

Outline

- Loads modeling options for DWT
 - simplified load methodology
 - aeroelastic modeling
- Loads validation
- More about aeroelastic modeling
 - Options for different types of turbines
 - Getting into aeroelastic modeling
 - Pre and post-processing
- Other useful tools



Simplified loads model

- Simple, conservative equations
- Only applicable for
 - Horizontal axis
 - 2+ cantilevered blades
 - Coordinated blade movement
 - Rigid hub
- Example: Load Case A

$$\Delta F_{\rm ZB} = 2 m_{\rm B} R_{\rm COg} \varpi_{\rm n,design}^2$$

$$\Delta F_{\rm X-shaft} = \frac{3}{2} \frac{\lambda_{\rm design} Q_{\rm design}}{R}$$

$$\Delta M_{\rm XB} = \frac{Q_{\rm design}}{B} + 2 m_{\rm B} g R_{\rm COg}$$

$$\Delta M_{\rm X-shaft} = Q_{\rm design} + 2 m_{\rm F} g e_{\rm F}$$

$$\Delta M_{\rm Shaft} = 2 m_{\rm F} g L_{\rm Tb} + \frac{R}{6} \Delta F_{\rm X-shaft}$$

Table 2 - Design load cases for the simplified load calculation method

Design situation		Load cases	Wind inflow	Type of analysis	Remarks	
Power production	Α	Normal operation		F		
	В	Yawing	$V_{\rm hub} = V_{\rm design}$	U		
	С	Yaw error	$V_{\rm hub} = V_{\rm design}$	U		
	۵	Maximum thrust	$V_{\rm hub}$ =2,5 $V_{\rm ave}$	U	Rotor spinning but could be furling or fluttering	
Power production plus occurrence of	E	Maximum rotational speed		U		
fault		Short at load connection	V _{hub} =V _{design}	U	Maximum short-circuit generato torque	
Shutdown	G	Shutdown (Braking)	$V_{\rm hub} = V_{\rm design}$	U		
Extreme wind Loading	Н	Extreme wind loading	V _{hub} =V _{e50}	U	The turbine may be parked (idling or standstill) or governing. No manual intervention has occurre	
Parked and fault conditions	_	Parked wind loading, maximum exposure	$V_{\rm hub} = V_{\rm ref}$	U	Turbine is loaded with most unfavourable exposure	
Transport, assembly, maintenance and repair	J	To be stated by manufacturer		U		

Key

F analysis of fatigue loads

U analysis of ultimate loads

Inputs and calculations

Description	Input Value	Units	Symbol	Description	Value	Units	Symbol
Air density	1.2250	kg/m^3	ρ	Design Wind Speed	10.50	m/s	V_design
Gravitational acceleration	9.8100	m/s^2	9	50 year extreme wind speed	52.50	m/s	V_e50
Reference Wind Speed	37.5000	m/s	V_ref	50yr extreme tip speed ratio	1.93	n/a	λ_e50
Average Wind Speed	7.5000	m/s	V_ave	Design Tip Speed Ratio	6.77	n/a	λ_design
Number of Blades	3	n/a	В	Drive Train Efficiency	0.60	n/a	á
Blade Tip Radius	0.9700	m	R	Design Torque	11.32	Ŋm	Q_design
Total Planform Area of the Blade	0.2310	m^2	A_groj,B	Projected Area (turbine swept area)	2.96	m^2	A_groj
Drag Coefficient of the Blades	1.5000	n/a	C_d	Design Rotational Speed of the Rotor	73.30	rad/s	ω_n,design
Max Lift Coefficient of the Blades	2.0000	n/a	C_I,max	Maximum Possible Rotor Speed	104.72	rad/s	ω_n,max
Thrust Coefficient	0.5000	n/a	C_T	Max Yaw Rate	2.99	rad/s	ω_yaw,max
Maximum Rotor Speed	1000.0000	rpm	n_max	50yr extreme tip speed ratio	1.93	n/a	λ_e50
Design Rotor Speed	700.0000	rpm	n_design	Ecentricity of the Rotor Centre of Mass	4.85E-03	m	e_r
Second Moment of Inertia for each Blade	0.0633	kgm^2	I_B	Effective brake torque	0.00	Nm	M_brake
Single Blade Mass	0.4000	kg	m_B	Cross Sectional Area of the Shaft	4.9087E-04	m^2	A_shaft
Rotor Mass (All Blades plus Hub)	3.9800	kg	m_r	The second moment of inertia for the shaft	1.9175E-08	m^4	l_x-shaft
Distance from Blade centre of gravity to rotor axis	0.3790	m	R_cog	Section modulus for the shaft	1.5340E-06	m^3	W_shaft
Distance Between Rotor Centre and First Bearing	0.0260	m	L_ <u>_</u>	Blade x-section modulus	3.0359E-06	m^3	W_xB
Distance Between the Rotor Centre and the yaw axis	0.2180	m	L_rt	Blade y-section modulus	1.5411E-04	m^3	W_yB
Gearbox Ratio (enter 1.0 for no gearbox)	1.0000	n/a	Gear	Number of Fatigue Cycles	2.21E+10	n/a	n_i
Enter "Y" if brake is on high speed side of gearbox, otherwise "N"	N	n/a	n/a				
Brake torque (enter 0.0 for no brake)	0.0000	Nm	M_brake				
Design Power	0.5000	kW	P_design				
Short Circuit Torque Factor	2.0000	n/a	G				
Type "Y" if blades are stationary during parking, otherwise "N"	Υ	n/a	n/a				
Diameter of the Shaft	2.5000E-02	m					
Cross Sectional Area of the Blade Root	1.4600E-03	m^2	A_B				
x for the blade	2.7900E-08	m^4	L _{XX} B				
x-distance from blade centroid to the maximum stress point	9.1900E-03	m	c_xB				
lyx for the blade	1.1990E-06	m^4	L _{XX} B				
y-distance from blade centroid to the maximum stress point	7.7800E-03	m	c_yB				
Ultimate Material Strength for the Blades	1.2000E+02	MPa	f kB		1.4.4		
Ultimate Material Strength for the Shaft	2.5000E+02	MPa	f k-shaft				
	20	Years	_				
Design life of the turbine	631152000	s	T_d		-		-
Number of Cycles to Failure as a Function of Stress (Shaft)	1.00E+10	n/a	N_shaft				
Number of Cycles to Failure as a Function of Stress (Blade)	1.23E+13	n/a	N blade				

SLM results

i											
	Loads from SLM										
Load Case A - Fatigue Loads on Blades and Rotor Shaft											
Equation	Description	Units	Symbol								
	Blade Loads										
9.4 (IEC 21)	Centrifugal Force at the Blade Root (z-axis)	1629.23	N	AE_zB							
9.5 (IEC 22)	Lead-lag Root Bending Moment (x-axis)	6.75	Ŋm	AM_xB							
9.6 (JEC 23)	Flapwise Root Bending Moment (y-axis)	25.55	Nm	AM_xB							
	Shaft Loads										
9.7 (JEC 24)	Thrust on shaft (x-axis)	118.55	N	ΔF_x-shaft							
9.8 (IEC 25)	Shaft Moment about x-axis	11.70	Nm	ΔM_x-shaft							
9.9 (IEC 26)	Shaft Moment	21.20	Nm	ΔM_shaft							
Load Case B ·	· Blade and Rotor Shaft Loads di	uring Yaw									
Equation	Description	SLM Value	Units	Symbol							
9.16 (IEC 28)	Flapwise Root Bending Moment (y-axis)	40.83	Ŋm	M_yB							
9.11,12 (JEC 29,30)	Bending moment on the shaft	61.81	Ŋm	M_shaft							
Load Case C ·	Yaw Error Load on Blades										
Equation	Description	SLM Value	Units	Symbol							
9.13 (JEC 31)	Flapwise Root Bending Moment (y-axis)	422.82	Nm	M_yB							
Load Case D ·	Maximum Thrust on Shaft										
Equation	Description	SLM Value	Units	Symbol							
9.14 (JEC 32)	Maximum Thrust on Shaft	318.25	N	F_x-shaft							
Load Case E -	Maximum Rotational Speed										

9.11,12 (JEC 29,30)	Bending moment on the shaft	61.81	Ŋm	M_shaft					
oad Case C -	Yaw Error Load on Blades								
Equation	Description	SLM Value	Units	Symbol					
9.13 (JEC 31)	Slapwise Root Bending Moment (y-axis) 422.82 Nm								
Load Case D - Maximum Thrust on Shaft									
Equation	Description	SLM Value	Units	Symbo					
9.14 (JEC 32)	Maximum Thrust on Shaft	318.25	N	F_x-shaf					
Load Case E -	Maximum Rotational Speed								
Equation	Description	SLM Value	Units	Symbo					
9.15 (JEC 33)	Centrifugal Force at the Blade Root (z-axis)	1662.48	N	F_zB					
9.16 (JEC 34)	Bending Moment on the shaft	6.52	Nm	M_shaft					
Load Case F -	Short at Load Connection								
Equation	Description	SLM Value	Units	Symbo					
9.17 (JEC 35)	Bending Moment on Shaft	22.64	Nm	M_x-shat					
9.18 (JEC 36)	Lead-lag Root Bending Moment (x-axis)	7.55	Nm	M_xB					
Load Case G -	Shutdown Braking								
Equation	Description	SLM Value	Units	Symbo					
9.19 (JEC 37)	Bending Moment on Shaft	n/a	Nm	M_x-shat					
9.20 (JEC 38)	Lead-lag Root Bending Moment (x-axis)	n/a	Ŋm	M_xB					
Load Case H -	Parked Wind Loads during Idlin	g							
Equation	Description	SLM Value	Units	Symbo					
9.23,24 (JEC 39,40)	Flapwise Root Bending Moment (y-axis)	283.71	Ŋm	М_ұВ					
	Maximum Thrust on Shaft	1754.89	N	F x-shaf					

SLM applicability and safety factors

	Micro wind turbines up to 1 kW Peak Power	1-30 kW Peak Power	30-65 kW Peak Power	65-150 kW Peak Power
STRUCTURAL	L DESIGN			
SLM	Not required	Not recommended for turbines with Peak Power greater than 10 kW	Not allowed	Not allowed
Aeroelastic model	Not required	Allowed with validation through power, rotor speed. Validate weight of major components.	Allowed with validation through power, rotor speed, blade first flapwise (static) natural frequency*. Validate weight of major components.	Allowed with validation through power, rotor speed, blade first flapwise (static) natural frequency, tower loads*. Validate weight of major components.
Structural Analysis	Not required	Required	Required	Required

Table 7 - Partial safety factors for loads

ı	oad determination method (see 5.2)	Fatigue loads, $\gamma_{\rm f}$	Ultimate loads, $\gamma_{\rm f}$
1.	Simplified equations	1,0	3,0
2.	Simulation model	1,0	1,35
3.	Full scale load measurement	1,0	3,0

Ref. International Electrotechnical Commission, Wind turbines - Part 2: Small wind turbines, EN 61400-2:2014.



Ref. ANSI/ACP 101-1 2021 The Small Wind Turbine Standard

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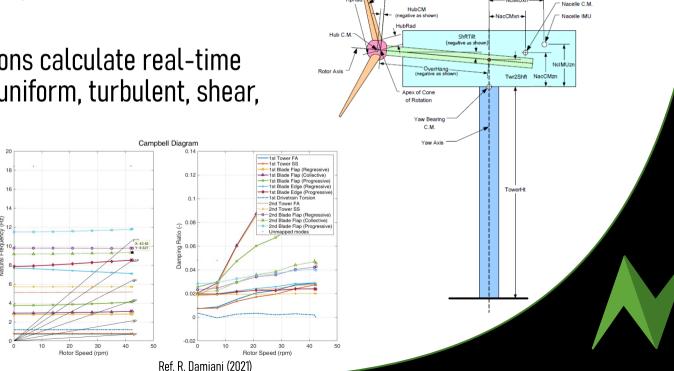
Aeroelastic modeling

 Combines aerodynamics, structural dynamics, and controls into a single integrated simulation for holistic analysis

 Time marching simulations calculate real-time response to any inflow: uniform, turbulent, shear,

gusts

 Captures structural dynamics and vibration mode coupling



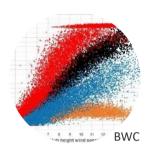
Precone

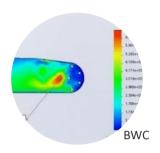
negative as shown)

Ref. FAST User's Guide, Jonkman, Buhl.

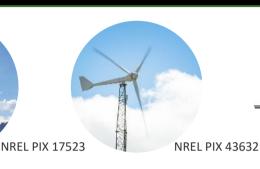
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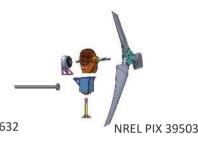
Aeroelastic modeling pros & cons











Understand the load and power behavior of the turbine before witnessing it in the field

Control parameters that have the highest impact on design

Optimize the configuration most efficiently

Provide a more realistic basis for design certification

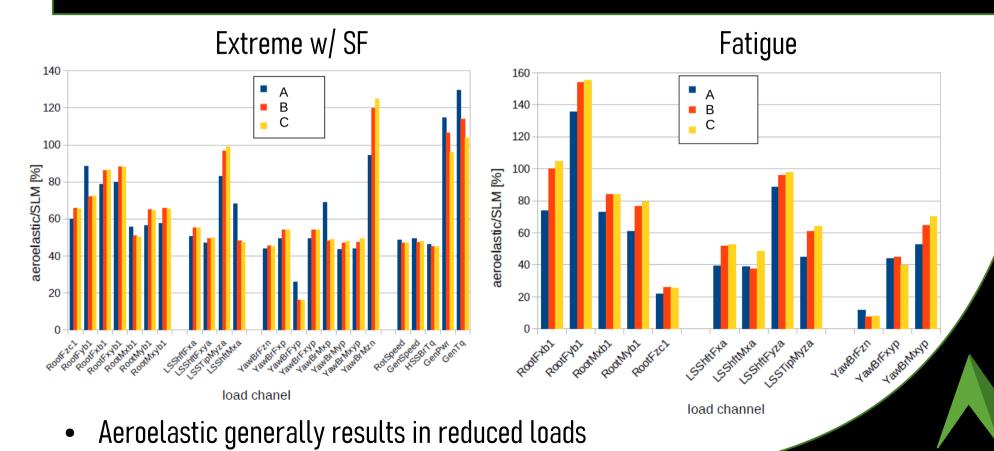
Simplify conformity assessment following a change in the turbine architecture

Ref. R. Damiani, D. Davis, B. Summerville (2021): Aeroelastic Modeling for Distributed Scale Wind Turbines.

Disadvantages

- Mostly HAWT-centric
- Steep learning curve, labour intensive
- Computationally expensive
- License fee for some codes

Aeroelastic vs. SLM



Tests to verify design data and validate model

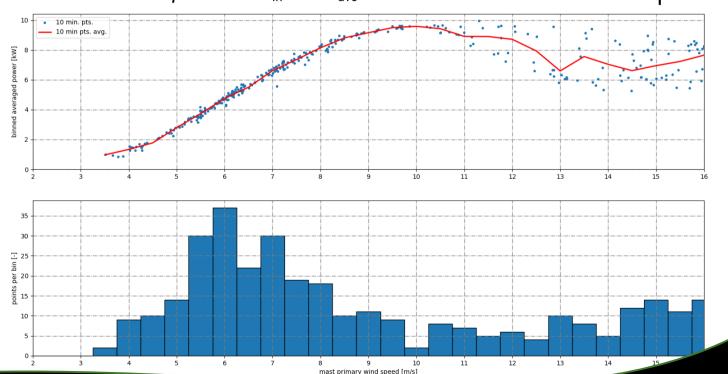
According to ANSI/ACP-101-1

		Desigr	values @	<u>1.4V_{ave}</u>	maxin	nums		Blade first		
		power	Rotor speed	Shaft torque*	Rotor speed	Yaw rate	/aw weights of flapwise (s major natura		Tower loads	
SL	М	χ	Χ	Χ	Χ	Χ				
	1 – 30 kW	X	X	X	X	X	X			
Aeroelastic	30 – 65 kW	Х	Х	Х	Х	Х	X	Х		
	65 – 150 kW	Х	Х	Х	Х	Х	X	X	X	

^{*}May be calculated from power and rotor speed

Validation measurements requirements

- Measured data shall be binned into 0.5 m/s wind speed bins
- Each bin from 1 m/s below V_{in} to 2V_{ave} shall contain at least 10 data points



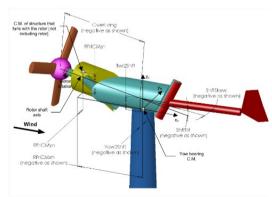
Validation measurements requirements

- Max yaw rate
 - Passive yaw: Measured value cannot be used for SLM (use 61400-2 eq. 27)
 - Semi-active / damped yaw
 - Measured value may be used in SLM
 - Must see an upper limit in measured values
- Max rotor speed
 - Shall be measured during condition most likely to give highest speed (e.g. loss of load or wind gust)
 - Wind speeds from 10 m/s 20 m/s
 - 2h of data
 - At least 1/2 h below 15 m/s and 1/2 h above
 - $-\,\,$ Max speed shall be extrapolated to V_{ref}

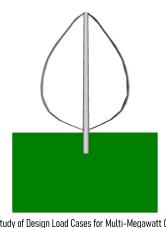


Aeroelastic modeling – Code options

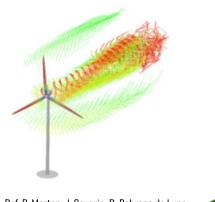
	OpenFAST	HAWC2	MSC.Adams	Bladed	QBlade	Flex5	OWENS	SimPack	SamCef	ASHES	alaska/ Wind
HAWT	Х	X	Х	χ	Х	Х		Х	Х	χ	Х
VAWT		Х			Х		Х				
General purpose			Х					Х	Х		Х
free	Х	trial available			trial available					trial available	



Ref. FAST User's Guide, Jonkman, Buhl, 2005.

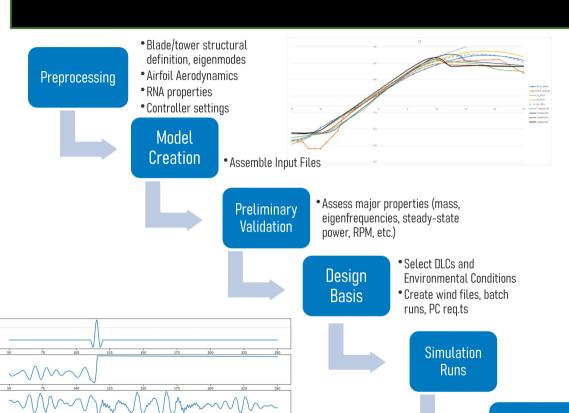


Ref. "Study of Design Load Cases for Multi-Megawatt Onshore Vertical Axis Wind Turbines", DTU Wind Energy, June 2015.



Ref. D. Marten, J. Saverin, R. Behrens de Luna, S. Perez-Becker. 2021.

Aeroelastic modeling workflow



Design situation	DLC	Wit	nd condition	Other conditions	Type of analysis
1) Power production	1.1	NTM	$V_{\rm in} < V_{\rm hub} < V_{\rm out}$ or $3 \times V_{\rm ave}$		F, U
	1.2	ECD	V _{hub} < V _{design}		U
	1.3	EOG ₅₀	$V_{\rm in} < V_{\rm hub} < V_{\rm out}$ or $3 \times V_{\rm ave}$		U
	1.4	EDC ₅₀	$\begin{array}{c} v_{\rm in} < v_{\rm hub} \\ < v_{\rm out} \ {\rm or} \ 3 \times v_{\rm ave} \end{array}$		U
	1.5	ECG	$V_{\rm hub} = V_{\rm design}$		U
Power production plus occurrence of fault	2.1	NWP	$v_{\text{hub}} = v_{\text{design}}$ or v_{out} or $2,5 \times v_{\text{ave}}$	Control system fault	U
	2.2	NTM	$v_{\rm in} < v_{\rm hub} < v_{\rm out}$	Control or protection system fault	F, U
	2.3	EOG ₁	$V_{\text{in}} < V_{\text{out}}$ or $2,5 \times V_{\text{ave}}$	Loss of electrical connection	U
3) Normal shutdown	3.1	NTM	$V_{\rm in} < V_{\rm hub} < V_{\rm out}$		F
	3.2	EOG ₁	V _{hub} = V _{out} or V _{max,shutdown}		U
4) Emergency or manual shutdown	4.1	NTM	To be stated by the manufacturer		U
5) Extreme wind loading (standing still or idling; or spinning)	5.1	EWM	$V_{\text{hub}} = V_{\text{e50}}$	Possible loss of electrical power network	U
	5.2	NTM	$V_{\rm hub} < 0.7 V_{\rm ref}$		F
6) Parked and fault condition	6.1	EWM	$v_{\rm hub}$ = $v_{\rm e1}$		U
7) Transport, assembly, maintenance and repair	7.1	To be s	tated by the		U

- Extract ULS, FLS, SLS driving loads, deflections, etc.
- Assess resonance & instability risk

Ref. R. Damiani (2021)

Postprocessing

Publicly available models

Archetype coverage table (HAWTs)

Active Yaw	Passive Yaw	Stall	Pitch	VarSpd	FixedSpd	Down- Wind	Up-Wind	
			✓	✓	✓		✓	Active Yaw
		✓		✓	✓	✓	✓	Passive Yaw
				✓	✓	✓	✓	Stall
				✓		✓	✓	Pitch
						✓	✓	VarSpd
						✓	✓	FixedSpd
								Down-Wind
								Up-Wind

Where:

Gray = N/A

Green = common in the current market

Yellow = rare in the current market

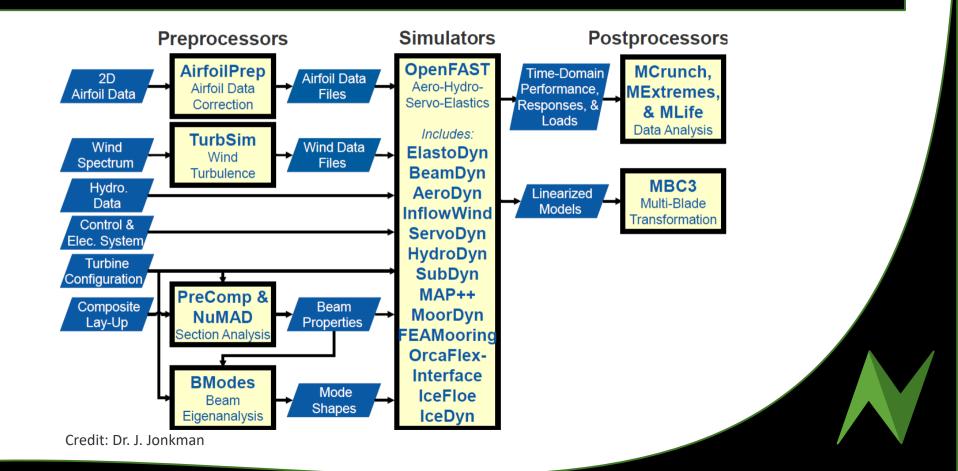
White = not seen in the current market

✓ = aeroelastic model template available

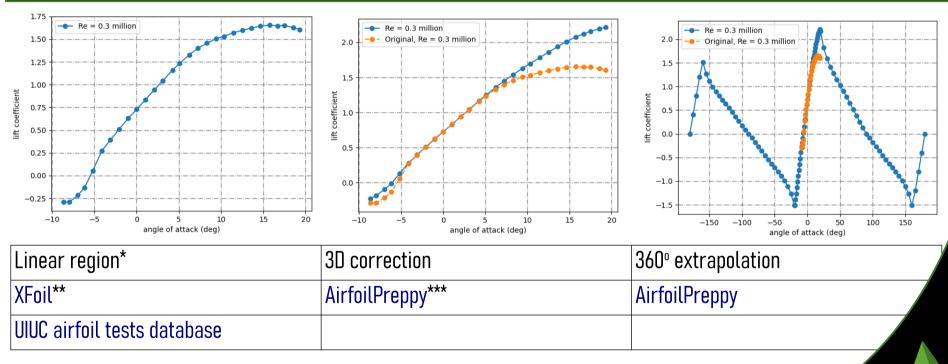
Ref. R. Damiani, D. Davis, B. Summerville (2021): Aeroelastic Modeling for Distributed Scale Wind Turbines.

- Other features included
 - Furling
 - Teetering
 - Tip brakes
 - Tail
 - Guyed tower
 - Lattice tower

OpenFAST workflow



Preprocessing – airfoil data

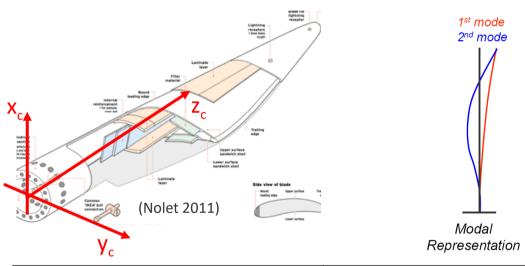


^{*} Use data at correct Reynolds number(s)

** Be sure of data at low Reynolds numbers (<5E5). Measurements are best.

*** Also calculates unstable aerodynamics model coefficients

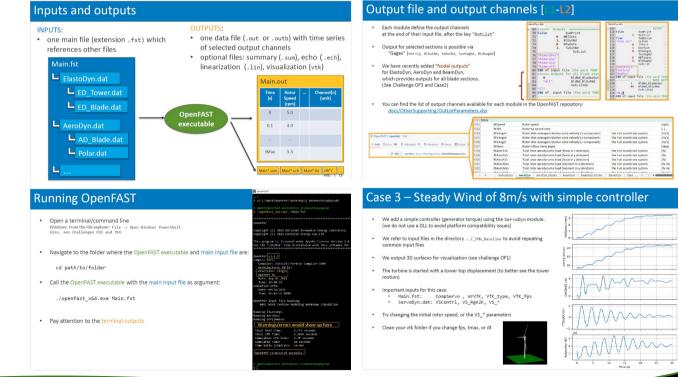
Preprocessing – structure files



Cross-sectional properties	Eigenfrequencies and mode shapes
PreComp	BModes
VABS	FEM
Sonata	Mode shape polynomial curve fitting

Running OpenFAST

Excellent material for learning OpenFAST from NAWEA 2022 OpenFAST workshop



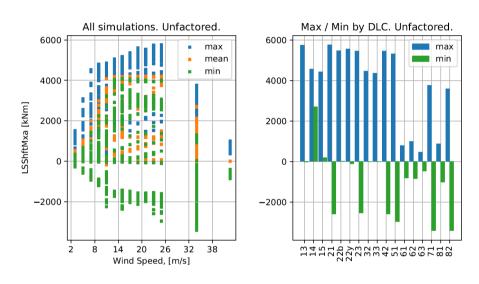
Modeling trip ups

- Time step
- Initial conditions
- Aerodynamic models
 - Disable induction when parked/idling
 - Be aware of high AOAs and yaw errors
- Airfoil polars
 - 3D correction
 - 360° extrapolation

- Drivetrain frequency and damping
- Structural data issues
 - Tune mass, CM, natural frequencies to match reference data
 - Mode shapes
- Geometry and topology
 - Use visualization tools to check

• The NREL forum is full of great tips and support from the developers

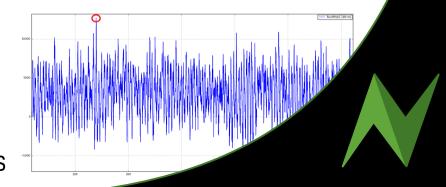
Postprocessing – Ultimate limit state (ULS)



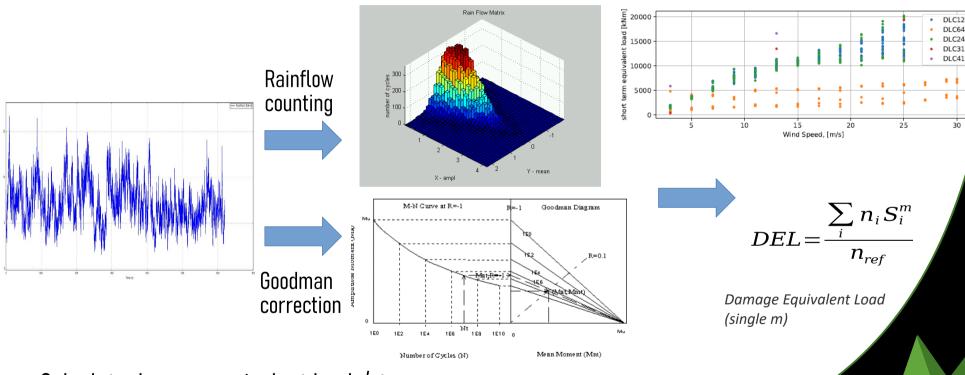
Contemporaneous load table: Blade 1 Root, Unfactored.

			RootFxc1	RootFyc1	RootFzc1	RootFxyc1	RootMxc1	RootMyc1	RootMzc1	RootMxyc1
			kN	kN	kN	kN	kNm	kNm	kNm	kNm
RootFxc1	Max	DLC22y_10020_19_300	4.84e+02	-1.89e+02	4.36e+02	5.19e+02	4.82e+03	1.78e+04	-7.61e+01	1.84e+04
RootFxc1	Min	DLC23_EOGO_55	-3.38e+02	5.74e+01	8.64e+02	3.43e+02	-3.33e+03	-1.40e+04	1.85e+02	1.44e+04
RootFyc1	Max	DLC62_12008_42.5_300	4.50e+01	4.40e+02	-1.49e+02	4.42e+02	-1.18e+04	6.94e+02	1.59e+02	1.18e+04
RootFyc1	Min	DLC62_12003_42.5_45	-7.26e+01	-4.84e+02	-1.70e+02	4.89e+02	1.30e+04	-1.91e+03	-3.95e+01	1.32e+04
RootFzc1	Max	DLC42_EOGO_56	-4.83e+00	-8.41e+01	1.07e+03	8.42e+01	5.42e+01	-2.63e+03	-1.27e+02	2.63e+03
RootFzc1	Min	DLC71_13002_34_30_0	-4.12e+01	-2.74e+02	-1.81e+02	2.77e+02	9.62e+03	-1.43e+03	1.88e+01	9.72e+03
RootFxyc1	Max	DLC22y_10023_25_300	4.65e+02	-2.55e+02	4.88e+02	5.30e+02	6.72e+03	1.64e+04	-5.83e+01	1.77e+04
RootFxyc1	Min	DLC71_13005_34_210_30	-3.73e-04	1.78e-02	-1.46e+02	1.79e-02	-1.01e+03	1.39e+02	9.19e+01	1.02e+03
RootMxc1	Max	DLC62_12003_42.5_45	-7.28e+01	-4.83e+02	-1.70e+02	4.89e+02	1.30e+04	-1.91e+03	-3.98e+01	1.32e+04
RootMxc1	Min	DLC62_12006_42.5_270	3.35e+01	4.38e+02	-1.60e+02	4.39e+02	-1.26e+04	6.75e+02	2.28e+02	1.26e+04
RootMyc1	Max	DLC22y_10020_19_300	4.84e+02	-1.89e+02	4.36e+02	5.19e+02	4.82e+03	1.78e+04	-7.61e+01	1.84e+04
RootMyc1	Min	DLC23_EOGO_55	-3.36e+02	5.00e+01	8.69e+02	3.40e+02	-3.12e+03	-1.41e+04	1.89e+02	1.44e+04
RootMzc1	Max	DLC62_12003_42.5_225	1.20e+01	3.96e+02	-1.68e+02	3.96e+02	-1.16e+04	4.28e+02	3.41e+02	1.17e+04
RootMzc1	Min	DLC62_12010_42.5_150	-8.92e+01	-3.53e+02	-1.72e+02	3.65e+02	1.03e+04	-1.72e+03	-3.33e+02	1.05e+04
RootMxyc1	Max	DLC22y_10020_19_300	4.84e+02	-1.89e+02	4.36e+02	5.19e+02	4.82e+03	1.78e+04	-7.61e+01	1.84e+04
RootMxyc1	Min	DLC21_10033_21_350	9.53e+00	-2.70e+01	-1.54e+02	2.86e+01	-3.77e-01	-1.79e-01	-1.88e+01	4.17e-01

- Extract ultimate loads, deflections, clearance
 - MExtremes or Pcrunch
- Contemporaneous loads tables
- Apply binning, safety factors according to standards

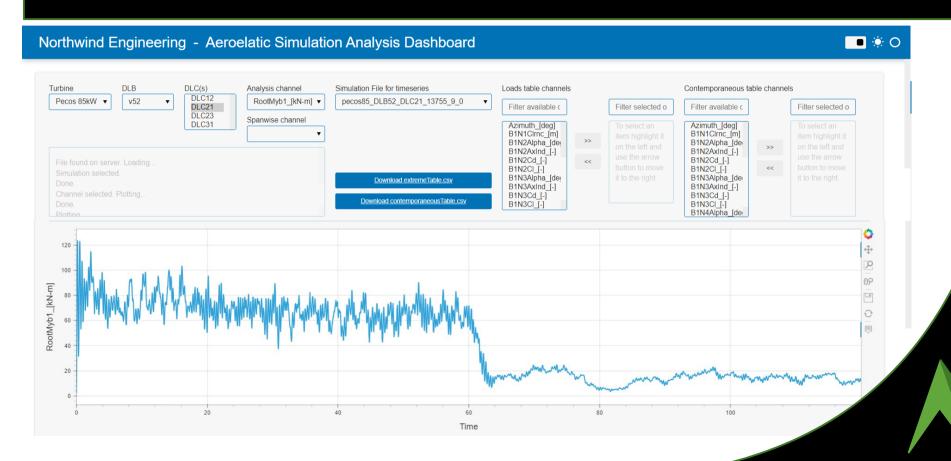


Postprocessing – Fatigue limit state (FLS)

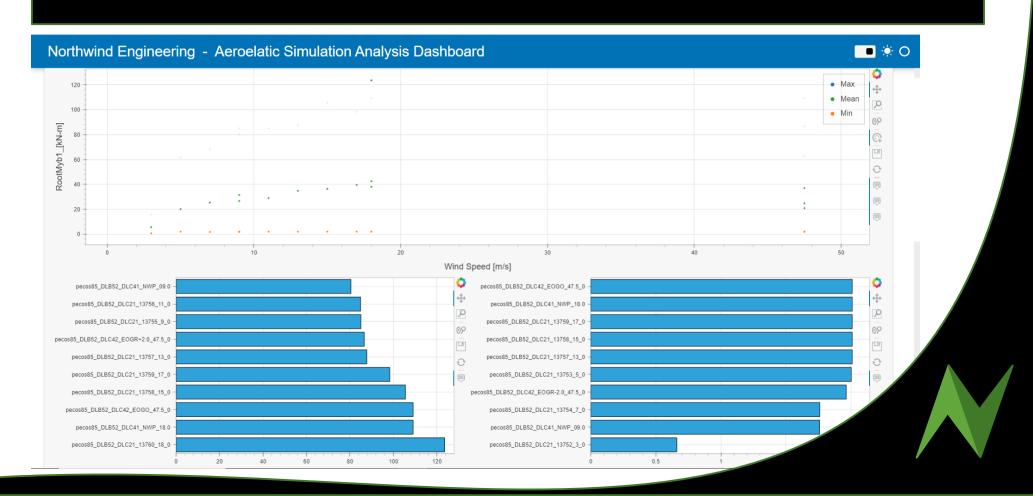


- Calculate damage equivalent loads/stresses
 - MLife or openfast-toolbox

Interactive simulations analysis dashboard

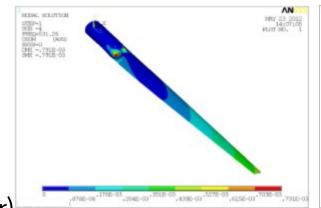


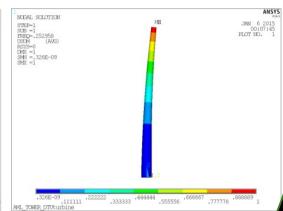
Interactive simulations analysis dashboard

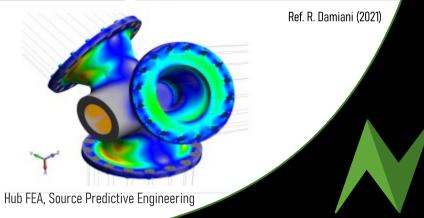


Structural verification of components

- Things to watch out for:
 - Sensitivity to Mesh
 - Boundary Conditions
 - Load Distribution
 - Failure Criteria (e.g. Tsai-Wu)
 - Buckling (linear vs. nonlinear)
 - Welds and stress concentrations
 - Bolts





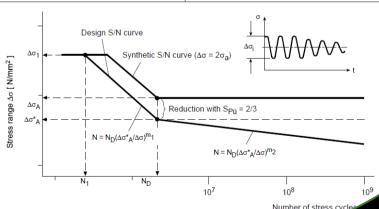


Structural verification of components

Analytical options

	Circular blade root	Rectangular blade root	Rotor shaft
Axial load	$\sigma_{zB} = \frac{F_{zB}}{A_{B}}$	$\sigma_{zB} = \frac{F_{zB}}{A_{B}}$	$\sigma_{\rm X-shaft} = \frac{F_{\rm X-shaft}}{A_{\rm shaft}}$
Bending	$\sigma_{MB} = \frac{\sqrt{M_{xB}^2 + M_{yB}^2}}{W_{B}}$	$\sigma_{MB} = \frac{M_{XB}}{W_{XB}} + \frac{M_{YB}}{W_{YB}}$	$\sigma_{ extsf{M-shaft}} = rac{M_{ extsf{shaft}}}{W_{ extsf{shaft}}}$
Shear	Negligible	Negligible	$ au_{M-shaft} = rac{M_{X-shaft}}{2W_{shaft}}$
Combined (axial + bending)	$\sigma_{\sf eqB} = \sigma_{\sf zB} + \sigma_{\sf MB}$		$\sigma_{\text{eq}} = \sqrt{(\sigma_{\text{x-shaft}} + \sigma_{\text{M-shaft}})^2 + 3\tau_{\text{M-shaft}}^2}$

- Evaluate damage and check for safety
 - Eurocodes, AISC
 - GL Guideline for the certification of wind turbines



Other useful tools

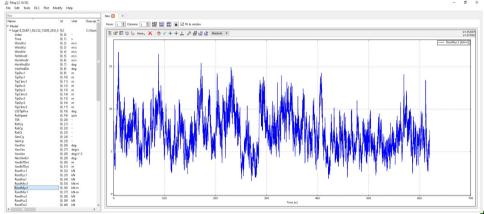
- Scripts to setup models, run simulations and postprocess the results
 - openfast_toolbox

DTU Wind Energy Toolbox

- Visualization of simulation results (and more)
 - PyDatView

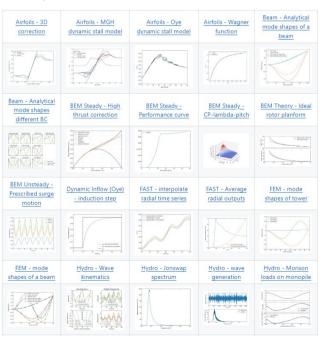
pyDatView v0.2 File Data Tools Help Format: auto (any supported file) (.*) = metData sonic10m w sonic32m wa sonic18m ws sonic45m t sonic45m wd sonic45m wd std sonic45m temp sonic45m z L sonic45m ProcFlag sonic45m sampNum sonic45m sampFreq sonic58m time sonic58m u sonic58m v sonic58m w sonic58m ti sonic58m wd sonic58m wd std sonic58m temp sonic58m z L sonic58m ProcFlag (Regular Scatter sonic58m sampNum OFFT sonic58m sampFreq Compare atmo time BP02m BP30m RH02m 9.1013 RH30m 2.1253 11.3655 0.3401 663 RH56m 91x6636

Pdap



Other useful tools

- Wind Energy Library (welib)
 - Suite of python and matlab tools aerodynamics, controls, structure/elasticity



WISDEM

- A set of models for assessing overall wind plant cost of energy (COE)
- Component and system optimization

