrix
 - Need to include off-diagonal stiffnesses

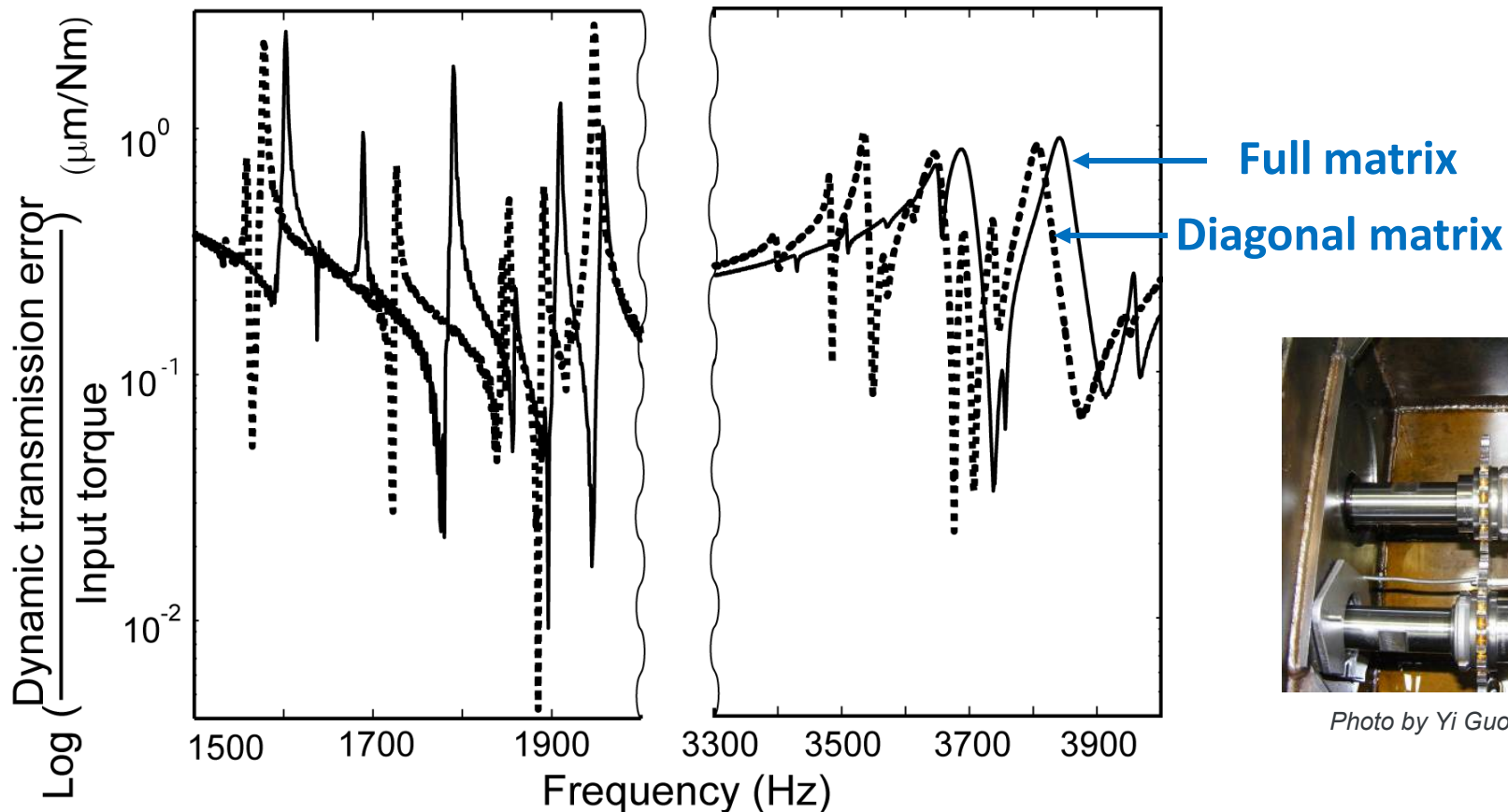


Photo by Yi Guo, NREL

Conclusions

- **A method developed to determine bearing stiffness matrices**
- **Method validated by experiments**
- **Comparison against theoretical models expose their limitations**
- **Bearing contact is nonlinear and time-varying**
- **Bearing microgeometry affects stiffness**
- **Off-diagonal bearing stiffnesses affect gear dynamics**

Thank You!

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